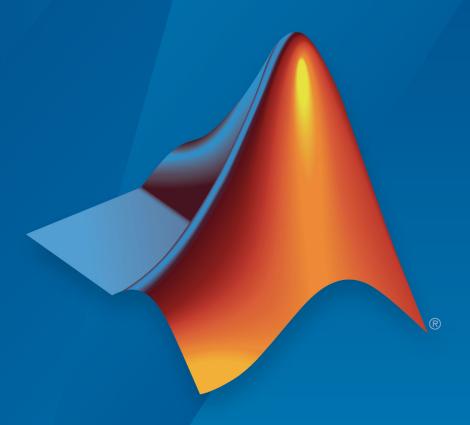
# Simscape™ Driveline™

Reference



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Simscape ™ Driveline ™ Reference

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#### **Revision History**

September 2010	Online only	New for Version 2.0 Beta (Release 2010b+)
April 2011	Online only	Revised for Version 2.0 (Release 2011a)
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March 2018	Online only	Revised for Version 2.14 (Release 2018a)

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# **Blocks — Alphabetical List**

# 4-Speed CR-CR

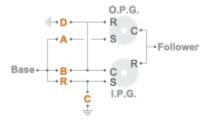
Clutch schedule for a four-speed carrier ring-carrier ring transmission **Library:** Transmissions



# **Description**

The 4-Speed CR-CR block consists of two planetary gear sets and five disk friction clutches. The follower shaft connects to the planet gear carrier of the output planetary gear and the ring gear of the input planetary gear. The clutches are configured to implement four ratios, one reverse ratio, and neutral. The reverse clutch and two of the clutches determine which gears the base shaft connects to. The other two clutches act as brakes, grounding various gears of the planetary sets to the transmission housing.

This diagram shows a four-speed carrier ring-carrier ring transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram.



Label	Component
I.P.G.	Input planetary gear
O.P.G.	Output planetary gear
R	Ring gear

Label	Component
С	Planet gear carrier
S	Sun gear
R	Reverse clutch
A-B	Forward clutches that control the power flow path
C-D	Forward, braking clutches

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_1 = \frac{N_{RI}}{N_{SI}},$$

and

$$g_2 = \frac{N_{RO}}{N_{SO}},$$

where:

- $N_{\mathrm{RI}}$  is the number of teeth in the planetary ring gear on the input shaft side.
- $N_{\rm SI}$  is the number of teeth in the planetary sun gear on the input shaft side.
- $N_{\mathrm{RO}}$  is the number of teeth in the planetary ring gear on the output shaft side.
- $N_{\rm SO}$  is the number of teeth in the planetary sun gear on the output shaft side.

The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the power-flow diagrams for each gear of the 4-Speed CR-CR block.

The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of 0 an unlocked state. The clutch schedule generates these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

The power-flow diagrams show the power flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear	Clu	itch	Sch	ned	ule	Drive Ratio Equation	Default Ratio	Power Flow
4	<b>A</b> 0		1			$\frac{g_1}{1+g_1}$	0.67	Base B C S I.P.G.
3	1	1	0	0	0	1	1	Base B C S I.P.G.
2	1	0	1	0	0	$\frac{g_1+g_2}{1+g_1}$	1.67	Base B C Follower

Gear	Cluto	ch Sc	hed	ule	Drive Ratio Equation	Default Ratio	Power Flow
1	1 0	) 0	1	0	$g_2$	3	Base B C C Follower C S I.P.G.
R	0 0	) 0	1	1	-g <sub>1</sub>	-2	Base B C Follower

# **Ports**

# Input

### Gear — Numerical input for the gear

scalar

Specify -1 for reverse, 0 for neutral, and 1-4 for the forward gears.

Data Types: single | double

# **Conserving**

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### F — Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

## **Parameters**

#### Initial gear — Gear state at the beginning of simulation

Neutral (default) | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

# See Also

10-Speed | 4-Speed Ravigneaux | 6-Speed Lepelletier | 7-Speed Lepelletier | 8-Speed | 9-Speed

#### Introduced in R2015a

# **4-Speed Ravigneaux**

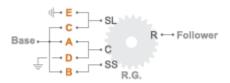
Clutch schedule for a four-speed Ravigneaux transmission **Library:** Transmissions



# **Description**

The 4-Speed Ravigneaux block consists of one Ravigneaux gear set and five clutches. The follower shaft connects to the ring gear of the Ravigneaux set. Three of the clutches determine the gears that the base shaft connects to for power transfer. The other two clutches serve as brakes, grounding various gears of the Ravigneaux set to the transmission housing.

This diagram shows a four-speed Ravigneaux gear transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram.



Label	Component
R.G.	Ravigneaux gear
R	Ring gear
C	Planet gear carrier
SL	Large sun gear
SS	Small sun gear
A-C	Forward clutches that control the power flow path

Label	Component
D-E	Forward, braking clutches

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_1 = \frac{N_R}{N_{SL}},$$

and

$$g_2 = \frac{N_R}{N_{SS}},$$

where:

- $N_R$  is the number of teeth in the Ravigneaux ring gear.
- $N_{\rm SL}$  is the number of teeth in the Ravigneaux large sun gear.
- $N_{\rm SS}$  is the number of teeth in the Ravigneaux small sun gear.

The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the power-flow diagrams for each gear of the 4-Speed Ravigneaux block.

The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of  $\theta$  an unlocked state. The clutch schedule generates these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

The power-flow diagrams show the power flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear Clutch Schedule	Drive Ratio Equation	Default Ratio	Power Flow
A B C D R			

Gear	Clu	itch	Sch	ned	ule	Drive Ratio Equation	Default Ratio	Power Flow
4	1	0	0	0	1	$\frac{g_1}{1+g_1}$	0.67	Base A C R Follower
3	1	1	0	0	0	1	1	Base A C R Follower
2	0	1	0	0	1	$\frac{g_1+g_2}{1+g_1}$	1.67	Base A C R Follower R.G.
1	0	1	0	1	0	$g^{}_2$	3	Base A C R Follower
R	0	0	1	1	0	-g <sub>1</sub>	-2	Base A C SI SS R.G.

# **Ports**

## Input

#### Gear — Numerical input for the gear

scalar

Specify -1 for reverse, 0 for neutral, and 1-4 for the forward gears.

Data Types: single | double

# Conserving

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### F - Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

# **Parameters**

## Initial gear — Gear state at the beginning of simulation

Neutral (default) | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

# **See Also**

10-Speed | 4-Speed CR-CR | 6-Speed Lepelletier | 7-Speed Lepelletier | 8-Speed | 9-Speed

#### Introduced in R2015a

# 6-Speed Lepelletier

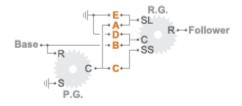
Clutch schedule for a six-speed Lepelletier transmission **Library:** Transmissions



# **Description**

The 6-Speed Lepelletier consists of one planetary gear set, one Ravigneaux gear set, and five disk friction clutches. The transmission base shaft connects to the ring gear of the planetary gear set. The follower shaft connects to the ring gear of the Ravigneaux gear set. Three of the clutches control the power flow paths between the planetary and Ravigneaux gear sets. The other two clutches serve as brakes, grounding various gears of the Ravigneaux set to the transmission housing.

This diagram shows a six-speed Lepelletier transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram.



Label	Component
P.G.	Planetary gear
R.G.	Ravigneaux gear
R	Ring gear
С	Planet gear carrier

Label	Component
S	Sun gear
SL	Large sun gear
SS	Small sun gear
A-C	Forward clutches that control the power flow path
D-E	Forward, braking clutches

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_1 = \frac{N_{PR}}{N_{PS}},$$

$$g_2 = \frac{N_{PR}}{N_{RSL}},$$

and

$$g_3 = \frac{N_{RR}}{N_{RSS}},$$

where:

- $N_{\rm PR}$  is the number of teeth in the planetary ring gear.
- $N_{\mathrm{PS}}$  is the number of teeth in the planetary sun gear.
- $N_{
  m RR}$  is the number of teeth in the Ravigneaux ring gear.
- $N_{\rm RSL}$  is the number of teeth in the Ravigneaux large sun gear.
- $N_{\rm RRS}$  is the number of teeth in the Ravigneaux small sun gear.

The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the power-flow diagrams for each gear of the 6-Speed Lepelletier block.

The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of 0 an unlocked state. The clutch schedule generates

these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

The power-flow diagrams show the power flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear	Clu	itch	Sc	hed	lule	Drive Ratio Equation	Default Ratio	Power Flow
6		<b>B</b>			1	$\frac{g_2}{1+g_2}$	0.69	Base R Follower
5	1	1	0	0	0	$\frac{g_2}{g_2 + 1 / (1 + g_1)}$	0.87	Base R Follower
4	0	1	1	0	0	$\frac{g_{3}\left(1+g_{1}\right)}{g_{3}\left(1+g_{1}\right)-1}$	1.14	Base R-Follower

Gear	Clu	ıtch	Sc	hed	lule	Drive Ratio Equation	Default Ratio	Power Flow
3	1	0	1	0	0	$\frac{1+g_1}{g_1}$	1.50	Base R-Follower SS P.G.
2	0	0	1	0	1	$\frac{(1+g_1)(g_3+g_2)}{g_1(1+g_2)}$	2.31	Base R-Follower SS P.G.
1	0	0	1	1	0	$\frac{g_{3}\left(1+g_{1}\right)}{g_{1}}$	4.12	Base R-Follower  Base R-Follower  B-SS  P.G.
R	1	0	0	1	0	$-\frac{g_2\left(1+g_1\right)}{g_1}$	-3.36	Base R-Follower SS P.G.

## **Ports**

## Input

#### Gear — Numerical input for the gear

scalar

Specify -1 for reverse, 0 for neutral, and 1-6 for the forward gears.

Data Types: single | double

# Conserving

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### F — Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

# **Parameters**

### Initial gear — Gear state at the beginning of simulation

Neutral (default) | 6 | 5 | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

# **See Also**

10-Speed | 4-Speed CR-CR | 4-Speed Ravigneaux | 7-Speed Lepelletier | 8-Speed | 9-Speed

#### Introduced in R2017a

# 7-Speed Lepelletier

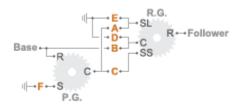
Clutch schedule for a seven-speed Lepelletier transmission **Library:** Transmissions



# **Description**

The 7-Speed Lepelletier block consists of one planetary gear set, one Ravigneaux gear set, and six disk friction clutches. The transmission base shaft connects to the ring gear of the planetary gear set. The follower shaft connects to the ring gear of the Ravigneaux gear set. Three of the clutches control the power-flow paths between the planetary and Ravigneaux gear sets. The other three clutches serve as brakes, grounding various gears of the Ravigneaux set to the transmission housing.

This diagram shows a seven-speed Lepelletier transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram.



Label	Component
P.G.	Planetary gear
R.G.	Ravigneaux gear
R	Ring gear
C	Planet gear carrier

Label	Component
S	Sun gear
SL	Large sun gear
SS	Small sun gear
A-C	Forward clutches that control the power-flow path
D-F	Forward, braking clutches

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_1 = \frac{N_{PR}}{N_{PS}},$$

$$g_2 = \frac{N_{RR}}{N_{RSL}},$$

and

$$g_3 = \frac{N_{RR}}{N_{RSS}},$$

#### where:

- $N_{\rm PR}$  is the number of teeth in the planetary ring gear.
- $N_{\rm PS}$  is the number of teeth in the planetary sun gear.
- $N_{\rm RR}$  is the number of teeth in the Ravigneaux ring gear.
- $N_{\mathrm{RSL}}$  is the number of teeth in the Ravigneaux large sun gear.
- $N_{\mathrm{RSS}}$  is the number of teeth in the Ravigneaux small sun gear.

The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the power-flow diagrams for each gear of the 7-Speed Lepelletier block.

The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of 0 an unlocked state. The clutch schedule generates

these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

The power-flow diagrams show the power-flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear	C	lut	ch S	Sch	edu	le	Drive Ratio Equation	Defaul Ratio	
7				<b>D</b> 0		<b>F</b>	$\frac{g_2}{1+g_2}$	0.70	Base R Follower
6	1	1	0	0	0	1	$\frac{g_{3}\left(1+g_{1}\right)}{g_{2}\left(1+g_{1}\right)+1}$	0.86	Base R-Follower  Base R-Follower  B-SS  R-Follower
5	1	1	1	0	0	0	1	1	Base R Follower

Gear	Clutch Schedule			ch Schedule			Drive Ratio Equation	Defaul Ratio	
4	0	1	1	0	0	1	$\frac{g_{3}\left(1+g_{1}\right)}{g_{3}\left(1+g_{1}\right)-1}$	1.17	Base R-Follower B-SS R-Follower P-S P.G.
3	1	0	1	0	0	1	$\frac{1+g_1}{g_1}$	1.63	Base R Follower P.G.
2	0	0	1	0	1	1	$\frac{\left(1+g_{1}\right)\!\left(g_{3}+g_{2}\right)}{g_{1}\!\left(1+g_{2}\right)}$	2.43	Base R Follower
1	0	0	1	1	0	1	$\frac{g_{3}\left(1+g_{1}\right)}{g_{1}}$	4.31	Base R-Follower  Base R-Follower  Base R-Follower  Base R-Follower  Base R-Follower

Gear	Clutch Schedule	Drive Ratio Equation	Default Ratio	Power Flow
R	<b>1</b> 0 0 <b>1</b> 0 <b>1</b>	$-\frac{g_{2}\left(1+g_{1}\right)}{g_{1}}$	-3.82 Base LR	R.G. R Follows

# **Ports**

## Input

#### **Gear** — **Numerical input for the gear**

scalar

Specify -1 for reverse, 0 for neutral, and 1-7 for the forward gears.

Data Types: single | double

# **Conserving**

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### F — Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

# **Parameters**

Initial gear — Gear state at the beginning of simulation

Neutral (default) | 7 | 6 | 5 | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

# See Also

10-Speed | 4-Speed CR-CR | 4-Speed Ravigneaux | 6-Speed Lepelletier | 8-Speed | 9-Speed

#### Introduced in R2015a

# 8-Speed

Clutch schedule for an eight-speed transmission **Library:** Transmissions



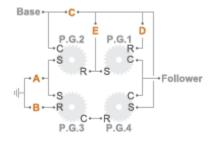
# **Description**

The 8-Speed block consists of four planetary gear sets and five clutches. The base shaft connects to the:

- Planet gear carrier of the second planetary gear
- Other gears through three clutches that determine the power flow path.

The follower shaft connects to the planet gear carrier of the first and fourth planetary gears. The other two clutches serve as brakes, grounding various gears of planetary sets two and three to the transmission housing.

This diagram shows an eight-speed transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram.



Label	Component
P.G.1-P.G.4	Planetary gears, 1-4

Label	Component
R	Ring gear
С	Planet gear carrier
S	Sun gear
С-Е	Forward clutches that control the power flow path
A-B	Forward, braking clutches

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_x = \frac{N_{R_x}}{N_{S_x}},$$

#### where:

- $N_{R_x}$  is the number of teeth in the planetary ring gear x, where x = 1, 2, and 3.
- $N_{S_x}$  is the number of teeth in the planetary sun gear x, where x = 1, 2, and 3.

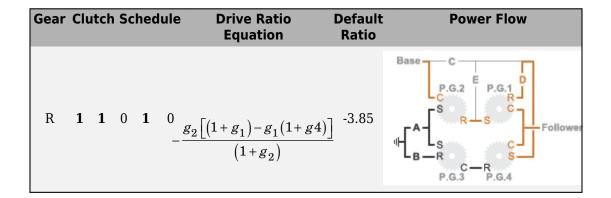
The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the power-flow diagrams for each gear of the 8-Speed block. The schedule and gear ratios are based on the manufacturer data for the GM 8L90 eight-speed automatic transmission.

The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of 0 an unlocked state. The clutch schedule generates these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

The power-flow diagrams show the power flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear	Clu	itch	Sc	hec	dule	Drive Ratio Equation	Default Ratio	Power Flow
8		0			E 1	$rac{g_2}{1+g_2}$	0.68	Base C P.G.1 D Follower S R S P.G.4
7	1	0	1	1	0	$\frac{g_{2}\!\left(1\!+\!g_{1}\right)}{1\!+\!g_{2}\!\left(1\!+\!g_{1}\right)}$	0.85	Base C P.G.1 P.G.2 Follower P.G.3 P.G.4
6	0	0	1	1	1	1	1	Base C P.G.2 P.G.1 P.G.2 Follower P.G.3 P.G.4
5	0	1	1	1	$\frac{\binom{0}{1+\varrho}}{\binom{1}{\varrho}}$	$egin{align} & (g_3) (1 + g_4) (g_2 g_4) (1 + g_3) (g_2 g_4) (1 + g_1) \end{aligned}$	$(-g_1)^{1.26}$	Base C P.G.2 P.G.1 P.G.2 Follower P.G.3 P.G.4

Gear	Clu	itch	Sc	hed	lule	Drive Ratio Equation	Default Ratio	Power Flow
4	0	1	0	1	1	$rac{1+g_2+g_3}{1+g_2}$	1.69	Base C P.G.1 D Follower P.G.3 P.G.4
3	0	1	1	0	1	$\frac{\left(1+g_{3}\right)\!\left(1+g_{4}\right)}{1+g_{3}+g_{4}}$	2.08	Base C P.G.1 D Follower P.G.3 P.G.4
2	1	1	0	0	1	1+g <sub>1</sub>	2.94	Base C P.G.1 D Follower S P.G.4
1	1	1	1	0	0	$1+g_4$	4.54	Base C P.G.1 D Follower S R S P.G.4



# **Ports**

# Input

#### **Gear — Numerical input for the gear**

scalar

Specify -1 for reverse, 0 for neutral, and 1–8 for the forward gears.

Data Types: single | double

# **Conserving**

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### F — Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

# **Parameters**

### Initial gear — Gear state at the beginning of simulation

Neutral (default) | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

# See Also

10-Speed | 4-Speed CR-CR | 4-Speed Ravigneaux | 6-Speed Lepelletier | 7-Speed Lepelletier | 9-Speed

Introduced in R2015a

# 9-Speed

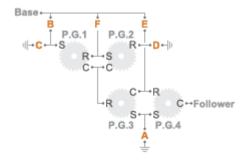
Clutch schedule for a nine-speed transmission **Library:** Transmissions



# **Description**

The 9-Speed block consists of four planetary gear sets and six clutches. The follower shaft connects to the planet gear carrier of the fourth planetary gear. Three of the clutches determine the power flow path for the base shaft. The other three clutches serve as brakes, grounding various gears of the planetary sets to the transmission housing.

This diagram shows a nine-speed transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram.



Label	Component
P.G.1-P.G.4	Planetary gears, 1-4
R	Ring gear
С	Planet gear carrier

Label	Component
S	Sun gear
B, E, F	Forward clutches that control the power flow path
A, C, D	Forward, braking clutches

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_x = \frac{N_{R_x}}{N_{S_x}},$$

#### where:

- $N_{\rm R}$  is the number of teeth in the planetary ring gear x, where x = 1, 2, 3, and 4.
- $N_{S_x}$  is the number of teeth in the planetary sun gear x, where x = 1, 2, 3, and 4

The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the plower-flow diagrams for each gear of the 9-Speed block. The schedule and gear ratios are based on the manufacturer data for the ZF 9HP nine-speed automatic transmission.

The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of 0 an unlocked state. The clutch schedule generates these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

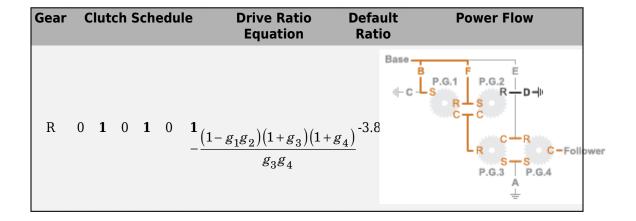
The plower-flow diagrams show the power flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear	Clutch Schedule	Drive Ratio Equation	Default Ratio	Power Flow
	A B C D E F			

Gear	Clut	ch S	Sch	edu	le Drive Rat Equation	
9	0 1	0	1	1	$0 \frac{1 + g_4}{1 + g_3 + g_4 - \left(\frac{1}{1 - \frac{1}{2}}\right)}$	Base    P.G.1   P.G.2   P.G.2     C   R   C   Follow   P.G.3   P.G.4     R   R   R   R   R   R     P.G.4   R   R   R   R     P.G.4   R   R   R   R     P.G.4   R   R   R   R   R     P.G.4   R   R   R   R   R     P.G.5   P.G.4   R   R   R     P.G.6   R   R   R   R   R     P.G.7   P.G.8   R   R   R     P.G.8   P.G.8   R   R   R     P.G.9   P.G.9   R   R   R     P.G.9   P.G.9   R   R   R     P.G.9   P.G.9   R   R     P.G.9   P.G.9   R   R     P.G.9   P.G.9   R
8	0 0	1	1	1	$0 \qquad \frac{1+g_4}{1+g_3+g_4}$	Base    P.G.1   P.G.2   P.G.2   P.G.2
7	<b>1</b> 0	0	1	1	$0  \frac{1+g_4}{1+g_3 - \left(\frac{g_3}{1+g_2}\right)}$	Base  B P.G.1 P.G.2 R C R C R C Follow P.G.3 A E

Gear	C	lute	ch S	Sch	edu	le	Drive Ratio Equation	Defa Rati	
6	1	0	1	0	1	0	$\frac{1+g_4}{1+g_3+g_4-\left(\frac{g_1g_3}{1+g_1}\right)}$	0.8	Base    P.G.1   P.G.2   D
5	1	1	0	0	1	0	1	1	Base  P.G.1  P.G.2  R  C  R  C  R  C  R  C  Follower  P.G.3  A  P.G.4
4	1	0	0	0	1	1	$\frac{1+g_4}{g_4}$	1.3	Base    P.G.1   P.G.2   D

Gear	С	lute	ch S	Sch	edu	le	Drive Ratio Equation	Defa Rat		Power Flow
3	1	1	0	0	0	1	$\frac{\left(1+g_3\right)\!\left(1+g_4\right)}{g_3g_4}$	1.9	Base P.C	3.1 F P.G.2 F D -   D -     C - Follow P.G.3 A -   E -   D -
2	1	0	1	0	0	1	$\frac{(1+g_1)(1+g_3)(1+g_4)}{g_1g_3g_4}$	2.8	Base B P.C	3.1 F P.G.2 E D III D II
1	1	0	0	1	0	1	$\frac{(1+g_2)(1+g_3)(1+g_4)}{g_3g_4}$	4.7	Base B P.C	P.G.2 P.G.4



### **Ports**

### Input

#### Gear — Numerical input for the gear

scalar

Specify -1 for reverse, 0 for neutral, and 1-9 for the forward gears.

Data Types: single | double

### **Conserving**

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### **F** — Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

### **Parameters**

#### Initial gear — Gear state at the beginning of simulation

Neutral (default) | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

### See Also

10-Speed | 4-Speed CR-CR | 4-Speed Ravigneaux | 6-Speed Lepelletier | 7-Speed Lepelletier | 8-Speed

Introduced in R2015a

# 10-Speed

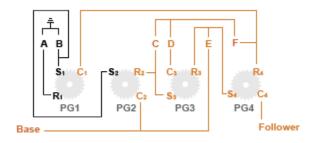
Clutch schedule for a 10-speed transmission **Library:** Transmissions



## **Description**

The 10-Speed transmission block consists of four planetary gear sets and six clutches. The follower shaft connects to the planet gear carrier of the fourth planetary gear. Four of the clutches determine the power flow path for the base shaft. The other two clutches serve as brakes, grounding various gears of the planetary sets to the transmission housing.

This diagram shows a 10-speed transmission. The labels for the gear components are superimposed on the input and output gears. The table lists the gear and clutch components that are labeled in the diagram. Power elements are shown in orange. Braking elements are shown in black.



Label	Component
PG1-PG4	Planetary gears, 1-4
$R_x$	Ring gear of planetary gear x

Label	Component
$C_x$	Planet gear carrier of planetary gear <i>x</i>
$S_{\chi}$	Sun gear of planetary gear x
C, D, E, F	Clutches that control the power flow path
A, B	Braking clutches

### **Drive Ratios, Clutch Schedule, and Power Flow**

The drive ratio between the transmission input and output shafts follows from the elementary gear ratios specified for the gear blocks. The elementary gear ratios are

$$g_x = \frac{N_{R_x}}{N_{S_x}},$$

#### where:

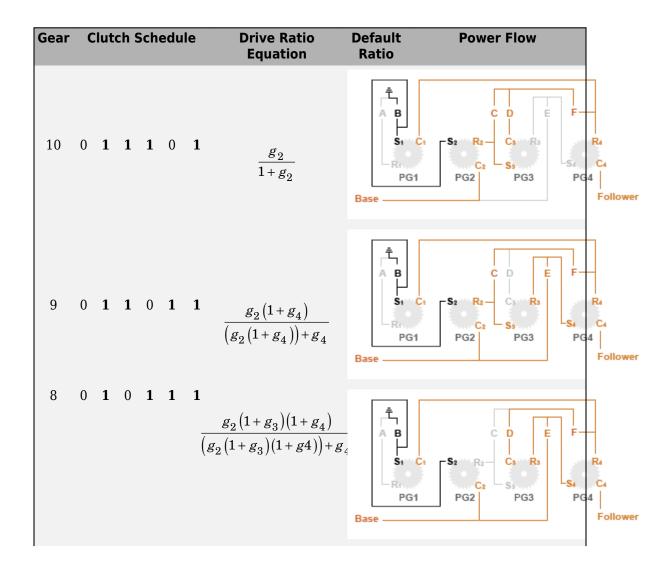
- $N_{R_x}$  is the number of teeth in the planetary ring gear x, where x = 1, 2, 3, and 4.
- $N_{S_x}$  is the number of teeth in the planetary sun gear x, where x = 1, 2, 3, and 4

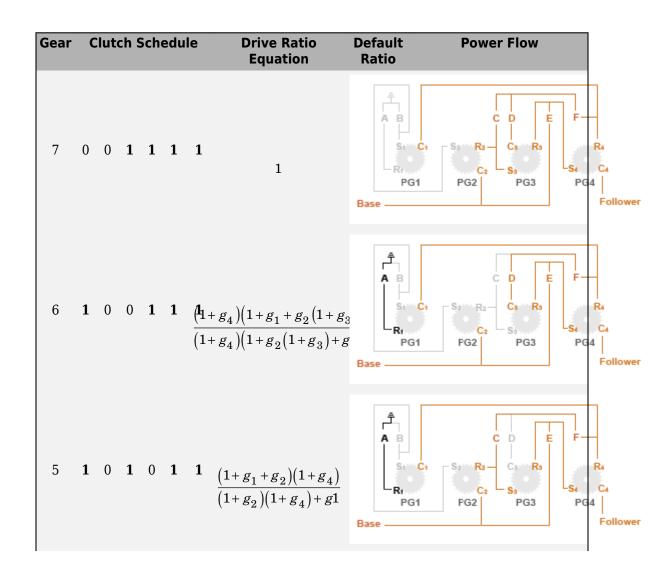
The table shows the clutch schedule, drive-ratio expressions, drive-ratio default values, and the power-flow diagrams for each gear of the 10-Speed block. The schedule and gear ratios are based on the manufacturer data for a 10R80 10-speed automatic transmission.

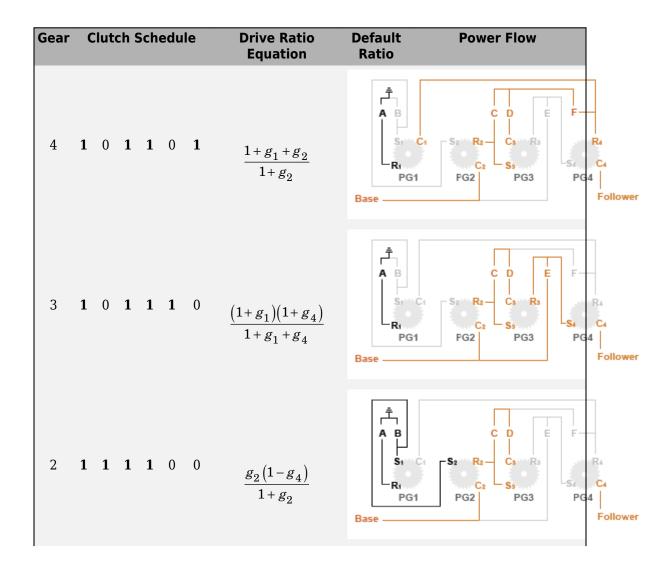
The letters in the clutch schedule columns denote the brakes and clutches. A value of 1 denotes a locked state and a value of 0 an unlocked state. The clutch schedule generates these signals based on the Gear port input signal. The signals are scaled through a Gain block and used as actuation inputs in the clutch blocks.

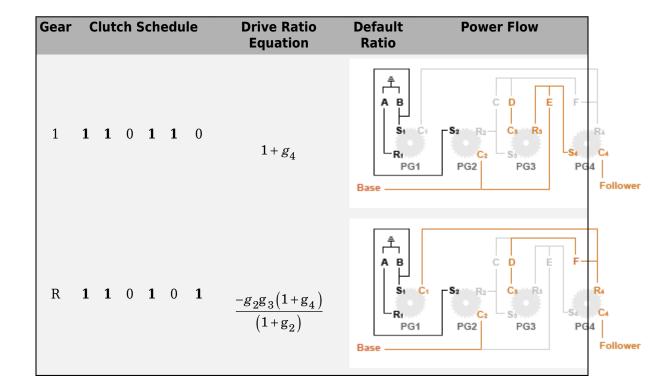
The power-flow diagrams show the power flow paths between input and output shafts for each gear setting. Power flow is shown in orange. Connections to the transmission housing (a mechanical ground) are shown in black.

Gear	Clutch Schedule	Drive Ratio Equation	Default Ratio	Power Flow
	A B C D E F			









### **Ports**

### Input

#### Gear — Numerical input for the gear

scalar

Specify -1 for reverse, 0 for neutral, and 1–10 for the forward gears.

Data Types: single | double

## **Conserving**

#### **B** — Base interface

mechanical rotational

Conserving port associated with the base shaft.

#### F — Follower interface

mechanical rotational

Conserving port associated with the follower shaft.

## **Parameters**

#### Initial gear — Gear state at the beginning of simulation

Neutral (default) | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | Reverse

Sets the initial engagement or disengagement of the clutches using the clutch schedule. When the transmission is in neutral, there is no power flow from the base shaft to the follower shaft.

### See Also

4-Speed CR-CR | 4-Speed Ravigneaux | 6-Speed Lepelletier | 7-Speed Lepelletier | 8-Speed | 9-Speed

#### Introduced in R2018a

## **Band Brake**

Frictional brake with flexible band wrapped around rotating drum

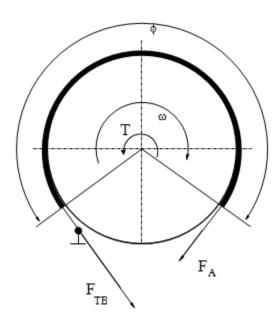


## Library

Brakes & Detents/Rotational

## **Description**

The block represents a frictional brake with a flexible band that wraps around the periphery of a rotating drum to produce a braking action. A positive actuating force causes the band to tighten around the rotating drum and it places the friction surfaces in contact. Viscous and contact friction between the drum and the flexible band surfaces cause the rotating drum to decelerate. Band brakes provide high braking torque at the cost of reduced braking precision in applications that include winch drums, chainsaws, go-karts, and mini-bikes. The model employs a simple parameterization with readily accessible brake geometry and friction parameters.



The following formula provides the braking torque as a function of the external brake actuation force that tightens the belt.

$$T = \left(F_{TB} - F_{A}\right) \cdot r_{D} + \mu_{visc} \cdot \omega,$$

In the formula, the parameters have the following meaning:

Parameter	Description
T	Braking torque
$F_{TB}$	Force acting on the tense branch of the band
$F_A$	External brake actuation force
$r_D$	Drum radius
$\mu_{visc}$	Viscous friction coefficient
μ	Contact friction coefficient
$\phi$	Wrap angle

Forces  $F_{TB}$  and  $F_A$  satisfy the relationship:

$$\frac{F_{TB}}{F_{\Delta}} = e^{\mu\phi},$$

Replacing the relationship in the braking torque formula eliminates force  $F_{TB}$ :

$$T = F_A \left( e^{\mu \phi} - 1 \right) \cdot r_D + \mu_{visc} \cdot \omega,$$

To avoid discontinuity at zero relative velocity, the model defines the actuation force  $F_S$  as a hyperbolic function:

$$F_A = F_{in} \cdot anh \left( rac{4\omega}{\omega_{threshold}} 
ight),$$

In the previous formula, the parameters represent the following quantities:

Parameter	Description
$F_{in}$	Force input signal
$\omega_{threshold}$	Angular velocity threshold

Connection F is a physical signal port that represents the external tensioning force applied on the belt. Connection S is a conserving rotational port that represents the rotating drum shaft.

#### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

### **Assumptions and Limitations**

The model does not account for actuator flow consumption.

## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

#### **Ports**

F

Physical signal port that represents the belt tensioning force.

S

Rotational conserving port that represents the rotating drum shaft.

Н

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

#### **Parameters**

### Geometry

#### **Drum radius**

Radius of the drum contact surface. The parameter must be greater than zero. The default value is  $150 \, \text{mm}$ .

#### Wrap angle

Contact angle between the flexible belt and the rotating drum. The parameter must be greater than zero. The default value is 270 deg.

#### **Friction**

#### Viscous friction coefficient

Value of the viscous friction coefficient at the belt-drum contact surface. The parameter must be greater than or equal to zero. The default value is  $.01 \, n*m/(rad/s)$ .

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The default value is [280.0, 300.0, 320.0] K.

This parameter is visible only when you select a block variant that includes a thermal port.

#### **Contact friction coefficient**

Value of the Coulomb friction coefficient at the belt-drum contact surface. The value is greater than zero. Unless you select a block variant that includes a thermal port, the default value is 0.3.

If you select a block variant that includes a thermal port, you specify this parameter as array. The array is the same size as the array for the **Temperature** parameter and the values increase left to right. The default value for the thermal variant is [0.1, 0.05, 0.03].

#### Angular velocity threshold

Angular velocity at which the friction coefficient at the belt-drum contact surface practically reaches its steady-state value. The parameter must be greater than zero. The default value is  $0.01 \, \text{rad/s}$ .

#### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. This parameter is enabled only if you select a block variant that includes a thermal port. The default value is  $50~\rm kJ/K$ .

### See Also

Double-Shoe Brake | Loaded-Contact Rotational Friction | Rotational Detent

**Topics**"Model Thermal Losses in Driveline Components"

## **Belt Drive**

Power transmission system with taut belt connecting two pulleys



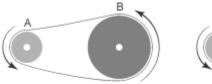
## Library

Couplings & Drives

## **Description**

The block represents a pair of pulleys connected with a flexible flat band or V-shaped belt. The model accounts for friction between the flexible belt and the pulley periphery. If the friction force is not sufficient to drive the load, the model allows slip. The relationship between the tensions in the tight and loose branches conforms to the Euler equation. The model accounts for centrifugal loading in the flexible belt, pulley inertia, and bearing friction.

The schematics show the belt drive in its two possible configurations: open (left) and crossed (right). In the open belt configuration, both pulleys tend to rotate in the same direction, and the larger pulley tends to have a larger belt wrap angle. In the crossed belt configuration, the pulleys tend to rotate in opposite directions, and both pulleys have the same wrap angle.



Open Belt Configuration



Crossed Belt Configuration

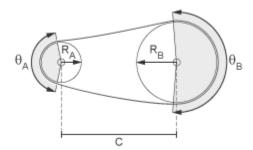
In the open configuration, the wrap angle of the belt around each pulley is given by the expressions:

$$\theta_{A} = \pi + 2 * \sin^{-1} \frac{R_{A} - R_{B}}{C},$$

$$\theta_{B} = \pi - 2 * \sin^{-1} \frac{R_{A} - R_{B}}{C}$$

- $\theta_A$  is the wrap angle of pulley A.
- $\theta_{\rm B}$  is the wrap angle of pulley B.
- $R_A$  is the effective radius of pulley A.
- $R_{\rm B}$  is the effective radius of pulley B.
- *C* is the distance between the centers of pulley A and pulley B.

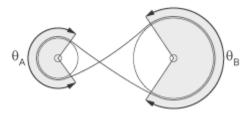
The following figure shows the wrap angles and the equation parameters used in the open-configuration calculations.



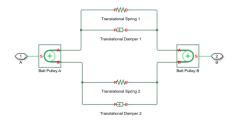
In the crossed configuration, the wrap angle of the belt around each pulley is given by the following expression. The two wrap angles are equal:

$$\theta_A = \theta_B = \pi + 2 * \sin^{-1} \frac{R_A + R_B}{C}$$

The figure shows the wrap angles calculated in the crossed-configuration expression.



The Belt Drive block is a structural component based on the Simscape Driveline Belt Pulley block and Simscape Translational Spring and Translational Damper blocks. The Translational Spring and Translational Damper blocks model the compliance of the belt. For the equations governing the contact dynamics between the belt and the pulley, see the Belt Pulley block reference page. The following figure shows the block diagram upon which the Belt Drive block is based.



## **Assumptions and Limitations**

- The pulleys do not translate.
- The friction coefficient and friction velocity threshold between the belt and each of the pulleys is the same.

#### **Ports**

### Conserving

#### A — Rotational velocity

mechanical rotational

Rotational conserving port associated with the shaft of pulley A.

#### **B** — Rotational velocity

mechanical rotational

Rotational conserving port associated with the shaft of pulley B.

### **Parameters**

### **Drive type**

Select the type of belt drive that you want to model.

- Open belt (Default)
- · Crossed belt

The schematic in this page shows the two drive types.

### **Belt type**

Type of flexible element modeled.

- Flat band (Default)
- V-belt— Exposes the **V-belt sheave angle** and **Number of V-belts** parameters.

### V-belt sheave angle

Sheave angle of the V-belt. Default is 30 deg.

The **V-belt sheave angle** parameter is visible only when the **Belt type** parameter is **V-belt**.

#### **Number of V-belts**

Number of parallel V-belts. Default is 1.

Non-integer values are rounded to the nearest integer. Increasing the number of belts increases the friction force, effective mass per unit length, and maximum allowable tension.

The **Number of V-belts** parameter is visible only when the **Belt type** parameter is V-belt.

### **Centrifugal force**

Select whether to include the effects of centrifugal force. If included, centrifugal force saturates to approximately 90% of the value of the force on each belt end. Options are:

- Do not model centrifugal force suitable for HIL simulation —
   Default option which does not include centrifugal force contributions.
- Model centrifugal force— Exposes the **Belt mass per unit length** parameter for configuring the centrifugal force contribution.

#### Belt mass per unit length

Linear density of each belt. Default is 0.6 kg/m.

The model uses this value to calculate the centrifugal loading. This parameter is enabled only if you select Model centrifugal force for the **Centrifugal force** parameter.

## Longitudinal stiffness

The effective stiffness of the belt. Default is 1e+4 N/m.

## Longitudinal damping

Effective damping of the belt. Default is 1000 N/(m/s).

#### **Pre-tension**

Tension in the belt when the belt and pulleys are at rest. The value must be positive. The default value is 100 N.

#### **Maximum tension**

Specifies whether the block throws an assertion when the belt tension is too large.

- No maximum tension (Default)
- Specify maximum tension— Throws an assertion when the belt tension is too high.
   Exposes the **Belt maximum tension** parameter.

#### **Belt maximum tension**

Maximum allowable tension for each belt. Default is 1e+5 N.

When the tension on either end of the belt meets or exceeds this value, the simulation ends with an error.

The **Belt maximum tension** parameter is visible only when the **Maximum tension** parameter is Specify maximum tension.

To specify the characteristics of pulley attached to port A, select the **Pulley A** tab. To specify the characteristics of pulley attached to port B, select the **Pulley B** tab.

### **Pulley radius**

Radius of the pulley. Default is  $0.15\,$  m for pulley A and  $0.3\,$  m for pulley B.

#### **Bearing viscous friction coefficient**

Viscous friction associated with the bearings that hold the axis of the pulley. Default is 0 N\*m/(rad/s) for pulley A and 0.001 N\*m/(rad/s) for pulley B.

### Inertia

Specifies whether the block models rotational inertia of the pulley.

- No inertia (Default)
- Specify inertia and initial velocity— Models rotational inertia. Exposes the **Pulley inertia** and **Pulley initial velocity** parameters.

### **Pulley inertia**

Rotational inertia of the pulley. Default is  $0.01 \text{ kg*m^2}$  for pulley A, and  $0.03 \text{ kg*m^2}$  for pulley B.

The **Pulley inertia** parameter is visible only when the **Inertia** parameter is Specify inertia and initial velocity.

### **Pulley initial velocity**

Initial rotational velocity of the pulley. Default is 0 rad/s.

The **Pulley initial velocity** parameter is visible only when the **Inertia** parameter is Specify inertia and initial velocity.

To specify contact characteristics, select the **Contact** tab.

#### Contact friction coefficient

Coulomb friction coefficient between the belt and the pulley surface. Default is 0.5.

#### Wrap calculations

Specifies whether the block calculates the wrap angle of the belt on the pulleys using the pulley radii, center separation, and drive type or if the wrap angles are specified directly.

 Specify pulley center separation — (Default) The block calculates the wrap angle of the belt on the pulleys using the pulley radii, center separation, and drive type.

Exposes the **Pulley center separation** parameter.

• Specify wrap angles — Uses the wrap angles that you specify.

Exposes the Pulley A wrap angle and Pulley B wrap angle parameters.

### **Pulley center separation**

Distance between the centers of the pulleys. Default is  $0.5\,$  m.

The **Pulley center separation** parameter is visible only when the **Wrap calculations** parameter is Specify pulley center separation.

### **Pulley A wrap angle**

Angle of contact between the belt and pulley attached to port A. Default is 145 deg.

The **Pulley A wrap angle** parameter is visible only when the **Wrap calculations** parameter is Specify wrap angles.

### **Pulley B Wrap angle**

Angle of contact between the belt and pulley attached to port B. Default is 215 deg.

The **Pulley B wrap angle** parameter is visible only when the **Wrap calculations** parameter is Specify wrap angles.

## Friction velocity threshold

Relative velocity required for peak kinetic friction in the contact. The friction velocity threshold improves the numerical stability of the simulation by ensuring that the force is continuous when the direction of the velocity changes. Default is 0.001 m/s.

### **See Also**

Belt Pulley | Chain Drive

### **Topics**

"Best Practices for Modeling Pulley Networks"

"Rotational-Translational Couplings"

## **Belt Pulley**

Power transmission element with frictional belt wrapped around pulley circumference

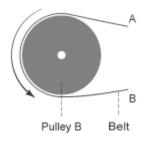


## Library

Simscape Driveline / Couplings & Drives

## **Description**

This block represents a pulley wrapped in a flexible flat band or V-shaped belt. The model accounts for friction between the flexible belt and the pulley periphery. If the friction force is not sufficient to drive the load, the model allows slip. The relationship between the tensions in the tight and loose branches conforms to the Euler equation. The model accounts for centrifugal loading in the flexible belt, pulley inertia, and bearing friction.



The block dialog box enables you to select the relative belt direction of motion. Depending on the chosen setting, the two belt ends can move in equal or opposite directions. The block model assumes noncompliance in the belt and no resistance to motion due to wrapping around the pulley.

The block equations model power transmission between the belt branches or to/from the pulley. The tight and loose branches use the same calculation. Without sufficient tension, the frictional force is not enough to transmit power between the pulley and belt.

The model is valid when both ends of the belt are in tension. An optional warning can display at the MATLAB® command line when either belt end loses tension. When assembling a model, ensure that tension is maintained throughout the simulation. Consider this requirement when you interpret the simulation results.

### **Equations**

If the relative velocity between the belt and pulley is positive or zero, that is  $V_{rel} \ge 0$ , the Belt Pulley block calculates friction force as

$$F_{fr} = F_B - F_C = (F_A - F_C) * \exp(f * \theta).$$

If the relative velocity is negative, that is  $V_{rel} < 0$ , the friction force is calculated as

$$F_{fr} = F_A - F_C = (F_B - F_C) * \exp(f * \theta).$$

In both cases:

$$V_{rel} = V_A - \omega_S * R$$

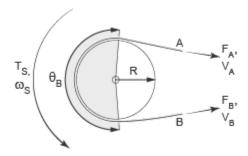
$$F_C = \rho * V_B^2$$

$$V_A = -V_B$$

Where:

- $V_{rel}$  is the relative velocity between the belt and pulley periphery.
- $V_A$  is the Branch A linear velocity.
- $V_B$  is the Branch B linear velocity.
- $\omega_{\scriptscriptstyle S}$  is the pulley angular velocity.
- *R* is the pulley radius.

- $F_C$  is the belt centrifugal force.
- $\rho$  is the belt linear density.
- $F_{fr}$  is the friction force between the pulley and the belt.
- $F_A$  is the force acting along branch A.
- $F_B$  is the force acting along branch B.
- *f* is the friction coefficient.
- $\theta$  is the contact wrap angle.



For a flat band, specify the value of f directly in the block parameters dialog box. For a V-belt, the model calculates the value as

$$f = \frac{f}{\sin(\frac{\phi}{2})},$$

where:

- f is the effective friction coefficient for a V-belt.
- $\Phi$  is the V-belt sheave angle.

The idealization of the discontinuity at  $V_{rel} = 0$  is both difficult for the solver to resolve and not physically accurate. To alleviate this issue, the friction coefficient is assumed to change its value as a function of the relative velocity such that

$$\mu = -f * \tanh \left( 4 * \frac{V_{rel}}{V_{thr}} \right),$$

where

- $\mu$  is the instantaneous value of the friction coefficient.
- *f* is the steady-state value of the friction coefficient.
- $V_{thr}$  is the friction velocity threshold.

The friction velocity threshold controls the width of the region within which the friction coefficient changes its value from zero to a steady-state maximum. The friction velocity threshold specifies the velocity at which the hyperbolic tangent equals 0.999. The smaller the value, the steeper is the change of  $\mu$ .

This parameter calculate the friction force as

$$F_{fr} = F_A - F_C = (F_B - F_C) * \exp(\mu * \theta).$$

The resulting torque on the pulley is given as

$$T_S = (F_A + F_B) * R * anh \left( 4 rac{V_{
m rel}}{V_{
m thr}} 
ight) * anh \left( rac{F_B}{F_{
m thr}} 
ight) - \omega_S * b.$$

where:

- $T_S$  is the pulley torque.
- *b* is the bearing viscous damping.
- $F_{thr}$  is the force threshold.

### **Assumptions and Limitations**

- The model does not account for compliance along the length of the belt.
- · Both belt ends maintain adequate tension throughout the simulation.

#### **Ports**

The sign convention is such that, when **Belt direction** is set to Ends move in opposite direction, a positive rotation in port **S** tends to give a negative translation for port **A** and a positive translation for port **B**.

### Conserving

#### S - Rotational velocity

mechanical rotational

Rotational conserving port associated with the pulley shaft.

#### A — Velocity

mechanical translational

Translational conserving port associated with the belt end *A*.

#### **B** — Velocity

mechanical translational

Translational conserving port associated with the belt end *B*.

### **Parameters**

#### **Belt**

#### Belt type

Type of flexible element modeled.

- Flat band (Default)
- V-belt— Exposes the **V-belt sheave angle** and **Number of V-belts** parameters.

#### V-belt sheave angle

Sheave angle of the V-belt. Default is 30 deg.

The **V-belt sheave angle** parameter is visible only when the **Belt type** parameter is **V-belt**.

#### **Number of V-belts**

Number of parallel V-belts. The default value is 1.

Non-integer values are rounded to the nearest integer. Increasing the number of belts increases the friction force, effective mass per unit length, and maximum allowable tension.

The **Number of V-belts** parameter is visible only when the **Belt type** parameter is V-belt.

#### Centrifugal force

Select whether to include the effects of centrifugal force. If included, centrifugal force saturates to approximately 90% of the value of the force on each belt end. Options are:

- Do not model centrifugal force suitable for HIL simulation Default option which does not include centrifugal force contributions.
- Model centrifugal force— Exposes the **Belt mass per unit length** parameter for configuring the centrifugal force contribution.

#### Belt mass per unit length

Linear density of each belt. Default is 0.6 kg/m.

The model uses this parameter to calculate the centrifugal loading. This parameter is enabled only if you select Model centrifugal force for the **Centrifugal force** parameter.

#### Belt direction.

Relative direction of translational motion of one belt end with respect to the other. Options include:

- Ends move in opposite direction
- Ends move in same direction

#### Maximum tension

Specifies whether the block throws an assertion when the belt tension is too large.

- No maximum tension (Default)
- Specify maximum tension Throws an assertion when the belt tension is too high. Exposes the **Belt maximum tension** parameter.

#### **Belt maximum tension**

Maximum allowable tension for each belt. Default is 1e+5 N.

When the tension on either end of the belt meets or exceeds this value, the simulation ends with an error.

The **Belt maximum tension** parameter is visible only when the **Maximum tension** parameter is Specify maximum tension.

#### **Tension warning**

Specifies whether the block writes a warning at the MATLAB command line when the tension at either end of the belt falls below zero.

- Do not check belt tension (Default)
- Warn if either belt end loses tension

Select the **Pulley** tab to specify the pulley characteristics.

### **Pulley**

#### **Pulley radius**

Radius of the pulley. Default is 0.15 m.

#### **Bearing viscous friction coefficient**

Viscous friction associated with the bearings that hold the axis of the pulley. Default is 0.001 N\*m/(rad/s).

#### Inertia

Specifies whether the block models rotational inertia of the pulley.

- No inertia (Default)
- Specify inertia and initial velocity Models rotational inertia. Exposes the **Pulley inertia** and **Pulley initial velocity** parameters.

#### **Pulley inertia**

Rotational inertia of the pulley. Default is 0.01 kg\*m^2.

The **Pulley inertia** parameter is visible only when the **Inertia** parameter is Specify inertia and initial velocity.

#### **Pulley initial velocity**

Initial rotational velocity of the pulley. Default is  $\theta$  rad/s.

The **Pulley initial velocity** parameter is visible only when the **Inertia** parameter is Specify inertia and initial velocity.

to specify contact characteristics, use the Contact pane.

#### **Contact**

#### **Contact friction coefficient**

Coulomb friction coefficient between the belt and the pulley surface. Default is 0.5.

#### Wrap angle

Angle of contact between the belt and pulley. Default is 180 deg.

#### Friction velocity threshold

Relative velocity required for peak kinetic friction in the contact. The friction velocity threshold improves the numerical stability of the simulation by ensuring that the force is continuous when the direction of the velocity changes. Default is 0.001 m/s.

## **Example**

The sdl\_power\_window Simscape Driveline example model shows the use of the Belt Pulley block.

### See Also

Belt Drive | Rope Drum | Wheel and Axle

### **Topics**

"Best Practices for Modeling Pulley Networks"

"Rotational-Translational Couplings"

## **Chain Drive**

Power transmission system with chain and two sprockets

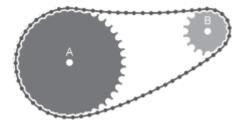


## Library

Couplings & Drives

## **Description**

This block represents a power transmission system with a chain and two sprockets. The chain meshes with the sprockets, transmitting rotary motion between the two. Power transmission can occur in reverse, that is, from driven to driver sprocket, due to external loads. This condition is known as back-driving.



The drive chain is compliant. It can stretch under tension and slacken otherwise. The compliance model consists of a linear spring-damper set in a parallel arrangement. The spring resists tensile strain in the chain. The damper resists tensile motion between chain elements.

The spring and damper forces act directly on the sprockets that the chain connects. The spring force is present when one chain branch is taut. The damper force is present

continuously. If you specify a maximum tension value, when the net tensile force in the chain exceeds this value, simulation stops with an error.

The block accounts for viscous friction at the sprocket joint bearings. During motion, viscous friction causes power transmission losses, reducing chain-drive efficiency. These losses compound due to chain damping. Setting viscous friction and chain damping to zero eliminates power transmission losses in the chain drive.

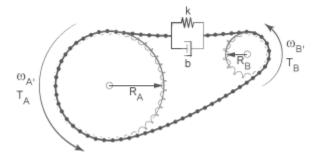
The tensile strain rate in the chain is the difference between the sprocket tangential velocities, each the product of the angular velocity and pitch radii. Mathematically,

$$\dot{x} = \omega_A R_A - \omega_B R_B,$$

#### where:

- *x* is the tensile strain.
- $\omega_{A}$ ,  $\omega_{B}$  are the sprocket angular velocities.
- $R_A$ ,  $R_B$  are the sprocket pitch radii.

The figure shows the relevant equation variables.



The chain tensile force is the net sum of spring and damper forces. The spring force is the product of the tensile strain and the spring stiffness constant. This force is zero whenever the tensile strain is smaller than the chain slack. The damper force is the product of the tensile strain rate and the damping coefficient. Mathematically,

$$F = \begin{cases} -\left(x - \frac{S}{2}\right)k - \dot{x}b, & x > \frac{S}{2} \\ -\dot{x}b, & \frac{S}{2} \ge x \ge -\frac{S}{2}, \\ -\left(x + \frac{S}{2}\right)k - \dot{x}b, & x < -\frac{S}{2} \end{cases}$$

where:

- S is the chain slack.
- *k* is the spring stiffness constant.
- *b* is the damper coefficient.

The chain exerts a torque on each sprocket equal to the product of the tensile force and the sprocket pitch radius. The two torques act in opposite directions according to the equations

$$T_A = -F \cdot R_A$$

and

$$T_B = F \cdot R_B$$
,

where:

- $T_A$  is the torque that the chain applies on sprocket A.
- $T_{\rm B}$  is the torque that the chain applies on sprocket B.

### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations

corresponding to the selected block configuration, the values specified for this variable are ignored.

# **Assumptions and Limitations**

- The sprocket tooth ratio equals the sprocket pitch radius ratio.
- Chain inertia is negligible.

## **Parameters**

## **Geometry**

Specify the sprocket and chain dimensions.

### **Sprocket A pitch radius**

Radius of the sprocket A pitch circle. The pitch circle is an imaginary circle passing through the contact point between a chain roller and a sprocket cog at full engagement. The default value is 80 mm.

## Sprocket B pitch radius

Radius of the sprocket B pitch circle. The pitch circle is an imaginary circle passing through the contact point between a chain roller and a sprocket  $\cos$  at full engagement. The default value is 40 mm.

## Chain slack length

Maximum distance the loose branch of the drive chain can move before it is taut. This distance equals the length difference between actual and fully taut drive chains.

If one sprocket is held in place while the top chain branch is taut, then the slack length is the tangential distance that the second sprocket must rotate before the lower chain branch becomes taut. The default value is 50 mm.

## **Dynamics**

Specify the internal forces acting in the chain and on the sprockets.

#### Chain stiffness

Linear spring constant in the chain compliance model. This constant describes the chain resistance to strain. The spring element accounts for elastic energy storage in the chain due to deformation. The default value is 1e+5 N/m.

### Chain damping

Linear damping coefficient in the chain compliance model. This coefficient describes the chain resistance to tensile motion between adjacent chain elements. The damper element accounts for power losses in the chain due to deformation. The default value is 5 N/(m/s).

### Viscous friction coefficient of sprocket A

Friction coefficient due to the rolling action of the sprocket A joint bearing in the presence of a viscous lubricant. The default value is 0.001 N\*m/(rad/s).

### Viscous friction coefficient of sprocket B

Friction coefficient due to the rolling action of the sprocket B joint bearing in the presence of a viscous lubricant. The default value is 0.001 N\*m/(rad/s).

### Maximum tension

Specify the upper tension limit in the drive chain.

#### Maximum tension

Select whether to constrain the maximum tensile force in the drive chain.

- No maximum tension Chain tension can be arbitrarily large during simulation.
- Maximum tension Chain tension must remain lower than a maximum value.
   Simulation stops with an error when tension exceeds this value.

#### Chain maximum tension

Maximum allowed value of the tensile force acting in the chain. The default value is 1e+6 N.

# **Ports**

Port	Description
A	Conserving rotational port associated with sprocket A
В	Conserving rotational port associated with sprocket B

# **Example**

To see how you can use the Chain Drive block in a model, open sdl\_sheet\_metal\_feeder.

# **See Also**

Simple Gear | Variable Ratio Transmission

# **Topics**

"Gear Coupling Control Using Clutches"

# **Compound Planetary Gear**

Planetary gear train with stepped planet gear set

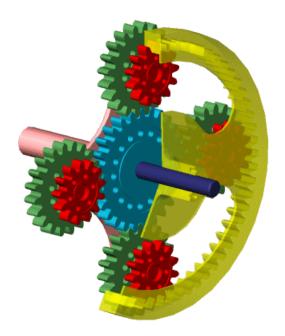


# Library

Simscape / Driveline / Gears

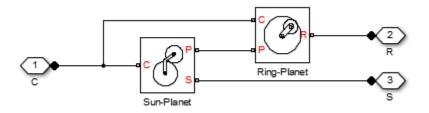
# **Description**

This block represents a planetary gear train with composite planet gears. Each composite planet gear is a pair of rigidly connected and longitudinally arranged gears of different radii. One of the two gears engages the centrally located sun gear while the other engages the outer ring gear.



## **Compound Planetary Gear**

The block models the compound planetary gear as a structural component based on Sun-Planet and Ring-Planet Simscape Driveline blocks. The figure shows the block diagram of this structural component.



To increase the fidelity of the gear model, you can specify properties such as gear inertia, meshing losses, and viscous losses. By default, gear inertia and viscous losses are assumed negligible. The block enables you to specify the inertias of the internal planet

gears only. To model the inertias of the carrier, sun, and ring gears, connect Simscape Inertia blocks to ports C, S, and R.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Compound Planetary Gear Model**

### **Ideal Gear Constraints and Gear Ratios**

Compound Planetary Gear imposes two kinematic and two geometric constraints on the three connected axes and the fourth, internal wheel (planet):

$$r_{\rm C}\omega_{\rm C}=r_{\rm S}\omega_{\rm S}+r_{\rm P1}\omega_{\rm P}$$
 ,  $r_{\rm C}=r_{\rm S}+r_{\rm P1}$  ,  $r_{\rm R}\omega_{\rm R}=r_{\rm C}\omega_{\rm C}+r_{\rm P2}\omega_{\rm P}$  ,  $r_{\rm R}=r_{\rm C}+r_{\rm P2}$  .

The ring-planet gear ratio  $g_{\rm RP} = r_{\rm R}/r_{\rm P2} = N_{\rm R}/N_{\rm P2}$  and the planet-sun gear ratio  $g_{\rm PS} = r_{\rm P1}/r_{\rm S} = N_{\rm P1}/N_{\rm S}$ . N is the number of teeth on each gear. In terms of these ratios, the key kinematic constraint is:

$$(1 + g_{RP} \cdot g_{PS})\omega_C = \omega_S + g_{RP} \cdot g_{PS}\omega_R$$
.

The four degrees of freedom reduce to two independent degrees of freedom. The gear pairs are (1,2) = (P2,R) and (S,P1).

**Warning** The gear ratio  $g_{RP}$  must be strictly greater than one.

The torque transfers are:

$$g_{\rm RP} \tau_{\rm P2} + \tau_{\rm R} - \tau_{\rm loss}({\rm P2,R}) = 0$$
 ,  $g_{\rm PS} \tau_{\rm S} + \tau_{\rm P1} - \tau_{\rm loss}({\rm S,P1}) = 0$  ,

with  $\tau_{loss} = 0$  in the ideal case.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . See "Model Gears with Losses".

## Limitations

- · Gears are assumed rigid.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port representing the planet gear carrier
R	Rotational conserving port representing the ring gear
S	Rotational conserving port representing the sun gear
Н	Thermal conserving port for thermal modeling

# **Parameters**

## Main

## Ring (R) to planet (P) teeth ratio (NR/NP)

Fixed ratio  $g_{RP}$  of the ring gear to the planet gear. The gear ratio must be strictly greater than 1. The default is 2.

## Planet (P) to sun (S) teeth ratio (NP/NS)

Fixed ratio  $g_{PS}$  of the planet gear to the sun gear. The gear ratio must be strictly positive. The default is 1.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

### **Constant Efficiency**

### Sun-planet and ring-planet ordinary efficiencies

Vector of torque transfer efficiencies [ $\eta_{SP}$   $\eta_{RP}$ ] for sun-planet and ring-carrier gear wheel pair meshings, respectively.

### Sun-carrier and planet-carrier power thresholds

Vector of power thresholds  $p_{\rm th}$  above which full efficiency factors apply, for sun-carrier and planet-carrier, respectively. Below these values, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default array is [0.001 0.001] W.

#### With Thermal Port

## Temperature

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as each efficiency array. The default array is [280 300 320] K.

## **Sun-planet efficiency**

Array of mechanical efficiencies with power flowing from the sun gear to the planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

## Ring-planet efficiency

Array of mechanical efficiencies with power flowing from the ring gear to the planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

#### Sun-carrier and planet-carrier power thresholds

Array of power thresholds above which the full efficiency factors apply. Enter the thresholds for the sun and planet gears relative to the gear carrier, in this order. A hyperbolic tangent function smooths the efficiency factors between zero at rest and the values provided by the temperature-efficiency lookup tables at the power thresholds. The default array is [0.001 0.001] W.

### Viscous Losses

#### Sun-carrier and planet-carrier viscous friction coefficients

Vector of viscous friction coefficients  $[\mu_S \mu_P]$  for the sun-carrier and planet-carrier gear motions, respectively. The default is  $[0 \ 0]$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

### Inertia

### Planet gear inertia

Moment of inertia of the combined planet gears. This value must be positive or zero. Enter 0 to ignore gear inertia. The default value is 0 kg\*m^2.

## **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

## Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

# See Also

#### **Simscape Blocks**

Planetary Gear | Ravigneaux Gear | Ring-Planet | Sun-Planet

## **Topics**

"Basic Motion, Torque, and Force Modeling"

"Model Thermal Losses in Driveline Components"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Cone Clutch**

Friction clutch with conical plates that engage when normal force exceeds threshold



# Library

Clutches

# **Description**

This block represents a friction clutch with a conical contact interface. The conical interface creates a wedging action between the clutch components, a cone and a cup, thereby reducing the normal force required for clutch engagement.

The cup component connects rigidly to the drive shaft, spinning with it as a unit. The cone component connects rigidly to the driven shaft, which sits in axial alignment with the drive shaft. The clutch engages when the cone slides toward the cup and presses tightly against its internal surface.

Friction at the cone-cup contact interface enables the clutch to transmit rotational power between the drive and driven shafts. The friction model of this block includes both static and kinetic friction contributions, the latter of which leads to power dissipation during slip between the cone and cup components.

Cone clutches find real-world application in synchromesh gearboxes, which synchronize the drive and driven shaft speeds to enable smoother engagement between transmission gears. For block model details, see "Cone Clutch Model" on page 1-78.

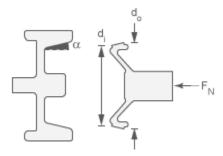
## **Cone Clutch Model**

The Cone Clutch is based on the Fundamental Friction Clutch. For the complete friction clutch model, consult the Fundamental Friction Clutch block reference page. This section discusses the specialized model implemented in the Cone Clutch.

When you apply a normal force  $F_{\rm N}$ , the Cone Clutch block can apply two kinds of friction to the driveline motion, kinetic and static. The clutch applies kinetic friction torque only when one driveline axis is spinning relative to the other driveline axis. The clutch applies static friction torque when the two driveline axes lock and spin together. The block iterates through multistep testing to determine when to lock and unlock the clutch.

## **Clutch Geometry and Variable Summary**

The figure shows the cone clutch geometry and some model parameters. Refer to the table for a summary of variable descriptions.



#### **Clutch Variables**

Parameter	Definition	Significance
$d_{\rm o}$	Outer diameter of the conical contact surface	See the preceding figure
$d_{ m i}$	Inner diameter of the conical contact surface	See the preceding figure
α	Cone half angle	See the preceding figure
ω	Relative angular velocity (slip)	$\omega_{\rm F}$ - $\omega_{\rm B}$
$\omega_{ m Tol}$	Slip tolerance for clutch locking	See the following model
$F_{ m N}$	Normal force applied to conical surfaces	Normal force applied, if greater than threshold: $F_{\rm N} > F_{\rm th}$
α	Cone half-angle	See the preceding figure
$r_{ m eff}$	Effective torque radius	Effective moment arm of clutch friction force
$k_{\mathrm{K}}$	Kinetic friction coefficient	Dimensionless coefficient of kinetic friction of conical friction surfaces. Function of $\omega$ .
k <sub>S</sub>	Static friction coefficient	Dimensionless coefficient of static friction of conical friction surfaces.
$\tau_{\mathrm{K}}$	Kinetic friction torque	See the following model
$ au_{ m S}$	Static friction torque limit	(static friction peak factor)·(kinetic friction torque for $\omega \to 0$ ) (See the following model)

## **Relation to Fundamental Friction Clutch**

The Cone Clutch is based on the Fundamental Friction Clutch. Instead of requiring the kinetic and static friction limit torques as input signals, the Cone Clutch calculates the kinetic and static friction from the clutch parameters and the input normal force signal  $F_{\rm N}$ . See the Fundamental Friction Clutch reference page for more information about the friction clutch.

The kinetic friction torque is the product of four factors:

$$\tau_{\rm K} = k_{\rm K} \cdot F_{\rm N} \cdot r_{\rm eff} \cdot {\rm sgn}(\omega)$$
.

The kinetic friction torque opposes the relative slip and is applied with an overall minus sign. It changes sign when  $\omega$  changes sign.

You specify the kinetic friction coefficient  $k_{\rm K}$  as either a constant or a tabulated discrete function of relative angular velocity  $\omega$ . The tabulated function is assumed to be symmetric for positive and negative values of the relative angular velocity. Therefore, specify  $k_{\rm K}$  for positive values of  $\omega$  only.

The *effective torque radius*  $r_{\text{eff}}$  is the effective radius, measured from the driveline axis, at which the kinetic friction forces are applied at the frictional surfaces. It is related to the geometry of the conical friction surface geometry by:

$$r_{\text{eff}} = \frac{1}{3\sin\alpha} \frac{d_o^3 - d_i^3}{d_o^2 - d_i^2}$$

 $d_0$  and  $d_i$  are the contact surface maximum and minimum diameters, respectively.

The static friction limit is related to the kinetic friction, setting  $\omega$  to zero and replacing the kinetic with the static friction coefficient:

$$\tau_{\rm S} = k_{\rm S} \cdot F_{\rm N} \cdot r_{\rm eff} \ge 0$$
.

 $k_{\rm S} > k_{\rm K}$ , so that the torque  $\tau$  needed across the clutch to unlock it by overcoming static friction is larger than the kinetic friction at the instant of unlocking, when  $\omega = 0$ .

The static friction limit defines symmetric *static friction torque limits* as:

$$\tau_{\rm S} \equiv \tau_{\rm S}^+ = -\tau_{\rm S}^- \,.$$

The range  $[\tau_S^-, \tau_S^+]$  is used by the Fundamental Friction Clutch.

The clutch engages (transmits torque) when the conical friction surfaces are subject to a positive normal force and generate kinetic friction:  $F_N > 0$  and  $\tau_K > 0$ .

The clutch locks if and only if it is engaged, and the slip is less than the velocity tolerance:  $|\omega| < \omega_{\text{Tol}}$ .

The power dissipated by the clutch is  $|\omega \cdot \tau_K|$ . The clutch dissipates power only if it is both slipping ( $\omega \neq 0$ ) and applying kinetic friction ( $\tau_K > 0$ ).

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Ports**

В

Rotational conserving ports associated with the driving (base) shaft. The clutch motion is measured as the  $slip\ \omega = \omega_{F^-}\ \omega_B$ , the angular velocity of follower relative to base.

F

Rotational conserving ports associated with the driven (follower) shaft

Ν

Physical signal terminal through which you import the normal force. This signal is positive or zero. A signal N less than zero is interpreted as zero.

Н

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

## **Parameters**

# Geometry

#### Contact surface maximum diameter

Outer conical diameter  $d_0$ . The default value is 150 mm.

#### Contact surface minimum diameter

Inner conical diameter  $d_i$ . The default value is 100 mm.

#### Cone half angle

Half opening angle  $\alpha$  of the cone geometry. The default value is 12 deg.

## **Friction**

#### Friction model

Select a parameterization method to model the kinetic friction coefficient. The options and default values for this parameter depend on the variant that you select for the block. The options are:

- Fixed kinetic friction coefficient Provide a fixed value for the kinetic friction coefficient. This option:
  - Is only visible if you use the default variant of the block
  - Is the default method for parameterizing the default variant of the block
  - Affects the visibility of other parameters

#### Fixed kinetic friction coefficient

#### Kinetic friction coefficient

The kinetic, or Coulomb, friction coefficient. The coefficient must be greater than zero. The default value is 0.3.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Table lookup kinetic friction coefficient Define the kinetic friction coefficient by one-dimensional table lookup based on the relative angular velocity between disks. This option:
  - Is only visible if you use the default variant of the block
  - · Affects the visibility of other parameters

## Table lookup kinetic friction coefficient Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values

depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient vector

Specify the output values for the kinetic friction coefficient as a vector. All values must be positive. The default value is [0.3, 0.22, 0.19].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Temperature-dependent kinetic friction coefficient Define the kinetic friction coefficient by table lookup based on the temperature. This option:
  - Is only visible if you use a thermal variant of the block

- Is the default method for parameterizing the thermal variant of the block
- Affects the visibility of other parameters

## Temperature-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

#### Kinetic friction coefficient vector

Specify the output values for kinetic friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. All values must be greater than zero. The default value is [0.3, 0.28, 0.25].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

## Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

 Linear — Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region. • Nearest — Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

- Temperature and speed-dependent kinetic friction coefficient —
  Define the kinetic friction coefficient by table lookup based on the temperature
  and the relative angular velocity between disks. This option:
  - Is only visible if you use the default variant of the block
  - Affects the visibility of other parameters

# Temperature and speed-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient matrix

Specify the output values for kinetic friction coefficient as a matrix. All the values must be greater than zero. The size of the matrix must equal the size of the matrix that is the result of the temperature vector  $\times$  the kinetic friction coefficient relative velocity vector. The default value is [0.34, 0.32, 0.3; 0.3, 0.28, 0.25; 0.25, 0.2, 0.15].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

## Velocity tolerance

Relative velocity below which the two surfaces can lock. The surfaces lock if the torque across the B and F rotational ports is less than the product of the effective radius, the static friction coefficient, and the applied normal force. The default value is 0.001 rad/s.

#### Threshold force

The normal force applied to the physical signal port N is applied to the contact only if the amount of force exceeds the value of the **Threshold force** parameter. Forces below the **Threshold force** are not applied, and there is consequently no transmitted frictional torque. The default value is  $1\ N$ .

## **Initial Conditions**

#### **Initial state**

Clutch state at the start of simulation. The clutch can be in one of two states, locked and unlocked. A locked clutch constrains the base and follower shafts to spin at the

same velocity, that is, as a single unit. An unlocked clutch allows the two shafts to spin at different velocities, resulting in slip between the clutch plates. The default setting is Unlocked.

## **Thermal Port**

These thermal parameters are visible only when you select a block variant that includes a thermal port.

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 25 kJ/K.

## Initial temperature

Component temperature at the start of simulation. The initial temperature influences the starting meshing or friction losses by altering the component efficiency according to an efficiency vector that you specify. The default value is 300 K.

## See Also

**Fundamental Friction Clutch** 

# **Topics**

"Gear Coupling Control Using Clutches"

# **Cycloidal Drive**

High-ratio speed reducer based on cycloidal disk motion



# Library

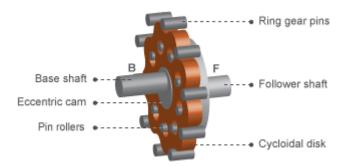
Gears

# **Description**

This block represents a compact, high-ratio, speed-reduction mechanism that contains four key components:

- · Eccentric cam
- Cycloidal disk
- · Ring-gear housing
- · Pin rollers

The eccentric cam, which extends from the base shaft, sits inside the cycloidal disk. This disk meshes with the ring-gear housing. The pin rollers, which extend from the follower shaft, sit in matching holes on the cycloidal disk.



During normal operation, the base shaft drives the eccentric cam. The cam spins inside the cycloidal disk, causing it to rotate in an eccentric pattern about an offset axis. As it moves, the cycloidal disk engages the internal teeth of the ring-gear housing. The internal meshing reverses the rotational velocity direction.

Pin rollers extending from cycloidal disk holes transmit rotational motion to the follower shaft. This shaft spins counter to the base shaft at a highly reduced speed. The large reduction ratio results from the near-equal cycloidal disk and ring gear tooth numbers. The effective gear reduction ratio is

$$r = \frac{n_R - n_C}{n_C},$$

where:

- *r* is the gear reduction ratio.
- $n_R$  is the number of teeth on the ring gear.
- $n_{\rm C}$  is the number of teeth on the cycloidal disk.

The gear reduction ratio constrains the angular velocities of the base and follower shafts according to the expression

$$\omega_F = -r\omega_B$$
,

where:

•  $\omega_{ extsf{F}}$  is the angular velocity of the follower shaft.

•  $\omega_{\rm C}$  is the angular velocity of the base shaft.

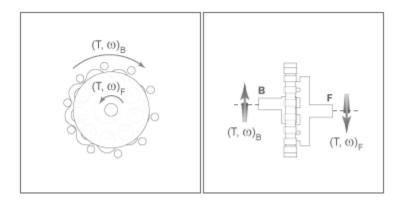
The gear reduction ratio also constrains the torques acting on the base and follower shafts, according to the expression

$$T_B = rT_F + T_f,$$

where:

- T<sub>B</sub> is the net torque at the base shaft.
- $T_{\rm F}$  is the net torque at the follower shaft.
- $T_{\rm f}$  is the torque loss due to friction. For more information, see "Model Gears with Losses".

The figure shows the cycloidal drive in front and side views. The kinematics of the drive system cause a reversal of the base and follower shaft angular velocities so that the two shafts spin in opposite directions.



The cycloidal drive can operate in reverse mode, e.g., with power flowing from the follower shaft to the base shaft. In this mode, torque transfer efficiencies are typically negligible. You can adjust the efficiency value in the block dialog box using the **Efficiency from follower shaft to base shaft** parameter.

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Specify the associated thermal parameters for the component.

## **Parameters**

#### Main

#### Number of teeth on cycloid disk

Total number of teeth projecting outward from the cycloidal disk perimeter. This number should be slightly smaller than the number of teeth or pins on the ring gear. The ratio of the gear tooth numbers defines the relative angular velocities of the base and follower shafts. The default value is 20.

### Number of teeth on ring gear

Total number of teeth or pins projecting inward from the ring gear housing. This number should be slightly larger than the number of teeth on the cycloidal disk. The ratio of the two gear tooth numbers defines the relative angular velocities of the base and follower shafts. The default value is 24.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

## Efficiency from base shaft to follower shaft

Torque transfer efficiency in normal operation mode, e.g., with the base shaft driving the follower shaft. Efficiency values must fall in the interval [0, 1]. Larger efficiency values correspond to greater torque transfer between the base and follower shafts. Values approaching unity are typical. The default value is 0.90.

## Efficiency from follower shaft to base shaft

Torque transfer efficiency in reverse operation mode, e.g., with the follower shaft driving the base shaft. Efficiency values must fall in the interval [0, 1]. Larger efficiency values correspond to greater torque transfer between base and follower shafts. Values approaching zero are typical. The default value is 0.05.

#### Power threshold

Absolute value of the cycloidal disk power above which the full efficiency factor applies. Below this value, a hyperbolic tangent function smooths the efficiency factor to one, lowering the efficiency losses to zero when at rest.

As a guideline, the power threshold should be lower than the expected power transmitted during simulation. Higher values might cause the block to underestimate efficiency losses. Very low values might, however, raise the computational cost of simulation.

The default value is 0.001 W.

#### With Thermal Port

#### **Temperature**

Array of temperatures used to construct 1-D temperature-efficiency lookup tables. The array values must increase left to right. The temperature array must be the same size as each efficiency arrays. The default array is [280 300 320] K.

## Efficiency from base shaft to follower shaft

Array of mechanical efficiencies with power flowing from the base shaft to the follower shaft. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.85 0.80].

### Efficiency from follower shaft to base shaft

Array of mechanical efficiencies with power flowing from the follower shaft to the base shaft. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.10 0.05 0.03].

#### Power threshold

Absolute value of the cycloidal disk power above which the full efficiency factor applies. A hyperbolic tangent function smooths the efficiency factor between zero when at rest and the value provided by the temperature-efficiency lookup table when at the power threshold. The default value is  $0.001\,\mathrm{W}$ .

## **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

## **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is  $300~\rm K$ .

## **Ports**

Port	Description
В	Rotational conserving port representing the base shaft
F	Rotational conserving port representing the follower shaft
Н	Thermal conserving port for thermal modeling

# See Also

Harmonic Drive | Simple Gear | Simple Gear with Variable Efficiency

# **Differential**

Gear mechanism that allows driven shafts to spin at different speeds



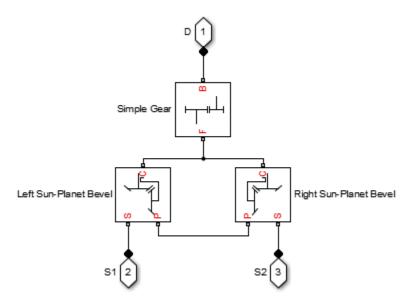
# Library

Simscape / Driveline / Gears

# **Description**

This block represents a gear mechanism that allows the driven shafts to spin at different speeds. Differentials are common in automobiles, where they enable the various wheels to spin at different speeds while cornering. Ports S, D1, and D2 represent the driving and driven shafts of the differential. Any of the shafts can drive the remaining two.

The block models the differential mechanism as a structural component based on Simple Gear and Sun-Planet Bevel Simscape Driveline blocks. The figure shows the block diagram of this structural component.



To increase the fidelity of the gear model, you can specify properties such as gear inertia, meshing losses, and viscous losses. By default, gear inertia and viscous losses are assumed negligible. The block enables you to specify the inertias of the gear carrier and internal planet gears only. To model the inertias of the outer gears, connect Simscape Inertia blocks to ports D, S1, and S2.

## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Differential Gear Model**

## **Ideal Gear Constraints and Gear Ratios**

Differential imposes one kinematic constraint on the three connected axes:

$$\omega_{\rm D} = \pm (1/2)g_{\rm D}(\omega_{\rm S1} + \omega_{\rm S2}) ,$$

with the upper (+) or lower (-) sign valid for the differential crown to the right or left, respectively, of the centerline. The three degrees of freedom reduce to two independent degrees of freedom. The gear pairs are (1,2) = (S,S) and (C,D). C is the carrier.

The sum of the lateral motions is the transformed longitudinal motion. The difference of side motions  $\omega_{S1}$  –  $\omega_{S2}$  is independent of the longitudinal motion. The general motion of the lateral shafts is a superposition of these two independent degrees of freedom, which have this physical significance:

- One degree of freedom (longitudinal) is equivalent to the two lateral shafts rotating at the same angular velocity ( $\omega_{S1} = \omega_{S2}$ ) and at a fixed ratio with respect to the longitudinal shaft.
- The other degree of freedom (differential) is equivalent to keeping the longitudinal shaft locked ( $\omega_D = 0$ ) while the lateral shafts rotate with respect to each other in opposite directions ( $\omega_{S1} = -\omega_{S2}$ ).

The torques along the lateral axes,  $\tau_{\rm S1}$  and  $\tau_{\rm S2}$ , are constrained to the longitudinal torque  $\tau_{\rm D}$  in such a way that the power flows into and out of the gear, less any power loss  $P_{\rm loss}$ , sum to zero:

$$\omega_{\rm S1}\tau_{\rm S1} + \omega_{\rm S2}\tau_{\rm S2} + \omega_{\rm D}\tau_{\rm D} - P_{\rm loss} = 0 \ .$$

When the kinematic and power constraints are combined, the ideal case yields:

$$g_{\mathrm{D}}\tau_{\mathrm{D}} = 2(\omega_{\mathrm{S1}}\tau_{\mathrm{S1}} + \omega_{\mathrm{S2}}\tau_{\mathrm{S2}}) \, / \, (\omega_{\mathrm{S1}} + \omega_{\mathrm{S2}}) \, . \label{eq:gdef}$$

#### **Fundamental Sun-Planet Bevel Gear Constraints**

The effective differential constraint is composed of two subconstraints.

• The first comes from the coupling of the two sun-planet bevel gears to the carrier:

$$(\omega_{S1} - \omega_C)/(\omega_{S2} - \omega_C) = -g_{SP2}/g_{SP1}.$$

• The second comes from the coupling of the carrier to the longitudinal driveshaft:  $\omega_{\rm D} = \pm g_{\rm D}\omega_{\rm C}$ .

 $g_{\rm SP1}=r_{\rm S1}/r_{\rm P1}$  and  $g_{\rm SP2}=r_{\rm S2}/r_{\rm P2}$  are the sun-planet gear ratios of the underlying sun-planet bevel gears, in terms of the radii r of the sun and planet gears. The Differential block is implemented with  $g_{\rm SP1}=g_{\rm SP2}=1$ , leaving  $g_{\rm D}$  free to adjust.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $au_{loss} \neq 0$  . See "Model Gears with Losses".

# **Limitations**

- Gears are assumed rigid.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
D	Rotational conserving port representing the longitudinal driveshaft
S1	Rotational conserving port representing one of the sun gears
S2	Rotational conserving port representing one of the sun gears
Н	Thermal conserving port for thermal modeling

# **Parameters**

### Main

#### **Crown wheel located**

Select the placement of the bevel crown gear with respect to the centerline of the gear assembly. The default is To the right of the centerline.

## Carrier (C) to driveshaft (D) teeth ratio (NC/ND)

Fixed ratio  $g_{\rm D}$  of the carrier gear to the longitudinal drives haft gear. The default is 4.

# **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

### **Constant Efficiency**

#### Sun-sun and carrier-driveshaft ordinary efficiencies

Vector of torque transfer efficiencies  $[\eta_{SS} \eta_D]$  for sun-sun and carrier-longitudinal driveshaft gear wheel pair meshings, respectively.

## Sun-carrier and driveshaft-casing power thresholds

Vector of power thresholds  $p_{th}$  above which full efficiency loss is applied, for sun-carrier and longitudinal driveshaft-casing  $[p_S, p_D]$ , respectively.

#### With Thermal Port

### **Temperature**

Array of temperatures used to construct 1-D temperature-efficiency lookup tables. The array values must increase left to right. The temperature array must be the same size as each efficiency arrays. The default array is [280 300 320] K.

## Sun-sun efficiency

Array of mechanical efficiencies with power flowing from one of the sun gears to the other. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

## Carrier-driveshaft efficiency

Array of mechanical efficiencies with power flowing from the gear carrier to the longitudinal driveshaft. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

### Sun-carrier and driveshaft-casing power thresholds

Array of power thresholds above which the full efficiency factors apply. Enter the thresholds for sun-carrier and longitudinal driveshaft-casing, in this order. A hyperbolic tangent function smooths the efficiency factors between zero when at rest and the values provided by the temperature-efficiency lookup tables at the power thresholds. The default array is [0.001 0.001] W.

### Viscous Losses

### Sun-carrier and driveshaft-casing viscous friction coefficients

Vector of viscous friction coefficients  $[\mu_S \mu_D]$  for the sun-carrier and longitudinal driveshaft-casing gear motions, respectively. The default is  $[0 \ 0]$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

## Inertia

#### Carrier inertia

Moment of inertia of the planet gear carrier. This value must be positive or zero. Enter 0 to ignore carrier inertia. The default value is 0 kg\*m^2.

## Planet gear inertia

Moment of inertia of the combined planet gears. This value must be positive or zero. Enter  $\theta$  to ignore gear inertia. The default value is  $\theta$  kg\*m^2.

## **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

## Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

Disk Friction Clutch | Simple Gear | Sun-Planet Bevel

## **Topics**

"Basic Motion, Torque, and Force Modeling"

<sup>&</sup>quot;Limited Slip Differential with Clutches"

<sup>&</sup>quot;Torsen Differential"

<sup>&</sup>quot;Vehicle with Four-Wheel Drive"

<sup>&</sup>quot;Model Thermal Losses in Driveline Components"

<sup>&</sup>quot;Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Disc Brake**

Frictional brake with pressure-applying cylinder and pads **Library:** Simscape / Driveline / Brakes & Detents / Rotational

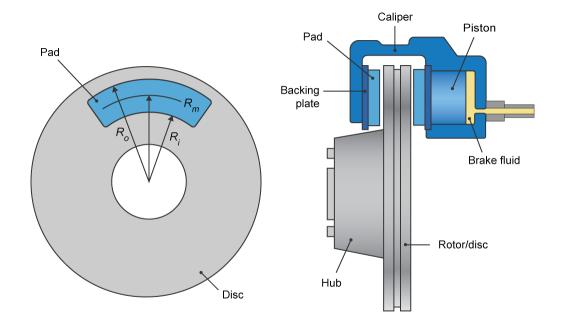


# **Description**

The Disc Brake block represents a brake arranged as a cylinder applying pressure to one or more pads that can contact the shaft rotor. Pressure from the cylinder causes the pads to exert friction torque on the shaft. The friction torque resists shaft rotation.

## **Disc Brake Model**

This figure shows the side and front views of a disc brake.



A disc brake converts brake cylinder pressure from the brake cylinder into force. The disc brake applies the force at the brake pad mean radius.

The equation that the block uses to calculate brake torque, depends on the wheel speed,  $\Omega$ , such that when  $\Omega \neq 0$ ,

$$T = \frac{\mu_k P \pi D_b^2 R_m N}{4}.$$

However when  $\Omega$  = 0, the torque applied by the brake is equal to the torque that is applied externally for wheel rotation. The maximum value of the torque that the brake can apply when  $\Omega$  = 0, is

$$T = \frac{\mu_s P \pi D_b^2 R_m N}{4}.$$

In any case, 
$$Rm = \frac{Ro + Ri}{2}$$
.

In the equations:

- *T* is the brake torque.
- *P* is the applied brake pressure.
- $\Omega$  is the wheel speed.
- *N* is the number of brake pads in disc brake assembly.
- $\mu_s$  is the disc pad-rotor coefficient of static friction.
- $\mu_k$  is the disc pad-rotor coefficient of kinetic friction.
- $D_b$  is the brake actuator bore diameter.
- $R_m$  is the mean radius of brake pad force application on brake rotor.
- $R_o$  is the outer radius of brake pad.
- $R_i$  is the inner radius of brake pad.

## **Thermal Model**

You can model the effects of heat flow and temperature change by selecting a thermal block variant. Selecting a thermal variant:

- ullet Exposes port  $oldsymbol{H}$ , a conserving port in the thermal domain.
- Enables the **Thermal mass** parameter, which allows you to specify the ability of the component to resist changes in temperature.
- Enables the **Temperature** variable, which allows you to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

To select a thermal variant, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port.

## **Ports**

## Input

### P — Cylinder pressure, bars

physical signal

Physical signal port associated with cylinder pressure.

## **Conserving**

#### S - Shaft

rotational mechanical

Rotational mechanical conserving port associated with the shaft.

#### H — Heat

thermal

The thermal conserving port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

### **Dependencies**

Selecting a thermal variant enables thermal parameters.

## **Parameters**

### Geometry

## Mean pad radius — Pad radius

150 mm (default)

Mean radius of the friction pads.

## Cylinder bore — Bore diameter

10 mm (default)

Diameter of the piston.

## Number of brake pads — Pad quantity

2 (default)

Number of friction pads.

#### Friction

### **Temperature** — **Temperature**

[280, 300, 320] K (default) | increasing vector

Independent vector for determining static and kinetic frictions. The values in the vector, in K, must increase from left to right.

### **Dependencies**

Selecting a thermal block variant for the **Block choice** parameter enables this parameter.

## Static friction coefficient — Static friction

0.9 (default) | [.9, .8, .7]

Coefficient of static friction. The value that you specify for this parameter must be greater than the value that you specify for the **Coulomb friction coefficient** parameter.

#### **Dependencies**

If you select a thermal block variant for the **Block choice** parameter, specify this parameter using a vector. The vector must contain the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector.

## Coulomb friction coefficient — Kinetic friction

0.7 (default) | [.8, .7, .6]

Coefficient of kinetic friction. The value that you specify for this parameter must be greater than 0.

### **Dependencies**

If you select a thermal block variant for the **Block choice** parameter, specify this parameter as a vector. The vector must contain the same number of elements as the temperature vector.

## Breakaway friction velocity — Friction threshold

0.1 rad/s (default)

Angular speed at which friction switches from static to kinetic.

### Viscous friction coefficient — Viscous friction

.001 N\*m/(rad/s) (default)

Coefficient of viscous friction.

#### **Thermal Port**

### Thermal mass — Resistance to temperature change

50 kj/K (default)

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change.

### **Dependencies**

Selecting a thermal block variant for the **Block choice** parameter enables this parameter.

## See Also

Band Brake | Double-Shoe Brake | Loaded-Contact Rotational Friction | Rotational Detent

#### Introduced in R2017b

## **Disk Friction Clutch**

Friction clutch with disk plates that engage when plate pressure exceeds threshold

# Library

Clutches

# **Description**

This block represents a friction clutch with two flat friction plate sets that come into contact to engage. The clutch engages when the applied plate pressure exceeds an engagement threshold pressure. Once engaged, the plates experience frictional torques that enable them to transmit power between the base and follower driveshafts.

The clutch can be bidirectional or unidirectional. A bidirectional clutch can slip in the positive and negative directions. A unidirectional clutch can slip only in the positive direction. The slip direction is positive if the follower shaft spins faster than the base shaft and negative if it slips slower. The block defines the slip velocity as the difference

$$\omega = \omega_{\rm F} - \omega_{\rm B}$$
,

where:

- $\omega$  is the slip velocity.
- $\omega_{ extsf{F}}$  is the angular velocity of the follower driveshaft.
- $\omega_B$  is the angular velocity of the base driveshaft.

The block provides a physical signal input port (P) for the applied pressure between the clutch plates. The applied pressure must be greater than or equal to zero and has units of Pascals. If the input signal falls below zero, the block treats the plate pressure as zero.

## **Disk Friction Clutch Model**

The Disk Friction Clutch is based on the Fundamental Friction Clutch. For the complete friction clutch model, consult the Fundamental Friction Clutch block reference page. This section discusses the simplified model implemented in the Disk Friction Clutch.

When you apply a pressure signal above threshold ( $P \ge P_{\rm th}$ ), the Disk Friction Clutch block can apply two kinds of friction to the driveline motion, kinetic and static. The clutch applies kinetic friction torque only when one driveline axis is spinning relative to the other driveline axis. The clutch applies static friction torque when the two driveline axes lock and spin together. The block iterates through multistep testing to determine when to lock and unlock the clutch.

## **Clutch Variable, State, and Mode Summary**

This table summarizes the clutch variables.

#### **Clutch Variables**

Symbol	Definition	Significance
ω	Relative angular velocity (slip)	$\omega_{\rm F}$ – $\omega_{\rm B}$
$\omega_{ ext{Tol}}$	Slip tolerance for clutch locking	See the following model
P, P <sub>th</sub>	Clutch pressure and threshold	Input pressure applied to clutch discs; threshold clutch pressure: $P_{\rm th}$ , $P>0$ .
$P_{ m fric}$	Clutch friction capacity	$\max[(P - P_{th}), 0]$
D	Clutch de-rating factor	See the following model
N	Number of friction surfaces	See the following model
A	Engagement surface area	See the following model
$r_{ m eff}$	Effective torque radius	Effective moment arm of clutch friction force
$k_{\mathrm{K}}$	Kinetic friction coefficient	Dimensionless coefficient of kinetic friction of clutch discs. Function of $\omega$ .
$k_{\mathrm{S}}$	Static friction coefficient	Dimensionless coefficient of static friction of clutch discs.
μ	Viscous drag coefficient	See the following model
$ au_{ m K}$	Kinetic friction torque	See the following model
$ au_{ m S}$	Static friction torque limit	(static friction peak factor)·(kinetic friction torque for $\omega \to 0$ ) (See the following model)

## **Relation to Fundamental Friction Clutch**

Instead of requiring the kinetic and static friction limit torques as input signals, the Disk Friction Clutch calculates the kinetic and static friction from the clutch parameters and the input pressure signal P.

The kinetic friction torque is the positive sum of viscous drag and surface contact friction torques:

$$\tau_{\rm K} = \mu \omega + \tau_{\rm contact}$$
.

(The kinetic friction torque opposes the relative slip and is applied with an overall minus sign.) The contact friction is a product of six factors:

$$\tau_{\text{contact}} = k_{\text{K}} \cdot D \cdot N \cdot r_{\text{eff}} \cdot P_{\text{fric}} \cdot A \ge 0$$
.

You specify the kinetic friction coefficient  $k_K$  as either a constant or a tabulated discrete function of relative angular velocity  $\omega$ . The tabulated function is assumed to be symmetric for positive and negative values of the relative angular velocity. Therefore, specify  $k_K$  for positive values of  $\omega$  only.

The clutch applies a normal force from its piston as the product of the clutch friction capacity  $P_{\rm fric}$  and engagement surface area A, on each of N friction surfaces. The pressure signal P should be nonnegative. If P is less than  $P_{\rm th}$ , the clutch applies no friction at all.

The effective torque radius  $r_{\text{eff}}$  is the effective radius, measured from the driveline axis, at which the kinetic friction forces are applied at the frictional surfaces. It is related to the geometry of the friction surface by:

$$r_{\text{eff}} = \frac{2}{3} \frac{r_0^3 - r_1^3}{r_0^2 - r_1^2}$$

 $r_{\rm o}$  and  $r_{\rm i}$  are the outer and inner radii, respectively, of the friction surface, modeled as an annular disk.

The *clutch de-rating factor D* accounts for clutch wear. For a new clutch, *D* is one. For a clutch approaching a "uniform wear" state:

$$D \to \frac{3}{4} \frac{(r_o + r_i)^2}{r_o^2 + r_o r_i + r_i^2}$$

The static friction limit is related to the kinetic friction, setting  $\omega$  to zero and replacing the kinetic with the static friction coefficient:

$$\tau_{\rm S} = k_{\rm S} {\cdot} D {\cdot} N {\cdot} r_{\rm eff} {\cdot} P_{\rm fric} {\cdot} A \geq 0 \ .$$

 $k_{\rm S} > k_{\rm K}$ , so that the torque  $\tau$  needed across the clutch to unlock it by overcoming static friction is larger than the kinetic friction at the instant of unlocking, when  $\omega = 0$ .

The static friction torque range or limits are then defined symmetrically as:

$$\tau_{\rm S} \equiv \tau_{\rm S}^+ = -\tau_{\rm S}^-$$
.

The Wait state of the Disk Friction Clutch is identical to the Wait state of the Fundamental Friction Clutch, with the replacement of the positive kinetic friction condition ( $\tau_K > 0$ ) by the positive clutch friction capacity condition ( $P \ge P_{th}$ ).

The power dissipated by the clutch is  $|\omega \cdot \tau_K|$ . The clutch dissipates power only if it is both slipping ( $\omega \neq 0$ ) and applying kinetic friction ( $\tau_K > 0$ ).

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Ports**

В

Rotational conserving port that represents the base driveshaft

F

Rotational conserving port that represents the follower driveshaft

Ρ

Physical signal input port for the applied pressure between the clutch plates

Н

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

## **Parameters**

## **Geometry**

### Force action region

Select a parameterization method to model the clutch friction geometry. The default method is Define effective radius.

• Define effective radius — Model friction geometry in terms of disk radius.

#### **Effective Radius**

### **Effective torque radius**

Effective moment arm radius  $r_{\rm eff}$  that determines the kinetic friction torque inside the clutch. The default value is 130 mm.

#### **Number of friction surfaces**

Number N of friction-generating contact surfaces inside the clutch. The default value is 4.

### Engagement piston area

Effective area A of the clutch piston when the piston is applying pressure across the clutch. The default value is  $0.001 \, \text{m}^2$ .

## Directionality

Slip directions the clutch allows between its plates. A bidirectional clutch allows positive and negative slip velocities. A unidirectional clutch allows only positive slip velocities. The default setting is Bidirectional.

The unidirectional clutch is equivalent to a friction clutch connected in parallel to a one-way clutch that disengages only when the slip velocity becomes positive. To model a unidirectional clutch with slip in the negative direction, reverse the base and follower port connections.

• Define annular region — Model friction geometry in terms of annulus dimensions. If you select this option, the visible parameters change.

### **Annular Region**

### Friction disk outside diameter

Diameter  $2r_0$  across the outer edge of the friction disk annulus. The default value is 150 mm.

#### Friction disk inside diameter

Diameter  $2r_i$  across the inner edge of the friction disk annulus. The default value is 100 mm.

#### Number of friction surfaces

Number N of friction-generating contact surfaces inside the clutch. The default value is 4.

### Engagement piston area

Effective area A of the clutch piston when the piston is applying pressure across the clutch. The default value is  $0.001 \, \text{m}^2$ .

### Directionality

Slip directions the clutch allows between its plates. A bidirectional clutch allows positive and negative slip velocities. A unidirectional clutch allows only positive slip velocities. The default setting is Bidirectional.

The unidirectional clutch is equivalent to a friction clutch connected in parallel to a one-way clutch that disengages only when the slip velocity becomes positive. To model a unidirectional clutch with slip in the negative direction, reverse the base and follower port connections.

### **Friction**

#### Friction model

Select a parameterization method to model the kinetic friction coefficient. The options and default values for this parameter depend on the variant that you select for the block.

The options are:

- Fixed kinetic friction coefficient Provide a fixed value for the kinetic friction coefficient. This option:
  - Is only visible if you use the default variant of the block
  - Is the default method for parameterizing the default variant of the block
  - Affects the visibility of other parameters

#### Fixed kinetic friction coefficient

#### Kinetic friction coefficient

The kinetic, or Coulomb, friction coefficient. The coefficient must be greater than zero. The default value is 0.3.

#### Static friction coefficient

Dimensionless Coulomb static friction coefficient  $k_{\rm S}$  applied to the normal force across the clutch when the clutch is locked.  $k_{\rm S}$  must be larger than  $k_{\rm K}$ . The default value is 0.35.

- Table lookup kinetic friction coefficient Define the kinetic friction coefficient by one-dimensional table lookup based on the relative angular velocity between disks. This option:
  - Is only visible if you use the default variant of the block
  - Affects the visibility of other parameters

## Table lookup kinetic friction coefficient

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient vector

Specify the output values for the kinetic friction coefficient as a vector. All values must be positive. The default value is [0.3, 0.22, 0.19].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Static friction coefficient

Dimensionless Coulomb static friction coefficient  $k_{\rm S}$  applied to the normal force across the clutch when the clutch is locked.  $k_{\rm S}$  must be larger than  $k_{\rm K}$ . The default value is 0.35.

- Temperature-dependent kinetic friction coefficient Define the kinetic friction coefficient by table lookup based on the temperature. This option:
  - Is only visible if you use a thermal variant of the block
  - Is the default method for parameterizing the thermal variant of the block
  - Affects the visibility of other parameters

## Temperature-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is  $[280.0,\ 300.0,\ 320.0]$  K.

### Kinetic friction coefficient vector

Specify the output values for kinetic friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. All values must be greater than zero. The default value is [0.3, 0.28, 0.25].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector.

Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

- Temperature and speed-dependent kinetic friction coefficient —
  Define the kinetic friction coefficient by table lookup based on the temperature
  and the relative angular velocity between disks. This option:
  - Is only visible if you use the thermal variant of the block
  - Affects the visibility of other parameters

## Temperature and speed-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is  $[0.0,\ 100.0,\ 1000.0]$  rad/s.

#### Kinetic friction coefficient matrix

Specify the output values for kinetic friction coefficient as a matrix. All the values must be greater than zero. The size of the matrix must equal the size of the matrix that is the result of the temperature vector  $\times$  the kinetic friction coefficient relative velocity vector. The default value is  $[0.34,\ 0.32,\ 0.3;\ 0.3,\ 0.28,\ 0.25;\ 0.25,\ 0.2,\ 0.15]$ .

### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

### **De-rating factor**

Dimensionless de-rating factor *D* that accounts for clutch disk wear by proportionately reducing clutch friction. The default value is 1.

### **Clutch velocity tolerance**

Maximum slip velocity at which the clutch can lock. The slip velocity is the signed difference between the base and follower shaft angular velocities, that is,

 $w=w_F-w_B$ . If the kinetic friction torque is nonzero and the transferred torque is within the static friction torque limits, then the clutch locks if the actual slip velocity falls below the velocity tolerance. The default value is 0.001 rad/s.

### **Engagement threshold pressure**

Minimum pressure  $P_{\rm th}$  at which the clutch engages. If the pressure input signal falls below this threshold, the clutch automatically disengages. The default value is 100 Pa.

## **Viscous Drag**

## Viscous drag torque coefficient

Viscous friction coefficient  $\mu$  applied to the relative slip  $\omega$  between the base and follower axes. The default value is 0 N\*m/(rad/s).

## **Initial Conditions**

#### **Initial state**

Clutch state at the start of simulation. The clutch can be in one of two states, locked and unlocked. A locked clutch constrains the base and follower shafts to spin at the same velocity, that is, as a single unit. An unlocked clutch allows the two shafts to spin at different velocities, resulting in slip between the clutch plates. The default setting is Unlocked.

## **Thermal Port**

These thermal parameters are only visible when you select a block variant that includes a thermal port.

### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is  $25\ kJ/K$ .

### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is  $300 \, \text{K}$ .

## See Also

Differential | Fundamental Friction Clutch | Torque Converter | Variable Ratio Transmission

## **Topics**

"Gear Coupling Control Using Clutches"

"Clutches For Accelerating and Braking"

"CR-CR Four-Speed Transmission"

"Custom Clutch"

"Hydraulically-Actuated Driveline Clutch"

"Two-Speed Transmission"

"Vehicle with Dual Clutch Transmission"

Vehicle with Four-Speed Transmission

# **Dog Clutch**

Clutch with toothed plates that engage when plate teeth become enmeshed



# Library

Simscape / Driveline / Clutches

# **Description**

This block represents a nonslip clutch, a mechanical device that relies on the positive engagement of interlocking teeth to transfer torque between driveline shafts. The clutch contains three key components:

- Ring
- Hub
- Shift linkage

The ring and the hub are toothed components. The ring spins with the output shaft, sliding along its longitudinal axis to engage or disengage the coaxial hub. The hub, which sits on a bearing encircling the same shaft, can spin independently until engaged.

Engagement occurs when the toothed components interlock. Once engaged, the ring and the hub spin together as a unit. To control engagement, the dog clutch contains a shift linkage that governs the position of the ring with respect to the hub.

Moving the ring towards the hub so that their teeth interlock changes the clutch state to engaged. Tooth overlap must exceed a minimum value for engagement. Moving the ring in reverse so that the two sets of teeth no longer interlock changes the clutch state back to disengaged.

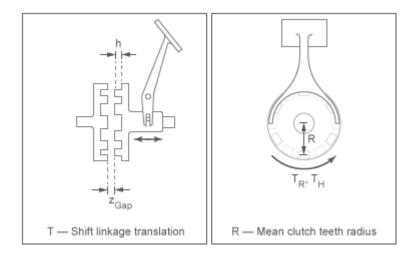
The translational conserving port S specifies the shift linkage position. When the clutch is fully disengaged, the shift linkage position is zero. When the clutch is fully engaged, the shift linkage position equals the sum of the tooth height and the ring-hub clearance of the fully disengaged state:

$$z = h + z_{Gap},$$

#### where:

- z is the shift linkage position.
- *h* is the tooth height.
- $z_{Gap}$  is the ring-hub clearance when disengaged.

The figure shows side and front views of the dog clutch and some of its relevant variables.



## **Torque Transmission Models**

The Dog Clutch block provides a choice of two torque transmission models.

Treat clutch engagement as a friction phenomenon between the ring and the hub. This model ignores special effects such as backlash, an approximation that makes the block better suited for linearization, fixed-step simulation, and hardware-in-loop (HIL) simulation. The Fundamental Friction Clutch block provides the foundation for the model.

In the friction approximate model, the clutch has three possible configurations: disengaged, engaged, and locked. When disengaged, the contact force between the ring and the hub is zero. This force remains zero until the shift linkage reaches the minimum position for engagement.

When the ring-hub tooth overlap (h) exceeds the minimum value for engagement, the contact force between the two components begins to increase linearly with the shift linkage position (z).

At full engagement, the contact force reaches its maximum value, and the clutch state switched to locked. In this state, the ring and the hub spin as a unit without slip. To unlock the clutch, the transmitted torque must exceed the maximum allowed value that you specify.

Capture clutch phenomena such as backlash, torsional compliance, and contact forces between ring and hub teeth. This model provides greater accuracy than the friction clutch approximation.

In the dynamic model, the clutch has two possible configurations: disengaged and engaged. When disengaged, the contact force between the ring and the hub is zero. This force remains zero until the shift linkage reaches the minimum position for engagement.

When the ring-hub tooth overlap (h) exceeds the minimum value for engagement, a contact force kicks in between the two components. This force is the sum of torsional spring and damper components. Including backlash between the ring and hub teeth:

$$T_C = \begin{cases} -k_{RH} \left(\phi - \frac{\delta}{2}\right) - \mu_R \cdot \omega & \phi > \frac{\delta}{2} \\ \\ 0 & -\frac{\delta}{2} < \phi < \frac{\delta}{2}, \\ -k_{RH} \left(\phi + \frac{\delta}{2}\right) - \mu_R \omega & \phi < -\frac{\delta}{2} \end{cases}$$

where:

- $k_{\rm RH}$  is the torsional stiffness of the ring-hub coupling.
- $\phi$  is the relative angle, about the common rotation axis, between the ring and the hub.
- $\delta$  is the backlash between ring and hub teeth.

•  $\omega$  is the relative angular velocity between the ring and the hub. This variable describes how fast the two components slip past each other.

Compliant end stops limit the translational motion of the clutch shift linkage and the ring. The compliance model treats the end stops as linear spring-damper sets. The location of the end stops depends on the relative angle and angular velocity between the ring and hub teeth:

- If the teeth align and the relative angular velocity is smaller than the maximum value for clutch engagement, the end-stop location is the sum of the ring-hub clearance when fully disengaged and the tooth height. With the end stop at this location, the clutch can engage.
- If the teeth do not align or the relative angular velocity exceeds the maximum value for clutch engagement, the end-stop location is set to prevent the ring from engaging the hub. The clutch remains disengaged.

Translational friction opposes shift linkage and ring motion. This friction is the sum of Coulomb and viscous components:

$$F_Z = -k_K \cdot F_N \cdot \tanh\left(\frac{4v}{v_{th}}\right) - \mu_T v,$$

where:

- $F_Z$  is the net translational friction force acting on the shift linkage and ring.
- $k_{\rm K}$  is the kinetic friction coefficient between ring and hub teeth.
- $F_{\rm N}$  is the normal force between ring and hub teeth.
- v is the translational velocity of the shift linkage and the ring.
- $v_{th}$  is the translational velocity threshold. Below this threshold, a hyperbolic tangent function smooths the Coulomb friction force to zero as the shift linkage and ring velocity tends to zero.
- $\mu_{\mathrm{T}}$  is the viscous damping coefficient acting on the shift linkage and the ring.

## **Clutch Engagement Conditions**

The clutch engages when it satisfies a set of geometrical and dynamic conditions. These conditions specify the values that certain variables can take for clutch engagement to occur:

The minimum position at which the ring and the hub can engage is

$$z = h_0 \, + z_{Gap},$$

where  $h_0$  is the minimum tooth overlap for clutch engagement. Adjust this parameter to minimize engagement instability, that is, the tendency of the clutch to switch rapidly between engaged and disengaged states

 The magnitude of the relative angular velocity between the ring and the hub must be smaller than the maximum engagement velocity:

$$|\omega| < |\omega_{\max}|$$

where  $\omega_{\max}$  is the maximum value of the relative angular velocity at which engagement can occur.

- If using the friction clutch approximate model, engagement occurs only if torque transfer between the ring and the hub remains smaller than the maximum transmitted torque that the clutch supports.
- If using the dynamic model with backlash, engagement occurs only if the relative angular position of the ring and hub teeth allows them to interlock.

## **Rotational Power Dissipation**

When the clutch slips under an applied torque, it dissipates power. The power loss equals the product of the slip angular velocity and the contact torque between the ring and the hub:

$$P_{loss} = \omega \cdot T_C$$

where:

- $P_{\rm loss}$  is the dissipated power due to slipping.
- $T_{\rm C}$  is the kinetic contact torque.

# **Shift Linkage and Thermal Variants**

The block provides four variants:

- · Mechanical port shift linkage
- Mechanical port shift linkage and thermal port
- Physical signal position input
- · Physical signal position input and thermal port

One of the two shift linkage variants accepts the position input through a physical signal port, the other through a translational conserving port. To model thermal effects, you can add a thermal port to either of the shift linkage variants.

To change from the current variant, right-click the block in your model and, under **Simscape > Block choices**, and select the desired variant. Changing the variant changes the ports and parameters.

## **Ports**

S

Translational conserving port or physical signal port that represents the shift linkage. The port type depends on the shift linkage variant that you select.

Χ

Physical signal port for sensing the clutch position

Τ

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

R

Rotational conserving port that represents the clutch ring

Н

Rotational conserving port that represents the clutch hub

## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Parameters**

### Clutch

If you select **Physical signal position input** or **Mechanical port shift linkage** as the variant for the Dog Clutch block, parameter visibility depends on the value that you select for the **Torque transmission model** parameter.

### **Torque transmission model**

### Torque transmission model

Computational framework for modeling the dynamic behavior of the dog clutch. The default setting is Friction clutch approximation — Suitable for HIL and linearization.

• Friction clutch approximation - Suitable for HIL and linearization — Model clutch engagement as a friction phenomenon between the ring and the hub. This model, based on the Fundamental Friction Clutch block, provides a computationally efficient approximation of the dog clutch.

## **Friction Clutch Approximation**

## Maximum transmitted torque

Largest torque that the clutch can transmit, corresponding to a nonslip engaged configuration. If the torque transmitted between the ring and the hub exceeds this value, the two components begin to slip with respect to each other. This torque determines the static friction limit in the friction clutch approximation. The default is  $1000 \, N^*m$ .

#### Clutch teeth mean radius

Distance from the ring or hub center to the corresponding tooth center. The mean tooth radius determines the normal contact forces between ring and hub teeth given the transmission torque between the two components. The mean radius is greater than zero. The default value is 50 mm.

 Dynamic with backlash — Model clutch engagement in detail, accounting for such phenomena as backlash, torsional compliance, and contact forces between ring and hub teeth. Selecting this option causes additional Shift Linkage and Initial Conditions parameters to appear.

### **Dynamic with Backlash**

#### Number of teeth

Total number of teeth in the ring or the hub. The two components have equal tooth numbers. The number of teeth is greater than or equal to one. The default value is 6.

### **Rotational backlash**

Allowable angular motion, or play, between the ring and hub teeth in the engaged clutch configuration. The backlash is greater than zero. The default value is 10 deg.

### **Torsional stiffness**

Linear torsional stiffness coefficient at the contact interface between the ring and hub teeth. This coefficient characterizes the restoring component of the contact force between the two sets of teeth. Greater stiffness values correspond to greater contact forces. The stiffness coefficient is greater than zero. The default value is 1e+7 N\*m/rad.

### Torsional damping

Linear torsional damping coefficient at the contact interface between the ring and hub teeth. This coefficient characterizes the dissipative component of the contact force between the two sets of teeth. Greater damping values correspond to greater energy dissipation during contact. The damping coefficient is greater than zero. The default value is 100 N\*m/(rad/s).

Selecting a thermal variant for the Dog Clutch block, makes other **Clutch** parameters visible.

### **Clutch Parameters for Thermal Variants**

### **Temperature vector**

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

## Maximum transmitted torque vector

Largest torque that the clutch can transmit, corresponding to a nonslip engaged configuration, specified as a vector. If the torque transmitted between the ring and the hub exceeds this value, the two components begin to slip with respect to each

other. This torque determines the static friction limit in the friction clutch approximation. The vector has the same number of elements as the temperature vector. The default value is [1000.0, 1050.0, 1000.0] N\*m.

### Interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous firstorder derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### **Extrapolation method**

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous firstorder derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Clutch teeth mean radius

Distance from the ring or hub center to the corresponding tooth center. The mean tooth radius determines the normal contact forces between ring and hub teeth given the transmission torque between the two components. The mean radius is greater than zero. The default value is 50 mm.

## **Shift Linkage**

### Tooth height

Distance between the base and crest of a tooth. Ring and hub teeth share the same height. The tooth height and the ring-hub clearance when fully disengaged determine the maximum travel span of the shift linkage. The tooth height is greater than zero. The default value is 10 mm.

### Hard stop at back of shift linkage

Choice of translational motion limiting device. Select whether to stop the shift linkage when fully disengaged. The default option is Hard stop when fully disengaged.

This parameter is only visible if you select one of these variants for the block:

- Mechanical port shift linkage
- Mechanical port shift linkage and thermal port

### Ring-hub clearance when disengaged

Maximum open gap between the ring and hub tooth crests along the shift linkage translation axis. This gap corresponds to the fully disengaged clutch state. The tooth height and the ring-hub clearance when fully disengaged determine the maximum travel span of the shift linkage. The ring-hub clearance is greater than zero. The default value is 3 mm.

### Ring stop stiffness

Linear stiffness coefficient of the ring end stop. This coefficient characterizes the restoring component of the contact force that resists translational motion past the end stops. Greater stiffness values correspond to greater contact forces and a smaller end stop compliance. The stiffness coefficient is greater than zero. The default value is 1e+6 N/m.

This parameter is only visible if you select one of these variants for the block:

- Mechanical port shift linkage
- Mechanical port shift linkage and thermal port

## Ring stop damping

Linear damping coefficient of the ring end stop. This coefficient characterizes the dissipative component of the contact force that resists translational motion past the end stops. Greater damping values correspond to greater energy dissipation during contact. The damping coefficient is greater than or equal to zero. The default value is 1000 N/(m/s).

This parameter is only visible if you select one of these variants for the block:

- · Mechanical port shift linkage
- Mechanical port shift linkage and thermal port

### Shift linkage viscous friction coefficient

Linear damping coefficient acting on the shift linkage. This coefficient characterizes the dissipative force that resists shift linkage motion due to viscous damping. Greater coefficient values correspond to greater energy dissipation during shift linkage motion. The viscous friction coefficient is greater than zero. The default value is  $100 \, \text{N/(m/s)}$ .

This parameter is only visible if you select one of these variants for the block:

- · Mechanical port shift linkage
- Mechanical port shift linkage and thermal port

#### **Tooth-tooth friction coefficient**

Kinetic friction coefficient at the contact interface between ring and hub teeth. This coefficient characterizes the dissipative force that resists shift linkage motion due to tooth-tooth contact during clutch engagement/disengagement.

Greater coefficient values correspond to greater energy dissipation during shift linkage motion. The friction coefficient is greater than zero. The default value is 0.05.

This parameter is only visible if you select the **Mechanical port shift linkage** variant for the block and set the **Torque transmission model** parameter to Dynamic with backlash.

## **Engagement Conditions**

## Linkage travel direction

Direction the shift linkage must travel in to engage the clutch. Choices include positive and negative displacements. The default setting is Positive shift linkage displacement engages clutch.

## Maximum engagement velocity

Relative angular velocity between the ring and the hub above which the clutch cannot engage. The maximum engagement velocity is greater than zero. The default value is inf (infinity) rad/s.

This parameter is only visible if you select one of these variants for the block:

## · Mechanical port shift linkage

### Mechanical port shift linkage and thermal port

### Tooth overlap to engage

Overlap length between ring and hub teeth along the common longitudinal axis above which the clutch can engage. The clutch remains disengaged until the tooth overlap by at least this length. The tooth overlap to engage is greater than zero. The default value is 3 mm.

## **Initial Conditions**

#### **Clutch Initial state**

Clutch configuration at the start of simulation. Options include:

- Disengaged Clutch transmits zero torque between the ring and the hub.
   Disengagedis the default value.
- Engaged Clutch transmits torque between the ring and the hub.

If you select **Physical signal position input** for the block variant, this parameter is only visible if you set the **Torque transmission model** parameter to Friction clutch approximation - Suitable for HIL and linearization.

## Initial shift linkage position

Shift linkage position at simulation time zero. Values between zero and the sum of the ring-hub clearance and the tooth overlap to engage are consistent with a disengaged clutch. Larger values are consistent with an engaged clutch. The default value is  $\theta$  mm.

This parameter is only visible if you select one of these variants for the block:

- · Mechanical port shift linkage
- Mechanical port shift linkage and thermal port

## Initial ring-hub offset angle

Rotation angle between the ring and the hub at simulation time zero. This angle determines whether the ring and hub teeth can interlock, and hence whether the clutch can engage. The initial offset angle must satisfy these conditions:

 If the clutch initial state is disengaged, the initial offset angle must fall in the range

$$-\frac{180^{\circ}}{N} \le \phi_0 \le +\frac{180^{\circ}}{N},$$

where N is the number of teeth present in the ring or the hub. The two components contain the same number of teeth.

If the clutch initial state is engaged, the initial offset angle must fall in the range

$$-\frac{\delta}{2} \leq \phi_0 \leq +\frac{\delta}{2},$$

where  $\delta$  is the backlash angle between the ring and hub teeth.

The default value is 0 deg.

This parameter is only visible if you satisfy both of these conditions:

- For the block variant, select Mechanical port shift linkage or Physical signal position input
- Set the Torque transmission model parameter to Dynamic with backlash.

## **Thermal Port**

These thermal parameters are only visible when you select a block variant that includes a thermal port.

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 25 kJ/K.

## Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is  $300 \, \text{K}$ .

# **Extended Capabilities**

### Linearization

To optimize your model for linearization, use the **Clutch > Torque transmission model** parameter default setting, Friction clutch approximation - Suitable for HIL and linearization.

## **Real-Time and Hardware-in-the-Loop Simulation**

For optimal simulation performance, use the **Clutch > Torque transmission model** parameter default setting, Friction clutch approximation - Suitable for HIL and linearization.

## See Also

### **Simscape Blocks**

Fundamental Friction Clutch | Loaded-Contact Rotational Friction | Torsional Spring-Damper

## **Topics**

- "Gear Coupling Control Using Clutches"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Double-Pinion Planetary Gear**

Planetary gear train with two meshed planet gear sets

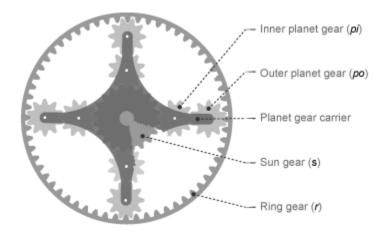


# Library

Simscape / Driveline / Gears

# **Description**

This block represents a planetary gear train with two meshed planet gear sets between the sun gear and the ring gear. A single carrier holds the two planet gear sets at different radii from the sun gear centerline, while allowing the individual gears to rotate with respect to each other. The gear model includes power losses due to friction between meshing gear teeth and viscous damping of the spinning gear shafts.



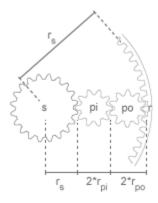
Structurally, the double-pinion planetary gear resembles a Ravigneaux gear without its second, large, sun gear. The inner planet gears mesh with the sun gear and the outer planet gears mesh with the ring gear. Because it contains two planet gear sets, the double-pinion planetary gear reverses the relative rotation directions of the ring and sun gears.

The teeth ratio of a meshed gear pair fixes the relative angular velocities of the two gears in that pair. The dialog box provides two parameters to set the ring-sun and outer planet-inner planet gear teeth ratios. A geometric constraint fixes the remaining teeth ratios—ring-outer planet and inner planet-sun. This geometric constraint requires that the ring gear radius equal the sum of the sun gear radius with the inner and outer planet gear diameters:

$$r_r = r_s + 2 \cdot r_{pi} + 2 \cdot r_{po},$$

#### where:

- $r_r$  is the ring gear radius
- $r_s$  is the sun gear radius
- $r_{pi}$  is the inner planet gear radius
- $r_{po}$  is the outer planet gear radius



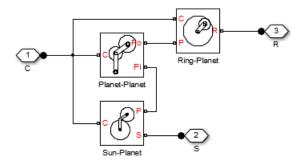
In terms of the ring-sun and outer planet-inner planet teeth ratios, the ring-outer planet teeth ratio is

$$rac{r_r}{r_{po}} = 2 \cdot rac{rac{r_r}{r_s}}{\left(rac{r_r}{r_s} - 1
ight)} \cdot rac{\left(rac{r_{po}}{r_{pi}} + 1
ight)}{rac{r_{po}}{r_{pi}}},$$

The inner planet-sun teeth ratio is

$$\frac{r_{pi}}{r_s} = \frac{\left(\frac{r_r}{r_s} - 1\right)}{2\left(\frac{r_{po}}{r_{pi}} + 1\right)},$$

The Differential block is a composite component. It contains three underlying blocks—Ring-Planet, Planet-Planet, and Sun-Planet—connected as shown in the figure. Each block connects to a separate drive shaft through a rotational conserving port.



## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Ports**

Port	Description	
С	Rotational conserving port representing the planet gear carrier	
S	Rotational conserving port representing the sun gear	
R	Rotational conserving port representing the ring gear	
Н	Thermal conserving port for thermal modeling	

## **Parameters**

## Main

### Ring (R) to sun (S) teeth ratio (NR/NS)

Teeth ratio between the ring and sun gears. This ratio is the number of teeth in the ring gear divided by the number of teeth in the sun gear. The default value is 2.

## Outer planet (Po) to inner planet (Pi) teeth ratio (NPo/NPi)

Teeth ratio between the outer-planet and inner-planet gears. This ratio is the number of teeth in the outer planet divided by the number of gear teeth in the inner planet. The default value is 1.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

List of friction models at various precision levels for estimating power losses due to meshing.

• No meshing losses - Suitable for HIL simulation — Neglect friction between gear cogs. Meshing is ideal.

• Constant efficiency — Reduce torque transfer by a constant efficiency factor. This factor falls in the range  $0 < \eta \le 1$  and is independent of load. Selecting this option exposes additional parameters.

### Sun-planet, ring-planet, and planet-planet ordinary efficiencies

Array of mechanical efficiencies between sun-planet, ring-planet, and planet-planet gear pairs, in that order. The default vector is [0.98 0.98 0.98].

### Sun-carrier, ring-carrier, and planet-carrier power thresholds

Array of power thresholds above which the full efficiency factors apply. Enter the thresholds in the order sun-carrier, ring-carrier, and planet-carrier. A hyperbolic tangent function smooths the efficiency factors from zero when at rest to the full efficiency values at the power thresholds.

As a guideline, the power threshold should be lower than the expected power transmitted during simulation. Higher values might cause the block to underestimate efficiency losses. Very low values might, however, raise the computational cost of simulation. The default vector is [0.001 0.001 0.001] W.

#### With Thermal Port

### **Temperature**

Array of temperatures used to construct 1-D temperature-efficiency lookup tables. The array values must increase left to right. The temperature array must be the same size as the efficiency arrays. The default array is [280 300 320] K.

## **Sun-planet efficiency**

Array of mechanical efficiencies with power flowing from the sun gear to the planet gears. Each array element is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.75 0.65 0.60].

## Ring-planet efficiency

Array of mechanical efficiencies with power flowing from the ring gear to the planet gears. Each array element is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.50 0.45 0.40].

## Planet-planet efficiency

Array of mechanical efficiencies with power flowing from the inner planet gears to the outer planet gears. Each array value is the ratio of output power to input power at

one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.50 0.45 0.40].

### Sun-carrier, ring-carrier and planet-carrier power thresholds

Array of power thresholds above which the full efficiency factors apply. Enter the thresholds in the order sun-carrier, ring-carrier, and planet-carrier. A hyperbolic tangent function smooths the efficiency factors between zero when at rest and the values provided by the temperature-efficiency lookup tables when at the power threshold. The default array is [0.001 0.001 0.001] W.

### Viscous Losses

Specify the power losses due to viscous damping of the gear carriers.

### Sun-carrier, ring-carrier, and planet-carrier viscous friction coefficients

Enter a vector with the viscous friction coefficients that dampen sun-carrier, ring-carrier, and planet-carrier motion, in that order. From the drop-down list, select a physical unit. The default vector is  $[0\ 0\ 0]\ N*m/(rad/s)$ .

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

# **See Also**

# **Simscape Blocks**

Compound Planetary Gear | Planetary Gear | Ravigneaux Gear

# **Topics**

"Model Thermal Losses in Driveline Components"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Double-Shoe Brake**

Frictional brake with two pivoted shoes diametrically positioned about a rotating drum

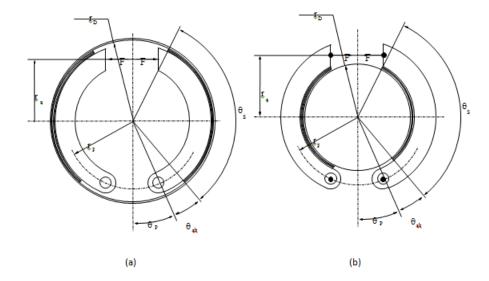


# Library

Brakes & Detents/Rotational

# **Description**

The block represents a frictional brake with two pivoted rigid shoes that press against a rotating drum to produce a braking action. The rigid shoes sit inside or outside the rotating drum in a diametrically opposed configuration. A positive actuating force causes the rigid shoes to press against the rotating drum. Viscous and contact friction between the drum and the rigid shoe surfaces cause the rotating drum to decelerate. Double-shoe brakes provide high braking torque with small actuator deflections in applications that include motor vehicles and some heavy machinery. The model employs a simple parameterization with readily accessible brake geometry and friction parameters.



In this schematic, a) represents an internal double-shoe brake, and b) represents an external double-shoe brake. In both configurations, a positive actuation force F brings the shoe and drum friction surfaces into contact. The result is a friction torque that causes deceleration of the rotating drum. Zero and negative forces do not bring the shoe and drum friction surfaces into contact and produce zero braking torque.

The model uses the long-shoe approximation. Contact angles smaller than 45° produce less accurate results. The equations for the friction torque that the leading and trailing shoes develop are:

$$T_{LS} = \frac{c\mu p_a r_D^{\ 2} \left(\cos\theta_{sb} - \cos\theta_s\right)}{\sin\theta_a},$$

$$T_{TS} = \frac{c\mu p_b r_D^{\ 2} \left(\cos\theta_{sb} - \cos\theta_s\right)}{\sin\theta_a}, \label{eq:TS}$$

$$c = r_a + r_p \cos \theta_p,$$

where for 
$$0 \le \theta_s \le \pi/2$$
 , 
$$\theta_a = \theta_s,$$
 and for  $\theta_s \ge \pi/2$  , 
$$\theta_a = \frac{\pi}{2}.$$

The parameters in the friction torque equations are:

Parameter	Description
$T_{LS}$	Brake torque the leading shoe develops
$T_{TS}$	Brake torque the trailing shoe develops
μ	Effective contact friction coefficient
$p_a$	Maximum linear pressure in the leading shoe-drum contact
$p_b$	Maximum linear pressure in the trailing shoe-drum contact
$r_{D}$	Drum radius
$\overline{ heta_{sb}}$	Shoe beginning angle
$\overline{ heta_s}$	Shoe span angle
$oldsymbol{ heta}_a$	Angle from hinge pin to maximum pressure point
C	Arm length of the cylinder force with respect to the hinge pin
$r_p$	Pin location radius
$\overline{ heta_p}$	Hinge pin location angle
$r_a$	Actuator location radius

The model assumes that only Coulomb friction acts at the shoe-drum surface contact. Zero relative velocity between the drum and the shoes produces zero Coulomb friction. To

avoid discontinuity at zero relative velocity, the friction coefficient formula employs this hyperbolic function

$$\mu = \mu_{Coulomb} \tanh \left( \frac{4\omega_{shaft}}{\omega_{threshold}} \right),$$

where:

Parameter	Description	
μ	Effective contact friction coefficient	
$\mu_{Coulomb}$	Contact friction coefficient	
$\omega_{shaft}$	Shaft velocity	
$\omega_{threshold}$	Angular velocity threshold	

Balancing the moments that act on each shoe with respect to the pin yields the pressure acting at the shoe-drum surface contact. The equations for determining the balance of moments for the leading shoe are

$$F = \frac{M_N - M_F}{c},$$

$$\boldsymbol{M}_{N} = \frac{\boldsymbol{p}_{a}\boldsymbol{r}_{p}\boldsymbol{r}_{D}}{\sin\theta_{a}} \bigg( \frac{1}{2} \big[ \boldsymbol{\theta}_{s} - \boldsymbol{\theta}_{sb} \big] - \frac{1}{4} \big[ \sin 2\theta_{s} - \sin 2\theta_{sb} \big] \bigg),$$

and

$$M_F = \frac{\mu p_a r_D}{\sin \theta_a} \left( r_D \left[ \cos \theta_{sb} - \cos \theta_s \right] + \frac{r_p}{4} \left[ \cos 2\theta_s - \cos 2\theta_{sb} \right] \right),$$

where:

Parameter	Description
F	Actuation Force

Parameter	Description	
$M_N$	Moment acting on the leading shoe due to normal force	
$M_F$	Moment acting on the leading shoe due to friction force	
С	Arm length of the cylinder force with respect to the hinge pin	
$p_a$	Maximum linear pressure at the shoe-drum contact surface	
$r_p$	Pin location radius	
$\theta_p$	Hinge pin location angle	
$r_a$	Actuator location radius	

The model does not simulate self-locking brakes. If brake geometry and friction parameters cause a self-locking condition, the model produces a simulation error. A brake self-locks if the friction moment exceeds the moment due to normal forces, that is, when  $M_F > M_N$ .

The balance of moments for the trailing shoe is

$$F = \frac{M_N + M_F}{c}.$$

The net braking torque is

$$T = T_{LS} + T_{TS} + \mu_{visc} * \omega_{shaft},$$

where  $\mu_{\textit{visc}}$  is the viscous friction coefficient.

# **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations

corresponding to the selected block configuration, the values specified for this variable are ignored.

# **Assumptions and Limitations**

- The brake uses the long-shoe approximation.
- The brake geometry does not self-lock.
- The model does not account for actuator flow consumption.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Ports**

F

Physical signal port that represents the brake actuating force

S

Rotational conserving port that represents the rotating drum shaft

Н

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

### **Parameters**

# **Geometry**

#### Drum radius

Radius of the drum contact surface. The parameter must be greater than zero. The default value is 150 mm.

#### **Actuator location radius**

Distance between the drum center and the force line of action. The parameter must be greater than zero. The default value is 100 mm.

#### Pin location radius

Distance between the hinge pin and drum centers. The parameter must be greater than zero. The default value is 125 mm.

#### Pin location angle

Angular coordinate of the hinge pin location from the brake symmetry axis. The parameter must be greater than or equal to zero. The default value is 15 deg.

### Shoe beginning angle

Angle between the hinge pin and the beginning of the friction material linen of the shoe. The value of the parameter must be in the range  $0 \le \theta_{sb} \le (\pi\text{-pin location angle})$ . The default value is 5 deg.

# Shoe span angle

Angle between the beginning and the end of the friction material linen on the shoe. The value of the parameter must be in the range  $0 < \theta_{sb} \le (\pi$  -pin location angle - shoe beginning angle). The default value is 120 deg.

### **Friction**

#### Viscous friction coefficient

Value of the viscous friction coefficient at the contact surface. The parameter must be greater than or equal to zero. The default value is  $.01 \, n*m/(rad/s)$ .

### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The default value is [280.0, 300.0, 320.0] K.

This parameter is visible only when you select a block variant that includes a thermal port.

#### **Contact friction coefficient**

Value of the Coulomb friction coefficient at the belt-drum contact surface. The value is greater than zero. Unless you select a block variant that includes a thermal port, the default value is 0.3.

If you select a block variant that includes a thermal port, you specify this parameter as array. The array is the same size as the array for the **Temperature** parameter. The default value for the thermal variant is [0.1, 0.05, 0.03].

### Angular velocity threshold

Angular velocity at which the contact friction coefficient practically reaches its steady-state value. The parameter must be greater than zero. The default value is 0.01 rad/s.

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. This parameter is enabled only if you select a block variant that includes a thermal port. The default value is 50 kJ/K.

# **See Also**

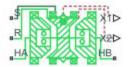
Band Brake | Loaded-Contact Rotational Friction | Rotational Detent

# **Topics**

"Model Thermal Losses in Driveline Components"

# **Double-Sided Synchronizer**

Back-to-back dog-cone clutch pairs assembled symmetrically about a translational detent to provide smooth gear engagement

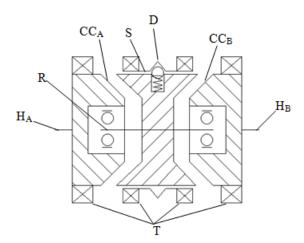


# Library

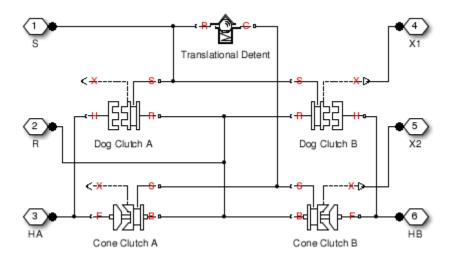
Simscape / Driveline / Clutches

# **Description**

The block represents a double-sided synchronizer that contains two back-to-back dog clutches, two back-to-back cone clutches, and one translational detent. Shift linkage translation along the negative direction causes the clutches to engage the ring with hub A. Shift linkage translation along the positive direction causes the clutches to engage the ring with hub B. When the magnitude of the shift linkage translation is smaller than the cone clutch ring-hub gap, the synchronizer is in neutral mode and does not transmit torque.



The schematic illustrates a double-sided synchronizer in the disengaged state. In this state, the ring (R) and hub ( $H_A$  and  $H_B$ ) shafts can spin independently at different speeds. As the shift linkage (S) translates in the negative direction, the faces of cone clutch A ( $CC_A$ ) come into contact. The friction in the cone clutch decreases the difference in rotational speed between the shafts. When the force on the shift linkage exceeds the peak force of detent (D), the dog clutch teeth (T) can engage. The detent peak force should be such that the cone clutch has enough time and normal force to bring the shafts to sufficiently similar speeds to allow engagement of the dog clutch. Similarly, translating the shift linkage along the positive direction allows the faces of cone clutch B ( $CC_B$ ) to come into contact, and can allow the shaft of the ring to engage with the shaft of the hub B ( $CC_B$ ).



The model implements two Dog Clutch blocks, one Translational Detent, and two modified Dog Clutch blocks. Refer to each block reference page for more information on the corresponding block function.

Connections R,  $H_A$ , and  $H_B$  are mechanical rotational conserving ports that represent the ring (R), hub A ( $H_A$ ), and hub B ( $H_B$ ), respectively. Connection S is a mechanical translational conserving port that represents the ring shifter handle.

Connections X1 and X2 are physical signal ports that output the shift linkage positions of the dog clutches and cone clutches, respectively. The following tables provide the values of X1 and X2 in common clutch engagement cases.

Dog Clutch State	X1
Disengaged	0
Fully engaged with hub A	Negative sum of ring-hub gap and tooth height
Fully engaged with hub B	Positive sum of ring-hub gap and tooth height

Cone Clutch State	X2
Disengaged	0

Cone Clutch State	X2	
Fully engaged with hub A	Negative value of ring-hub gap	
Fully engaged with hub B	Positive value of ring-hub gap	

The values of X1 and X2 are zero when the synchronizer is fully disengaged. When the dog clutch is fully engaged with hub A, X1 is equal to the negative sum of its ring-hub gap and tooth height. When the dog clutch is fully engaged with hub B, X1 is equal to the positive sum of its ring-hub gap and tooth height. When the cone clutch is fully engaged with hub A, X2 is equal to the negative of its ring-hub gap. When the cone clutch is fully engaged with hub B, X2 is equal to its ring-hub gap.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Assumptions and Limitations**

• The model does not account for inertia effects. You can add a Simscape Inertia block at each port to add inertia to the synchronizer model.

# **Ports**

S

Conserving translational port that represents the shift linkage

R

Conserving rotational port that represents the ring shaft

HA

Conserving rotational port that represents hub shaft A

HB

Conserving rotational port that represents hub shaft B

Х1

Physical signal output port that measures the magnitude of the dog clutch translation

X2

Physical signal output port that measures the magnitude of the cone clutch translation

Т

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

# **Parameters**

# **Dog Clutch**

The methods that are available for parameterizing the torque transmission depend on the variant of the block that you use. If you use the default variant, which has no thermal port, you parameterize the block using one of the options for the **Torque Transmission Model** parameter. If you select a variant that has a thermal port, you parameterize the block based on temperature. The models provide these common parameters:

#### Clutch teeth mean radius

Mean radius of the clutch teeth. The parameter must be greater than zero. The default value is 50 mm.

#### Maximum engagement speed

The relative angular speed between the ring and hub shafts above which the dog clutch cannot engage. The value is specific to the specific gearbox or transmission and must be minimized to avoid high dynamic impact during engagement. The default value is inf rad/s.

#### Additional Parameters for the Default Block Variant

#### **Torque Transmission Model**

Model used to represent torque transmission. The default setting is Friction clutch approximation - Suitable for HIL and linearization.

# Friction clutch approximation - Suitable for HIL and linearization

#### Maximum transmitted torque

Maximum expected torque across the clutch. The default value is 1000 N\*m.

### Dynamic with Backlash

#### Number of teeth

Number of teeth in the clutch. The parameter must be greater than or equal to one. The default value is 6.

#### Rotational backlash

Angular play of the ring with respect to the hub. Greater backlash values correspond to wider tooth gaps that makes engagement easier. The parameter must be greater than zero. The default value is 10 deg.

#### Torsional stiffness

Stiffness of the tooth contact. The model assumes deformation due to tooth interaction is elastic. The angular deformation at the contact surface is proportional to the applied torque and the reciprocal of the contact stiffness. The parameter must be greater than zero. The default value is 1e+7 N\*m/rad.

### Torsional damping

Damping at the tooth contact surface. The value of the parameter is inversely proportional to the number of oscillations following impact. The parameter must be greater than zero. The default value is  $100 \, N*m/(rad/s)$ .

#### Tooth-tooth friction coefficient

Friction coefficient for the translational relative motion between the hub and ring teeth. The value of the parameter depends on the tooth material, lubrication, and quality of contacting surfaces. The parameter must be greater than zero. The default value is 0.05.

#### Additional Parameters for the Thermal Block Variant

### Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Maximum transmitted torque vector

Largest torque that the clutch can transmit, corresponding to a nonslip engaged configuration, specified as a vector. If the torque transmitted between the ring and the hub exceeds this value, the two components begin to slip with respect to each other. This torque determines the static friction limit in the friction clutch approximation. The vector has the same number of elements as the temperature vector. The default value is [1000.0, 1050.0, 1000.0] N\*m.

### Interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this option, the default, to get the best performance. This
  method is the default.
- Smooth Select this option to produce a continuous curve with continuous firstorder derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### **Extrapolation method**

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default option, to produce a curve with continuous firstorder derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

# **Cone Clutch**

Common parameters for the cone clutch are:

#### Contact surface maximum diameter

Outer diameter of the friction material linen that lines the cone clutch disks. The parameter must be greater than zero. The default value is  $150\,$  mm.

#### Contact surface minimum diameter

Inner diameter of the friction material linen that lines the cone clutch disks. The parameter must be greater than zero but smaller than the value of **Contact surface maximum diameter**.

### Cone half angle

Half angle of the clutch cone. The parameter must be greater than zero and less than or equal to 90 degrees. The default value is 12 deg.

### Velocity tolerance

Relative velocity below which the two surfaces can lock. The surfaces lock if the torque across the B and F rotational ports is less than the product of the effective radius, the static friction coefficient, and the applied normal force. The default value is 0.001 rad/s.

#### Threshold force

The normal force applied to the physical signal port N is applied to the contact only if the amount of force exceeds the value of the **Threshold force** parameter. Forces below the **Threshold force** are not applied, and there is consequently no transmitted frictional torque. The default value is 1 N.

#### Friction model

Select a parameterization method to model the kinetic friction coefficient. The options and default values for this parameter depend on the variant that you select for the block. The options are:

- Fixed kinetic friction coefficient Provide a fixed value for the kinetic friction coefficient. This option:
  - Is visible only if you use the default variant of the block
  - Is the default method for parameterizing the default variant of the block
  - Affects the visibility of other parameters

#### Fixed kinetic friction coefficient

#### **Kinetic friction coefficient**

The kinetic, or Coulomb, friction coefficient. The coefficient must be greater than zero. The default value is 0.3.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Table lookup kinetic friction coefficient Define the kinetic friction coefficient by one-dimensional table lookup based on the relative angular velocity between disks. This option:
  - Is visible only if you use the default variant of the block
  - Affects the visibility of other parameters

### Table lookup kinetic friction coefficient

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient vector

Specify the output values for the kinetic friction coefficient as a vector. All values must be positive. The default value is [0.3, 0.22, 0.19].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go
  above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Temperature-dependent kinetic friction coefficient Define the kinetic friction coefficient by table lookup based on the temperature. This option:
  - Is visible only if you use a thermal variant of the block
  - Is the default method for parameterizing the thermal variant of the block
  - Affects the visibility of other parameters

### Temperature-dependent kinetic friction coefficient

### Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

#### Kinetic friction coefficient vector

Specify the output values for kinetic friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. All values must be greater than zero. The default value is [0.3, 0.28, 0.25].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

- Temperature and speed-dependent kinetic friction coefficient —
  Define the kinetic friction coefficient by table lookup based on the temperature
  and the relative angular velocity between disks. This option:
  - Is visible only if you use the default variant of the block
  - Affects the visibility of other parameters

# Temperature and speed-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient matrix

Specify the output values for kinetic friction coefficient as a matrix. All the values must be greater than zero. The size of the matrix must equal the size of the matrix that is the result of the temperature vector  $\times$  the kinetic friction coefficient relative velocity vector. The default value is [0.34, 0.32, 0.3; 0.3, 0.28, 0.25; 0.25, 0.2, 0.15].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### **Detent**

#### Peak force

Peak shear force of the detent. The default value is 500 N.

#### Notch width

Width of the region where the detent exhibits shear force. The default value is 3 mm.

#### Viscous friction coefficient

Viscous friction coefficient at the contact surface of the detent. The parameter must be greater than or equal to zero. The default value is 0.1 N/(m/s).

### Friction to peak force ratio

Ratio of the kinetic friction to the peak shear force of the detent. The parameter is used to set the value of the kinetic friction. The parameter must be greater than or equal to zero. The default value is 0.01.

### Friction velocity threshold

Velocity required for peak kinetic friction at the contact surface of the detent. The parameter ensures the force is continuous when the travel direction changes, increasing the numerical stability of the simulation. The parameter must be greater than zero. The default value is  $0.05\,$  m/s.

# **Shift Linkages**

### Ring-hub clearance when dog clutch disengaged

Distance between ring and dog clutch hub with the ring fully retracted. The parameter specifies the maximum travel distance if engagement requirements are not met. The parameter must be greater than the value of **Ring-hub clearance when cone clutch disengaged**. The default value is 5 mm.

### Tooth overlap to engage

Minimum value of the tooth overlap beyond which the dog clutch is considered engaged. The parameter must be greater than zero. The default value is 3 mm.

### Tooth height

Height of dog clutch teeth. The parameter must be greater than zero. The default value is 10 mm.

#### Ring-hub clearance when cone clutch disengaged

Distance between the ring and cone clutch hub when the ring is fully retracted. The cone clutch can begin to engage once the slider has translated this distance. The ring can travel only this distance if the engagement requirements are not satisfied. The parameter must be greater than zero. The default value is 3 mm.

### Dog clutch ring stop stiffness

Stiffness of the hard stops on both sides of the dog clutch ring. The model assumes the ring and stops behave elastically. Contact deformation is proportional to the applied force and the reciprocal of the contact stiffness. The value of the stiffness must be assigned with reference to the parameter **Tooth overlap to engage**. Too low a stiffness could cause the deformation to exceed the required overlap and initiate a false engagement. The parameter must be greater than zero. The default value is 1e +6 N/m.

### Cone clutch ring stop stiffness

Stiffness of the hard stops on both sides of the cone clutch ring. The model assumes the ring and stops behave elastically. Contact deformation is proportional to the applied force and the reciprocal of the contact stiffness. The parameter must be greater than zero. The default value is 1e+6 N/m.

### Dog clutch ring stop damping

Translational contact damping between the dog clutch ring and the hub. The value of the damping is inversely proportional to the number of oscillations that occur after impact. The parameter must be greater than zero. The default value is 1e+3 N/(m/s).

# Cone clutch ring stop damping

Translational contact damping between the cone clutch ring and the hub. The value of damping is inversely proportional to the number of oscillations that occur after impact. The parameter must be greater than zero. The default value is 1e+3 N/(m/s).

#### Viscous friction coefficient

Viscous friction coefficient for the relative translational motion between the hub and the ring. The value of the parameter depends on lubrication state and quality of contacting surfaces. The coefficient must be greater than or equal to zero. The default value is  $100 \, \text{N/(m/s)}$ .

### **Initial Conditions**

#### **Initial state**

Beginning configuration of cone and dog clutches. Choices include:

- Cone clutch A and dog clutch A locked
- Cone clutch A locked
- All clutches unlocked
- Cone clutch B locked
- Cone clutch B and dog clutch B locked

The default setting is All clutches unlocked.

### Dog clutch initial shift linkage position

Initial position of the shift linkage section that attaches to the dog clutch. The value of the parameter has the following restrictions:

Dog Clutch State	Parameter Restriction
Dog clutch A Initially engaged	Negative of the parameter value must be greater than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage
Dog clutch A Initially disengaged	Negative of the parameter value must be smaller than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage
Dog clutch B Initially engaged	Parameter value must be greater than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage

Dog Clutch State	Parameter Restriction
Dog clutch B Initially disengaged	Parameter value must be smaller than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage

The default value is 0 mm.

### Cone clutch initial shift linkage position

Initial position of the shift linkage section that attaches to the cone clutch. The value of the parameter has the following restrictions:

Dog Clutch State	Parameter Restriction
Cone clutch A initially engaged	Negative of parameter must be greater than the value of <b>Ring-hub clearance</b> when cone clutch disengaged
Cone clutch A initially disengaged	Negative of parameter must be smaller than the value of <b>Ring-hub clearance</b> when cone clutch disengaged
Cone clutch B initially engaged	Parameter must be greater than the value of Ring-hub clearance when cone clutch disengaged
Cone clutch B initially disengaged	Parameter must be smaller than the value of Ring-hub clearance when cone clutch disengaged

The default value is 0 mm.

# Initial dog clutch ring-hub A offset angle

Initial angle between the ring and hub A portions of dog clutch. If the clutch is disengaged, the initial angle must lie in the range  $-\pi/N \le \theta \le +\pi/N$ , where N denotes the number of teeth in the dog clutch. If the clutch is engaged, the initial angle must be in the range  $-\delta/2 \le \theta \le +\delta/2$ , where  $\delta$  is the backlash angle. The default value is  $\theta$  deg.

This parameter is only visible if you select a block variant that does not include a thermal port and set **Dog Clutch** > **Torque transmission model** to Dynamic with backlash.

#### Initial dog clutch ring-hub B offset angle

Initial angle between the ring and hub B portions of the dog clutch. If the clutch is disengaged, the initial angle must lie in the range  $-\pi/N \le \theta \le +\pi/N$ , where N denotes the number of teeth in the dog clutch. If the clutch is engaged, the initial angle must be in the range  $-\delta/2 \le \theta \le +\delta/2$ , where  $\delta$  is the backlash angle. The default value is  $\theta$  deg.

This parameter is only visible if you select a block variant that does not include a thermal port and set **Dog Clutch** > **Torque transmission model** to Dynamic with backlash.

### **Thermal Port**

These thermal parameters are only visible when you select a block variant that includes a thermal port.

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 100 kJ/K.

### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

### Linearization

To optimize your model for linearization, use the **Dog Clutch > Torque transmission model** parameter default setting, Friction clutch approximation - Suitable for HIL and linearization.

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Dog Clutch > Torque transmission model** parameter default setting, Friction clutch approximation - Suitable for HIL and linearization.

# See Also

#### **Simscape Blocks**

Cone Clutch | Dog Clutch | Synchronizer | Translational Detent

# **Topics**

"Model Thermal Losses in Driveline Components"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# Flexible Shaft

Driveline shaft with torsional compliance

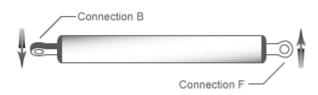


# Library

Couplings & Drives

# **Description**

This block represents a driveline shaft with torsional compliance. The shaft consists of a flexible material that twists in response to an applied torque. The twisting action delays power transmission between the shaft ends, altering the dynamic response of the driveline system. The shaft twists but does not bend.



To represent the flexible shaft, the block uses a lumped-parameter model. This model divides the shaft into different elements that interconnect through parallel spring-damper systems. The elements provide the shaft inertia while the spring-damper systems provide the shaft compliance.

You specify the shaft inertia, compliance, and number of shaft elements directly in the block dialog box. Choosing from two parameterizations, you can specify the shaft compliance using stiffness and damping values or, alternatively, the shaft shear modulus.

An additional parameter enables you to model the power losses due to viscous friction at the shaft ends.

# **Parameters**

### **Shaft**

#### **Parameterization**

Select how to characterize the flexible shaft. The default is By stiffness and inertia.

 By stiffness and inertia — Specify shaft characteristics by its inertia and elastic stiffness.

#### Stiffness and Inertia

#### **Stiffness**

Stiffness k of the shaft, the torque per unit angular deflection of the shaft. The default is 2e+5.

From the drop-down list, choose units. The default is newton-meters/radian (N\*m/rad).

#### Inertia

Rotational inertia J of the shaft around its principal axis. The default is 0.02.

From the drop-down list, choose units. The default is kilogram-meters<sup>2</sup> ( $kg-m^2$ ).

• By material properties — Specify shaft characteristics by its size and continuum properties. If you select this option, the panel changes from its default.

### **Shaft Geometry**

Select the geometry of the shaft. The default is Solid.

Solid — Specify a solid shaft geometry.

#### Solid

#### Shaft outside diameter

Diameter D of the solid shaft. Must be greater than 0. The default is 0.075.

From the drop-down list, choose units. The default is meters (m).

Annular— Specify an annular, or hollow, shaft geometry. If you select this option, the panel changes from its default.

#### **Annular**

#### Shaft outside diameter

Outside diameter D of the hollow shaft. Must be greater than 0. The default is 0.075.

From the drop-down list, choose units. The default is meters (m).

#### Shaft inside diameter

Inside diameter d of the hollow shaft. Must be greater than 0. The default is 0.05.

From the drop-down list, choose units. The default is meters (m).

#### Shaft length

Length *L* of the shaft. Must be greater than 0. The default is 1.

From the drop-down list, choose units. The default is meters (m).

# **Material density**

Mass density  $\rho$  of the shaft material. Must be greater than 0. The default is 7.8e+3.

From the drop-down list, choose units. The default is kilograms/meter $^3$  (kg/m $^3$ ).

#### Shear modulus

Shear modulus G of the shaft material. Must be greater than 0. The default is 7.93e+10.

From the drop-down list, choose units. The default is pascals (Pa).

### Damping ratio from internal losses

Damping ratio c for the first flexible torsional mode. The default value is 0.01.

# **Number of segments**

Number Nof rigid segments into which the shaft is divided. The default is 1.

# **Viscous Bearing Losses**

#### Viscous friction coefficients at base and follower

Viscous friction coefficients applied at the base and follower, respectively. The default is  $[0 \ 0]$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

#### **Initial Conditions**

### Initial shaft angular deflection

Initial torsional angular deflection of the shaft. The default is 0.

From the drop-down list, choose units. The default is radians (rad).

A positive initial deflection results in a positive torque action from the base (B) to the follower (F) port.

### Initial shaft angular velocity

Initial torsional angular velocity of the shaft. The default is 0.

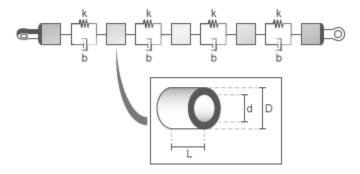
From the drop-down list, choose units. The default is revolutions/minute (rpm).

At the start of simulation, the entire shaft rotates collectively at this angular velocity, with no relative motion between the segments.

# Flexible Shaft Model

The Flexible Shaft block approximates the distributed, continuous properties of a shaft by a lumped parameter model. The model contains a finite number, N, of lumped inertiadamped spring elements in series, plus a final inertia. The result is a series of N+1 inertias connected by N rotational springs and N rotational dampers. The block can also include viscous friction at the shaft ends (base and follower ports) to represent bearing losses at these points. Do not confuse this viscous friction at the shaft ends with the internal material damping which corresponds to losses arising in the shaft material itself.

The Flexible Shaft block model is parameterized in either the shaft stiffness k and inertia J or its dimensions and material properties.



# **Shaft Characterized by Dimensions and Material Properties**

The shaft stiffness and inertia are computed from the shaft dimensions and material properties by the following relationships:

$$\begin{split} J_{\rm P} &= (\pi/32)(D^4 - d^4) \;, \\ m &= (\pi/4)(D^2 - d^2)\rho L \;, \\ J &= (m/8)(D^2 + d^2) = \rho L \cdot J_{\rm P} \;, \\ k &= J_{\rm P} \cdot G/L \;, \end{split}$$

#### where:

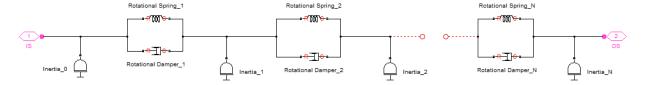
$J_{ m P}$	Polar moment of inertia		
D	Shaft outside diameter		
d	d Shaft inside	For solid shafts:	d = 0
diameter	For annular (hollow) shafts:	d> 0	
L	Shaft length		
m	Shaft mass		
J	Moment of inertia		
ρ	Shaft material density		
G	Shear modulus of elasticity		
k	Shaft rotational stiffness		

# **Internal Material Damping**

For either shaft parameterization, the internal material damping is defined by the damping ratio, c, for a single-segment model. In this case, the damping torque is  $2ck/\omega_N$ . The undamped natural frequency,  $\omega_N = \sqrt{(2k/J)}$ . The damping applied across an individual segment of a segmented model is equal to the product of the damping coefficient and the relative rotational velocity of that segment.

# **Equivalent Physical Network**

The following figure shows an equivalent physical network constructed from Simscape blocks only. There are *N* segments, each consisting of a spring, damper, and inertia. A segment represents a short section of the driveshaft, the spring representing torsional compliance, and the damper representing material damping. The total shaft inertia is split into N+1 parts, and partitioned as shown in the figure.



# **Limitations**

The distributed parameter model of a continuous torsional shaft is approximated by a finite number, N, of lumped parameters.

The flexible shaft is assumed to have a constant cross-section along its length.

# **Tradeoff Between Accuracy and Speed**

A larger number N of segments increases the accuracy of the model, but reduces its speed. The single-segmented model (N=1) exhibits an eigenfrequency which is close to the first eigenfrequency of the continuous, distributed parameter model.

For greater accuracy, you can select 2, 4, 8, or more segments. For example, the four lowest eigenfrequencies are represented with an accuracy of 0.1, 1.9, 1.6, and 5.3 percent, respectively, by a 16-segmented model.

# **Ports and Conventions**

B and F are rotational conserving ports associated with the shaft input and output sections, respectively.

# References

- [1] Bathe, K.-J., Finite Element Procedures, Prentice Hall, Inc, 1996.
- [2] Chudnovsky, V., D. Kennedy, A. Mukherjee, and J. Wendlandt, "Modeling Flexible Bodies in SimMechanics and Simulink," *MATLAB Digest* 14(3), May 2006.

# See Also

Inertia | Rotational Damper | Rotational Spring | Torsional Spring-Damper

# **Force Noise Source**

Model zero-mean normally (Gaussian) distributed force **Library:** Sources



# **Description**

The Force Noise Source block generates zero-mean normally (Gaussian) distributed force using the Random Number source in the Simscape Foundation library. The force produced by the block depends on two factors:

- The noise power spectral density input to the block
- A random number seed that you control using the Repeatability and, as applicable,
   Seed parameters

The defining equation for the force that the block generates is

$$F = \sqrt{PSD/2} \frac{N(0,1)}{\sqrt{h}},$$

#### where:

- *F* is the output force.
- *PSD* is the single-sided noise power spectral density.
- N is a Gaussian random number with zero mean and standard deviation of one.
- h is the sampling interval.

## **Ports**

## Input

## P — Single-sided noise power spectral density

physical signal

The power spectral density (PSD) of noise is the average noise power per unit of bandwidth, in  $N^2/Hz$ .

# Conserving

#### **B** — Base interface

mechanical translational

Mechanical translational conserving port associated with the base interface.

#### F - Follower interface

mechanical translational

Mechanical translational conserving port associated with the follower interface.

## **Parameters**

## Sample time — Time step period and offset

le-3 s (default) | [step, offset] s

The values of the time step period and the initial time offset. If you specify a scalar value for step, the block assumes an offset value of 0. To specify a nonzero value for the initial time offset, specify the parameter values using the vector [step, offset]. The offset value must be less than the step value and greater than or equal to zero.

## Repeatability — Random number seed control

Not repeatable (default) | Repeatable | Specify seed

The random number seed is the number that initializes the random number generator. The seed is  $\theta$  or a positive integer. To control the random number seed, set this parameter to:

• Not repeatable — The seed changes every time you simulate your model. The block resets the random seed using the MATLAB random number generator command:

```
seed = randi(2^32-1);
```

Repeatable — The seed is the same random number at the start of every simulation.
 The block sets the value using the same MATLAB random number generator command used by the Not repeatable parameter.

When you add a Force Noise Source block to your model from the Sources library, the block generates and stores a random value for the repeated seed. When you make a copy of the Force Noise Source block from an existing block in a model, the copy generates a new random value for the repeated seed.

Specify seed — The seed is a number that you specify using the Seed parameter.
 The Seed parameter is only available when you choose Specify seed for the Repeatability parameter.

## Seed — Random number generation seed value

0 (default)

The seed must be 0 or a positive integer. This parameter is only available when you select Specify seed for the **Repeatability** parameter.

# See Also

## **Simscape Blocks**

Random Number | Rotational Velocity Noise Source | Sinusoidal Force Source | Torque Noise Source | Translational Velocity Noise Source

#### **Functions**

randi

#### Introduced in R2016b

# **Fundamental Friction Clutch**

Friction clutch with kinetic and static-limit friction torques as inputs

Library: Simscape / Driveline / Clutches / Fundamental

Components



# **Description**

This block represents a friction clutch, a mechanism that transmits rotational power through friction. The clutch contains two friction plate sets, each rigidly connected to a driveshaft, that come into contact to engage. Once in contact, the plates experience frictional torques that enable power to flow between the driveshafts.

The clutch can be bidirectional or unidirectional. A bidirectional clutch can slip in the positive and negative directions. A unidirectional clutch can slip only in the positive direction. The slip direction is positive if the follower shaft spins faster than the base shaft and negative if it spins slower. The block defines the slip velocity as the difference

$$\omega = \omega_{\rm F} - \omega_{\rm B}$$
,

where:

- ω is the slip velocity.
- $\omega_{\text{F}}$  is the angular velocity of the follower driveshaft.
- $\omega_B$  is the angular velocity of the base driveshaft.

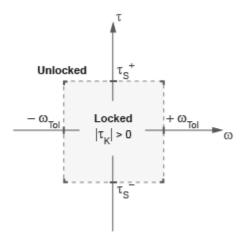
## **Clutch States**

The clutch can be in three states:

• Locked — Real clutch state in which the friction plates spin as a unit. A locked clutch has one rotational degree of freedom. It experiences no power losses due to friction.

- Unlocked Real clutch state in which the friction plates slip with respect to each
  other. An unlocked clutch has two rotational degrees of freedom. It experiences power
  losses equal to the product of the slip velocity and the kinetic friction torque.
- Wait Virtual clutch state that maintains the motion of the previous state while testing for locking and unlocking. The clutch degrees of freedom and power losses depend on the previous clutch state.

The schematic shows the conditions under which the clutch is locked and unlocked. The clutch is generally locked if the torque it transfers lies between its static friction torque limits and the magnitude of the slip velocity is smaller than its velocity tolerance. The clutch unlocked otherwise.



In the schematic:

- $\tau$  is the torque transferred between the clutch plates.
- $\tau_{\text{S}}^{\text{-}}$  and  $\tau_{\text{S}}^{\text{+}}$  are the static friction torque limits.
- $\tau_K$  is the kinetic friction torque between the clutch plates.
- $\omega_{\text{Tol}}$  is the slip velocity tolerance of the clutch.
- $\omega$  is the slip velocity between the clutch plates.

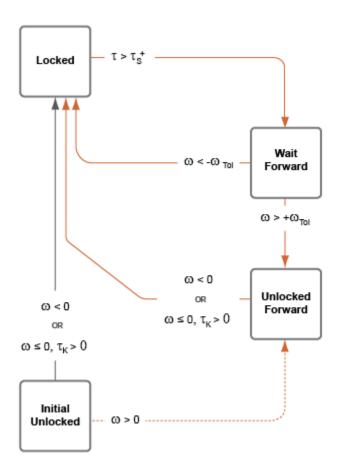
The block identifies the clutch state through physical signal port M using values -1, 0, and +1. The table summarizes the correspondence between the states and the output values.

State	Value
Unlocked Forward or Wait Forward	+1
Unlocked Reverse or Wait Reverse	-1
Locked or Unlocked Initial State	0

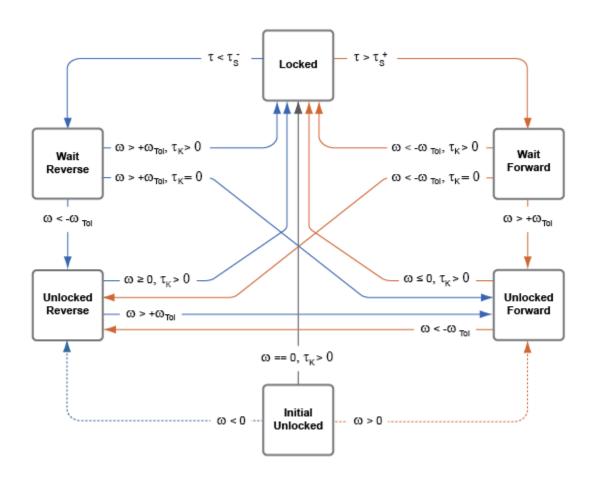
## **State Transitions**

At the start of simulation, the clutch is in one of two states—locked or initial unlocked. The initial unlocked state is unique in that it lacks a direction of motion. The clutch remains in this state until the clutch slip velocity becomes nonzero. The clutch then transitions to the appropriate state—unlocked reverse or unlocked forward—according to the schematic.

During simulation, the clutch tests various dynamic conditions to determine the appropriate state transitions, if any. The schematics show the possible transitions, their dynamic conditions, and the resulting states. If the clutch is unidirectional, the schematic reduces to the right half. The diagram shows transitions for a one-way clutch.



The diagram shows transitions for a two-way clutch.



## **Thermal Model**

You can model the effects of heat flow and temperature change by selecting a thermal block variant. Selecting a thermal variant:

- Exposes port  $\boldsymbol{H}\text{, a conserving port in the thermal domain.}$
- Enables the **Thermal mass** parameter which allows you to specify the ability of the component to resist changes in temperature.

• Enables the **Temperature** variable which allows you to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

To select a thermal variant, right-click the block in your model and from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port.

## **Ports**

## Input

## tK — Kinetic friction torque, N\*m

physical signal

Physical signal input port for the kinetic friction torque.

#### t+ - Kinetic friction torque upper bound, N\*m

physical signal

Physical signal input port for the upper static friction torque limit.

## t- - Static friction torque lower bound, N\*m

physical signal

Physical signal input port for the lower static friction torque limit.

## **Output**

## S — Clutch slip velocity, rad/sec

physical signal

Physical signal output port for the clutch slip velocity.

#### M — Clutch state

physical signal

Physical signal output port for the clutch state.

## Conserving

#### **B** — Rotational velocity, rad/sec

mechanical rotational

Rotational conserving ports associated with the driving shaft.

### F — Rotational speed, rad/sec

mechanical rotational

Rotational conserving ports associated with the driven shaft

#### H — Heat flow, W

thermal

The thermal conserving port is optional and is hidden by default.

#### **Dependencies**

To expose the port, select a thermal block variant.

## **Parameters**

## Directionality — Permissible inter-plate slip directions

Bidirectional (default) | Unidirectional

Slip directions the clutch allows between its plates. A bidirectional clutch allows positive and negative slip velocities. A unidirectional clutch allows only positive slip velocities.

The unidirectional clutch is equivalent to a friction clutch connected in parallel to a one-way clutch that disengages only when the slip velocity becomes positive. To model a unidirectional clutch with slip in the negative direction, reverse the base and follower port connections.

## Clutch velocity tolerance — Slip velocity threshold

0.001 rad/s (default)

Slip velocity below which the clutch can lock. The clutch locks if, after falling below the clutch velocity tolerance, the kinetic friction torque is nonzero and the transferred torque is between the static friction torque limits.

#### Initial state — Initial clutch state

Unlocked (default) | Locked

Clutch state at the start of simulation. The clutch can be in one of two states, locked and unlocked. A locked clutch constrains the base and follower shafts to spin at the same velocity, that is, as a single unit. An unlocked clutch allows the two shafts to spin at different velocities, resulting in slip between the clutch plates.

A clutch that starts simulation unlocked lacks a direction of motion. For this reason, after checking that the unlocked state is valid, the block automatically determines the appropriate direction of motion based on the driveline dynamics. Based on the direction of motion, the clutch then transitions to an unlocked-reverse or unlocked-forward state.

## Thermal mass — Resistance to temperature change

25 kJ/K (default)

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change.

#### **Dependencies**

Selecting a thermal block variant enables this parameter.

# **See Also**

Differential | Disk Friction Clutch | Torque Converter | Variable Ratio Transmission

## **Topics**

"Gear Coupling Control Using Clutches"

#### Introduced in R2011a

# **Generic Engine**

Internal combustion engine with throttle and rotational inertia and time lag

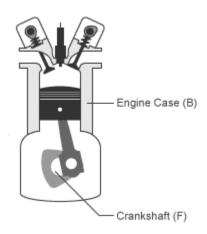


# Library

Simscape / Driveline / Engines

# **Description**

The block represents a general internal combustion engine. Engine types include sparkignition and diesel. Speed-power and speed-torque parameterizations are provided. A throttle physical signal input specifies the normalized engine torque. Optional dynamic parameters include crankshaft inertia and response time lag. A physical signal port outputs engine fuel consumption rate based on choice of fuel consumption model. Optional speed and redline controllers prevent engine stall and enable cruise control.



# **Generic Engine Model**

By default, the Generic Engine model uses a programmed relationship between torque and speed, modulated by the throttle signal.

# **Engine Speed, Throttle, Power, and Torque**

The engine model is specified by an *engine power demand* function  $g(\Omega)$ . The function provides the maximum power available for a given engine speed  $\Omega$ . The block parameters (maximum power, speed at maximum power, and maximum speed) normalize this function to physical maximum torque and speed values.

The normalized throttle input signal T specifies the actual engine power. The power is delivered as a fraction of the maximum power possible in a steady state at a fixed engine speed. It modulates the actual power delivered, P, from the engine:  $P(\Omega,T) = T \cdot g(\Omega)$ . The engine torque is  $\tau = P/\Omega$ .

# **Engine Power Demand**

The engine power is nonzero when the speed is limited to the operating range,  $\Omega_{\min} \leq \Omega \leq \Omega_{\max}$ . The absolute maximum engine power  $P_{\max}$  defines  $\Omega_0$  such that  $P_{\max} = g(\Omega_0)$ . Define  $w \equiv \Omega/\Omega_0$  and  $g(\Omega) \equiv P_{\max} p(w)$ . Then p(1) = 1 and dp(1)/dw = 0. The torque function is:

$$\tau = (P_{\text{max}}/\Omega_0) \cdot [p(w)/w].$$

You can derive forms for p(w) from engine data and models. Generic Engine uses a third-order polynomial form:

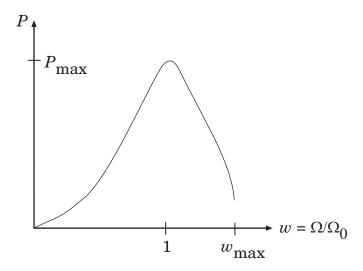
$$p(w) = p_1 \cdot w + p_2 \cdot w^2 - p_3 \cdot w^3$$

satisfying

$$p_1 + p_2 - p_3 = 1$$
,  $p_1 + 2p_2 - 3p_3 = 0$ .

In typical engines, the  $p_i$  are positive. This polynomial has three zeros, one at w = 0, and a conjugate pair. One of the pair is positive and physical; the other is negative and unphysical:

$$w_{\pm} = \frac{1}{2} \left( -p_2 \pm \sqrt{p_2^2 + 4p_1 p_3} \right)$$



#### **Typical Engine Power Demand Function**

- For the engine power polynomial, there are restrictions, as shown, on the polynomial coefficients  $p_i$ , to achieve a valid power-speed curve.
- If you use tabulated power or torque data, corresponding restrictions on  $P(\Omega)$  remain.

Specify the speed and power as  $w=\Omega/\Omega_0$  and  $p=P(\Omega)/P_0$  and define the boundaries as  $w_{\min}=\Omega_{\min}/\Omega_0$  and  $w_{\max}=\Omega_{\max}/\Omega_0$ . Then:

- The engine speed is restricted to a positive range above the minimum speed and below the maximum speed:  $0 \le w_{\min} \le w \le w_{\max}$ .
- The engine power at minimum speed must be nonnegative:  $p(w_{\min}) \ge 0$ . If you use the polynomial form, this condition is a restriction on the  $p_i$ :

$$p(w_{\min}) = p_1 \cdot w_{\min} + p_2 \cdot w_{\min}^2 - p_3 \cdot w_{\min}^3 \ge 0.$$

• The engine power at maximum speed must be nonnegative:  $p(w_{\text{max}}) \ge 0$ . If you use the polynomial form, this condition is a restriction on  $w_{\text{max}}$ :  $w_{\text{max}} \le w_{+}$ .

# **Engine Power Forms for Different Engine Types**

For the default parameterization, Generic Engine provides two choices of internal combustion engine types, each with different engine power demand parameters.

Power Demand	Engine Type:	
Coefficient	Spark-Ignition	Diesel
$p_1$	1	0.6526
$p_2$	1	1.6948
$p_3$	1	1.3474

# **Idle Speed Controller Model**

The idle speed controller adjusts the throttle signal to increase engine rotation below a reference speed according to the following expressions:

$$\Pi = \max(\Pi_i, \Pi_c)$$

and

$$\frac{d(\Pi_c)}{dt} = \frac{0.5 \cdot \left(1 - \tanh\left(4 \cdot \frac{\omega - \omega_r}{\omega_t}\right)\right) - \Pi_c}{\tau}$$

where:

- $\Pi$  Engine throttle
- $\Pi_i$  Input throttle (port T)
- $\Pi_c$  Controller throttle
- $\omega$  Engine speed
- $\omega_r$  Idle speed reference
- $\omega_t$  Controller speed threshold
- $\tau$  Controller time constant

The controlled throttle increases with a first-order lag from zero to one when engine speed falls below the reference speed. When the engine speed rises above the reference speed, the controlled throttle decreases from one to zero. When the difference between engine velocity and reference speed is smaller than the controller speed threshold, the *tanh* function smooths the time derivative of the controlled throttle. The controlled throttle is limited to the range 0-1. The engine uses the larger of the input and controlled

throttle values. If engine time lag is included, the controller changes the input *before* the lag is computed.

## **Redline Controller Model**

While the idle speed controller determines the minimum throttle value for maintaining engine speed, the redline controller prevents excessive speed based on a maximum throttle input. To determine the maximum throttle value, the redline controller uses the idle speed controller model equation. However, for the redline controller:

- $\omega_r$  is the redline speed reference.
- $\omega_t$  is the redline speed threshold.
- *τ* is the redline time constant.

## **Performance**

To increase simulation speed, use the default option, No fuel consumption, for the **Fuel consumption model** parameter.

If you select any other option for the **Fuel consumption model**, the block solves a nonlinear equation that is required for calculating fuel consumption. The block solves the equation even if the **FC** port, which reports the fuel consumption rate, is not connected to another block.

When the parameter is set to No fuel consumption, the block does not calculate fuel consumption, even if the FC port is connected to another block.

# Limitations

This block contains an engine time lag limitation.

# **Engine Time Lag**

Engines lag in their response to changing speed and throttle. The Generic Engine block optionally supports lag due to a changing throttle only. Time lag simulation increases model fidelity but reduces simulation performance.

## **Ports**

Port	Description
В	Rotational conserving port representing the engine block
F	Rotational Conserving port representing the engine crankshaft
T	Physical signal input port specifying the normalized engine throttle level
P	Physical signal output port reporting the instantaneous engine power
FC	Physical signal output port reporting the fuel consumption rate

Port T accepts a signal with values in the range 0-1. The signal specifies the engine torque as a fraction of the maximum torque possible in steady state at fixed engine speed. The signal saturates at zero and one. Values below zero are interpreted as zero. Values above one are interpreted as one.

Port **FC** does not output data when the **Fuel consumption model** parameter is set to **No** fuel consumption.

# **Parameters**

## **Engine Torque**

## Model parameterization

Select how to model the engine. Choose between these options, each of which enable other parameters:

- Normalized 3rd-order polynomial matched to peak power Parametrize the engine with a power function controlled by power and speed characteristics. This is the default option.
- Tabulated torque data Engine is parametrized by speed-torque table that you specify.
- Tabulated power data Engine is parametrized by speed-power table that you specify.

## **Engine type**

Choose type of internal combustion engine. Choose between Spark-ignition, the default option, and Diesel. Selecting Normalized 3rd-order polynomial

matched to peak power for the **Model parameterization** parameter enables this parameter.

#### Maximum power

Maximum power  $P_{\rm max}$  that the engine can output. The default is 150 kW. Selecting Normalized 3rd-order polynomial matched to peak power for the **Model parameterization** parameter enables this parameter.

### Speed at maximum power

Engine speed  $\Omega_0$  at which the engine is running at maximum power. The default is 4500 rpm. Selecting Normalized 3rd-order polynomial matched to peak power for the **Model parameterization** parameter enables this parameter.

#### Maximum speed

Maximum speed  $\Omega_{max}$  at which the engine can generate torque. The default is 6000 rpm. Selecting Normalized 3rd-order polynomial matched to peak power for the **Model parameterization** parameter enables this parameter.

During simulation, if  $\Omega$  exceeds this maximum, the simulation stops with an error. The engine maximum speed  $\Omega_{max}$  cannot exceed the engine speed at which the engine power becomes negative.

## Stall speed

Minimum speed  $\Omega_{min}$  at which the engine can generate torque. The default is 500 rpm. Selecting Normalized 3rd-order polynomial matched to peak power for the **Model parameterization** parameter enables this parameter.

During simulation, if  $\Omega$  falls below this minimum, the engine torque is blended to zero.

## **Speed vector**

Vector of values of the engine function's independent variable, the speed  $\Omega$ . The default is [500, 1000, 2000, 3000, 4000, 5000, 6000, 7000] rpm. Selecting Tabulated torque data or Tabulated power data for the **Model parameterization** parameter enables this parameter.

The first and last speeds in the vector are interpreted as the stall speed and the maximum speed, respectively. If the speed falls below the stall speed, engine torque is blended to zero. If the speed exceeds the maximum speed, the simulation stops with an error.

### **Torque vector**

Vector of values of the engine function's dependent variable, the torque  $\tau$ . The default is [380, 380, 380, 380, 350, 280, 200, 80] N\*m. Selecting Tabulated torque data for the **Model parameterization** parameter enables this parameter.

#### Power vector

Vector of values of the engine function's dependent variable, the power *P*. The default is [20, 40, 78, 120, 145, 148, 125, 60] kW. Selecting Tabulated power data for the **Model parameterization** parameter enables this parameter.

### Interpolation method

Method to interpolate the engine speed-torque or speed-power function between discrete relative velocity values within the range of definition. Choose between Linear, the default choice, and Smooth. Selecting Tabulated torque data or Tabulated power data for the **Model parameterization** parameter enables this parameter.

# **Dynamics**

#### Inertia

Select how to model the rotational inertia of the engine block. Choose between these options, each of which enables other parameters:

- No inertia Engine crankshaft is modeled with no inertia. This option is the
  default.
- Specify inertia and initial velocity Engine crankshaft is modeled with rotational inertia and initial angular velocity.

## **Engine Inertia**

Rotational inertia of the engine crankshaft. The default is 1 kg\*m^2. Selecting Specify inertia and initial velocity for the **Inertia** parameter enables this parameter.

## **Initial velocity**

Initial angular velocity  $\Omega(0)$  of the engine crankshaft. The default is 800 rpm. Selecting Specify inertia and initial velocity for the **Inertia** parameter enables this parameter.

#### Time constant

Select how to model the time lag of the engine response. Choose between these options, each of which enables other options:

- No time constant Suitable for HIL simulation Engine reacts with no time lag. This option is the default.
- Specify engine time constant and initial throttle Engine reacts with a time lag.

#### **Engine time constant**

Engine time lag. The default is 0.2 s.

#### Initial normalized throttle

Initial normalized engine throttle T(0), ranging between zero and one. The default is 0.

#### Limits

### **Speed threshold**

Width of the speed range over which the engine torque is blended to zero as  $\Omega$  approaches the stall speed. The default is 100 rpm.

# **Fuel Consumption**

## Fuel consumption model

Select a model for calculating engine-fuel consumption. Model parameterizations are compatible with standard industrial data. Choose between these options, some of which enable other options:

- No fuel consumption The default option
- Constant per revolution
- Fuel consumption by speed and torque
- Brake specific fuel consumption by speed and torque
- Brake specific fuel consumption by speed and brake mean effective pressure

## No fuel consumption

The block does not calculate fuel consumption even when the **FC** port, which reports the fuel consumption rate, is connected to another block. Selecting this option increases simulation speed.

### Fuel consumption per revolution

Enter the volume of fuel consumed in one crankshaft revolution. The default is 25 mg/rev. Selecting Constant per revolution for the **Fuel consumption model** parameter enables this parameter.

#### **Displaced volume**

Enter the volume displaced by a piston stroke. The default is 400 cm<sup>3</sup>.

Selecting Brake specific fuel consumption by speed and brake mean effective pressure for the **Fuel consumption model** parameter enables this parameter.

## Revolutions per cycle

Enter the number of crankshaft revolutions in one combustion cycle — e.g. 2 for a four-stroke engine, or 1 for a two-stroke engine. The default is 2.

Selecting Brake specific fuel consumption by speed and brake mean effective pressure for the **Fuel consumption model** parameter enables this parameter.

### **Speed vector**

Enter vector of engine speeds used in lookup table parameterizations. Vector size must match **Torque vector size**. The default is [1000, 2000, 3000, 4000, 5000, 6000] rpm. Selecting Fuel consumption by speed and torque, Brake specific fuel consumption by speed and torque, or Brake specific fuel consumption by speed and brake mean effective pressure for the **Fuel consumption model** parameter enables this parameter.

#### **Torque vector**

Enter vector of engine torques used in the lookup table parameterizations. Vector size must match **Speed vector** size. The default is [0, 80, 160, 200, 240, 320, 360, 400] N\*m. Selecting Fuel consumption by speed and torque or Brake specific fuel consumption by speed and torque for the **Fuel** consumption model parameter enables this parameter.

### Fuel consumption table

Enter matrix with fuel consumption rates corresponding to engine speed and torque vectors. The number of rows must equal the number of elements in the **Speed vector**. The number of columns must equal the number of elements in the **Torque vector**. The default is [.5, .9, 1.4, 1.6, 1.9, 2.7, 3.4, 4.4; 1, 1.7, 2.7, 3.1, 3.6, 5, 6, 7.4; 1.4, 2.7, 4, 4.8, 5.6, 7.5, 8.5, 10.5;

2, 3.6, 5.8, 6.7, 8, 10.4, 11.7, 13.3; 2.5, 4.8, 7.9, 9.4, 10.8, 14, 16.2, 18.6; 3.1, 6, 10.3, 11.9, 13.8, 18.4, 22, 26.5] g/s.

Selecting Fuel consumption by speed and torque for the **Fuel consumption model** parameter enables this parameter.

#### Brake mean effective pressure vector

Enter vector of brake mean effective pressure (BMEP) values. The default is [0, 250, 500, 625, 750, 1000, 1150, 1250] kPa. The BMEP satisfies the expression:

$$BMEP = T \cdot \left(\frac{2\pi \cdot n_c}{V_d}\right)$$

where:

- *T* Output torque
- $n_c$  Number of cycles per revolution
- $V_d$  Cylinder displaced volume

Selecting Brake specific fuel consumption by speed and brake mean effective pressure for the **Fuel consumption model** parameter enables this parameter.

## Brake specific fuel consumption table

Selecting Brake specific fuel consumption by speed and torque or Brake specific fuel consumption by speed and brake mean effective pressure for the **Fuel consumption model** parameter enables this parameter.

For the Brake specific fuel consumption by speed and torque fuel model, enter the matrix with brake specific fuel consumption (BSFC) rates corresponding to engine speed and torque vectors. BSFC is the ratio of the fuel consumption rate to the output power. The number of rows must equal the number of elements in the **Speed vector**. The number of columns must equal the number of elements in the **Torque vector**.

For the Brake specific fuel consumption by speed and brake mean effective pressure fuel model, enter the matrix with brake specific fuel consumption (BSFC) rates corresponding to engine speed and brake mean effective pressure (BMEP) vectors. BSFC is the ratio of the fuel consumption rate to the output power. The number of rows must equal the number of elements in the **Speed vector**.

The number of columns must equal the number of elements in the **Brake mean effective pressure vector**.

```
For both fuel-consumption models, the default is [410, 380, 300, 280, 270, 290, 320, 380; 410, 370, 290, 270, 260, 270, 285, 320; 415, 380, 290, 275, 265, 270, 270, 300; 420, 390, 310, 290, 285, 280, 280, 285; 430, 410, 340, 320, 310, 300, 310, 320; 450, 430, 370, 340, 330, 330, 350, 380] g/hr/kW.
```

#### Interpolation method

Select the interpolation method used to calculate fuel consumption at intermediate speed-torque values. Methods are Linear and Smooth. Outside the data range, fuel consumption is held constant at the last value given in the lookup table. Selecting Fuel consumption by speed and torque, Brake specific fuel consumption by speed and torque, or Brake specific fuel consumption by speed and brake mean effective pressure for the **Fuel consumption model** parameter enables this parameter.

# **Speed Control**

## **Idle speed control**

Select speed control model. The options are:

- No idle speed controller Omit idle speed controller. Throttle input is used directly. This option is the default.
- Enable idle speed controller Include idle speed controller to prevent engine stalling. This option enables other parameters. For more information, see "Idle Speed Controller Model" on page 1-188.

## Idle speed reference

Enter the value of the speed reference below which speed increases, and above which speed decreases. The default is 1000 rpm.

Selecting Enable idle speed controller for the **Idle speed control** parameter enables this parameter.

#### **Controller time constant**

Enter the value of the time constant associated with an increase or decrease of the controlled throttle. The constant value must be positive. The default is 1 s.

Selecting Enable idle speed controller for the **Idle speed control** parameter enables this parameter.

### Controller threshold speed

Parameter used to smooth the controlled throttle value when the engine's rotational speed crosses the idle speed reference. For more information, see "Idle Speed Controller Model" on page 1-188. Large values decrease controller responsiveness. Small values increase computational cost. This parameter must be positive. The default is 1 rpm.

Selecting Enable idle speed controller for the **Idle speed control** parameter enables this parameter.

#### Redline control

Select redline control model. Options include No redline controller and Enable redline controller.

- No redline controller Omit redline controller. Throttle depends only on the idle speed controller. This option is the default.
- Enable redline controller Include redline controller to prevent excessive speed. This option enables other parameters.

## Redline speed

Enter the value of the speed reference above which the redline control activates. The default is 5000 rpm.

Selecting Enable redline controller for the **Redline control** parameter enables this parameter.

#### Redline time constant

Enter the value of the time constant associated with an increase or decrease of the controlled throttle. The constant value must be positive. The default is 1 s.

Selecting Enable redline controller for the **Redline control** parameter enables this parameter.

## Redline threshold speed

Specify the width of the region around the redline speed where the controller goes from fully enabled to not enabled. The block uses this parameter for smoothing the controlled throttle value when the engine's rotational speed crosses the redline speed reference. Large values decrease controller responsiveness. Small values increase computational cost. This parameter must be positive. The default is 1 rpm.

Selecting Enable redline controller for the **Redline control** parameter enables this parameter.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, set the **Dynamics** > **Time Constant** parameter to No time constant - Suitable for HIL simulation.

# See Also

## **Simscape Blocks**

Piston | Piston Engine

## **Topics**

"Complete Vehicle Model"

"Adjust Model Fidelity"

"Hydraulically-Actuated Driveline Clutch"

"Vehicle with Dual Clutch Transmission"

Vehicle with Four-Speed Transmission

"Vehicle with Four-Wheel Drive"

Vehicle with Manual Transmission

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

"Troubleshoot Engine Issues"

# **Harmonic Drive**

High-ratio speed reducer based on elastic deformation of an elliptical gear



# Library

Gears

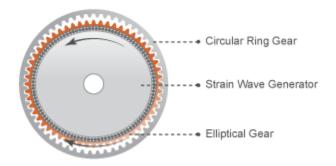
# **Description**

This block represents a compact, high-ratio, speed reduction mechanism that contains three key components:

- Strain wave generator
- Elliptical gear
- Circular ring gear

The strain wave generator comprises an elliptical plug mated to a raced ball bearing. It sits inside an elastic metal gear, deforming it into a slight elliptical pattern. Rotation of the elliptical pattern in the body of the gear constitutes a strain wave.

The elliptically deformed gear engages the internal teeth of a fixed circular ring gear of only slightly larger diameter. Meshing occurs concurrently at the two elongated ends of the elliptical gear. This design doubles the teeth in mesh, boosting the torque capacity of the drive system.



During normal operation, the base shaft drives the strain wave generator. The elliptical plug spins freely inside the elastic metal gear, propagating the strain wave about the gear rotation axis. This strain wave causes the elliptical gear teeth to engage the internal teeth of the circular ring gear progressively.

The internal meshing between the two gears causes the elliptical gear axis to spin counter to the elliptical strain wave. For every clockwise rotation that the strain wave generator completes, the elliptical gear axis rotates counterclockwise by a small amount.

Large reduction ratios arise from the near-equal gear tooth numbers. The effective gear reduction ratio is:

$$r = \frac{n_{\rm E}}{n_{\rm C} - n_{\rm E}},$$

#### where:

- *r* is the gear reduction ratio.
- $n_{\rm C}$  is the tooth number of the circular ring gear.
- $n_{\rm E}$  is the tooth number of the deformable elliptical gear.

Optional parameters account for power losses due to gear meshing and viscous friction. The Simple Gear block provides the foundation for this block. For more information, see Simple Gear.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Ports**

Port	Description
В	Conserving rotational port representing the base shaft
F	Conserving rotational port representing the follower shaft

# **Parameters**

#### Main

## Number of teeth on elliptical gear

Total number of teeth protruding outward from the elliptical gear perimeter. This number should be slightly smaller than the number of teeth on the circular ring gear. The ratio of the two gear tooth numbers defines the relative angular velocities of the base and follower shafts. The default value is 100.

## Number of teeth on circular gear

Number of teeth protruding inward from the circular ring gear perimeter. This number should be slightly larger than the number of teeth on the elliptical gear. The ratio of the two gear tooth numbers defines the relative angular velocities of the base and follower shafts. The default value is 102.

# **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

List of friction models at various precision levels for estimating power losses due to meshing.

- No meshing losses Suitable for HIL simulation Neglect friction between gear cogs. Meshing is ideal.
- Constant efficiency Reduce torque transfer by a constant efficiency factor. This factor falls in the range  $0 < \eta \le 1$  and is independent of load. Selecting this option exposes additional parameters.

## Constant efficiency

### **Efficiency**

Torque transfer efficiency  $(\eta)$  between base and follower shafts. This parameter is inversely proportional to the meshing power losses. Values can range from 0 to 1. The default value is 0.95.

### Follower power threshold

Absolute value of the follower shaft power above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor from zero when at rest to the full efficiency value at the power threshold.

As a guideline, the power threshold should be lower than the expected power transmitted during simulation. Higher values might cause the block to underestimate efficiency losses. Very low values might, however, raise the computational cost of simulation. The default value is 0.001 W.

• Load-dependent efficiency — Reduce torque transfer by a variable efficiency factor. This factor falls in the range  $0 < \eta < 1$  and varies with the torque load. Selecting this option exposes additional parameters.

## **Load-Dependent Efficiency**

## Input shaft torque at no load

Net torque  $(\tau_{idle})$  acting on the input shaft in idle mode, e.g., when torque transfer to the output shaft equals zero. For nonzero values, the power input in idle mode completely dissipates due to meshing losses. The default value is  $0.1~\mathrm{N*m}$ .

#### Nominal output torque

Output torque ( $\tau_F$ ) at which to normalize the load-dependent efficiency. The default value is 5 N\*m.

#### Efficiency at nominal output torque

Torque transfer efficiency ( $\eta$ ) at the nominal output torque. Efficiency values must fall in the interval [0, 1]. Larger efficiency values correspond to greater torque transfer between the input and output shafts. The default value is 0.95.

### Follower angular velocity threshold

Absolute value of the follower shaft angular velocity above which the full efficiency factor is in effect ( $\omega_{\rm F}$ ). Below this value, a hyperbolic tangent function smooths the efficiency factor to one, lowering the efficiency losses to zero when at rest.

As a guideline, the angular velocity threshold should be lower than the expected angular velocity during simulation. Higher values might cause the block to underestimate efficiency losses. Very low values might, however, raise the computational cost of simulation.

The default value is 0.01 rad/s.

#### With Thermal Port

#### Friction model

Choice of model for representing friction. The model can incorporate the temperature and load dependences of friction or just the temperature dependence. The default setting is Temperature-dependent efficiency.

## **Temperature**

Array of temperatures used to construct an efficiency lookup table. The array values must increase from left to right. The temperature array must be the same size as the efficiency array in temperature-dependent models. It must be the same size as a single row of the efficiency matrix in temperature-and-load-dependent models. The default array is [280 300 320] K.

## Load at elliptical gear

Array of elliptical-gear loads used to construct a 2-D temperature-load-efficiency lookup table for temperature-and-load-dependent efficiency models. The array values must increase from left to right. The load array must be the same size as a single column of the efficiency matrix. The default array is [1 5 10] N\*m.

## **Efficiency**

Array of efficiencies used to construct a 1-D temperature-efficiency lookup table for temperature-dependent efficiency models. The array elements are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size.

This parameter appears only when you select a temperature-dependent friction model. The default array is [0.95 0.9 0.85].

#### Efficiency matrix

Matrix of component efficiencies used to construct a 2-D temperature-load-efficiency lookup table. The matrix elements are the efficiencies at the temperatures in the **Temperature** array and at the loads in the **Load at elliptical gear** array.

The number of rows must be the same as the number of elements in the **Temperature** array. The number of columns must be the same as the number of elements in the **Load at elliptical gear** array.

This parameter appears only when you select a temperature-and-load-dependent efficiency model. The default matrix is  $[\ 0.85\ 0.8\ 0.75;\ 0.95\ 0.9\ 0.85;\ 0.85\ 0.8\ 0.7\ ].$ 

## Follower power threshold

Visible only if you select Temperature-dependent efficiency as the friction model. Absolute value of the follower shaft power above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero when at rest and the value provided by the temperature-efficiency lookup table when at the power threshold. The default value is 0.001 W.

## Follower angular velocity threshold

Visible only if you select Temperature and load-dependent efficiency as the friction model. Absolute value of the follower shaft angular velocity above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor to one, lowering the efficiency losses to zero when at rest. The default value is 0.01 rad/s.

## **Viscous Losses**

## Viscous friction coefficients at base (B) and follower (F)

Two-element array with the viscous friction coefficients in effect at the base and follower shafts. The default array,  $[0 \ 0]$ , corresponds to zero viscous losses.

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

## **Simscape Blocks**

Cycloidal Drive | Simple Gear | Simple Gear with Variable Efficiency

## **Topics**

"Model Thermal Losses in Driveline Components"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# Leadscrew

Leadscrew gear set of threaded rotating screw and translating nut, with adjustable thread and friction losses



# Library

Simscape / Driveline / Gears / Rotational-Translational

# **Description**

The Leadscrew block represents a threaded rotational-translational gear that constrains the two connected driveline axes, screw (S) and nut( N), to, respectively, rotate and translate together in a fixed ratio that you specify. You can choose whether the nut axis translates in a positive or negative direction, as the screw rotates in a positive right-handed direction. If the screw helix is right-handed,  $\omega_{\rm S}$  and  $\nu_{\rm N}$  have the same sign. If the screw helix is left-handed,  $\omega_{\rm S}$  and  $\nu_{\rm N}$  have opposite signs. For model details, see "Leadscrew Gear Model" on page 1-207.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Leadscrew Gear Model**

### **Ideal Gear Constraint and Gear Ratio**

Leadscrew imposes one kinematic constraint on the two connected axes:

$$\omega_{\rm S} L = 2\pi v_{\rm N}$$
.

The transmission ratio is  $R_{\rm NS}=2\pi/L$ . L is the screw lead, the translational displacement of the nut for one turn of the screw. In terms of this ratio, the kinematic constraint is:

$$\omega_{\rm S} = R_{\rm NS} \nu_{\rm N}$$
.

The two degrees of freedom are reduced to one independent degree of freedom. The forward-transfer gear pair convention is (1,2) = (S,N).

The torque-force transfer is:

$$R_{\rm NS}\tau_{\rm S} + F_{\rm N} - F_{\rm loss} = 0$$
,

with  $F_{\rm loss}=0$  in the ideal case.

## **Nonideal Gear Constraint and Losses**

In the nonideal case,  $F_{loss} \neq 0$ . For general considerations on nonideal gear modeling, see "Model Gears with Losses".

In the contact friction case,  $\eta_{\rm SN}$  and  $\eta_{\rm NS}$  are determined by:

- The screw-nut threading geometry, specified by lead angle  $\lambda$  and acme thread half-angle  $\alpha$ .
- The surface contact friction coefficient k.

$$\eta_{\rm SN} = (\cos\alpha - k \cdot \tan\alpha)/(\cos\alpha + k/\tan\lambda) ,$$
  
$$\eta_{\rm NS} = (\cos\alpha - k/\tan\lambda)/(\cos\alpha + k \cdot \tan\alpha) .$$

In the constant efficiency case, you specify  $\eta_{\rm SN}$  and  $\eta_{\rm NS}$ , independently of geometric details.

 $\eta_{\rm NS}$  has two distinct regimes, depending on lead angle  $\lambda$ , separated by the *self-locking point* at which  $\eta_{\rm NS}=0$  and  $\cos\alpha=k/\tan\lambda$ .

- In the *overhauling regime*,  $\eta_{NS} > 0$ . The force acting on the nut can rotate the screw.
- In the self-locking regime,  $\eta_{\rm NS} <$  0. An external torque must be applied to the screw to release an otherwise locked mechanism. The more negative is  $\eta_{\rm NS}$ , the larger the torque must be to release the mechanism.

 $\eta_{\rm SN}$  is conventionally positive.

# **Meshing Efficiency**

The efficiencies  $\eta$  of meshing between screw and nut are fully active only if the transmitted power is greater than the power threshold.

If the power is less than the threshold, the actual efficiency is automatically regularized to unity at zero velocity.

### **Viscous Friction Force**

The viscous friction coefficient  $\mu$  controls the viscous friction torque experienced by the screw from lubricated, nonideal gear threads. The viscous friction torque on a screw driveline axis is  $-\mu_S\omega_S$ .  $\omega_S$  is the angular velocity of the screw with respect to its mounting.

# Limitations

- Gear inertia is assumed negligible.
- · Gears are treated as rigid components.
- · Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
S	Rotational conserving port representing the screw
N	Translational conserving port representing the nut
Н	Thermal conserving port for thermal modeling

# **Parameters**

## Main

#### Screw lead

Translational displacement L of the nut per revolution of the screw. The default is 0.015.

From the drop-down list, choose units. The default is meters (m).

## Screw helix type

Choose the directional sense of screw rotation corresponding to positive nut translation. The default is  ${\tt Right-hand}.$ 

# **Friction Losses**

Parameters for friction losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### **Without Thermal Port**

#### Friction model

Select how to implement friction losses from nonideal meshing of gear threads. The default is No friction losses.

• No friction losses — Suitable for HIL simulation — Gear meshing is ideal.

• Constant efficiency — Transfer of torque and force between screw and nut is reduced by friction. If you select this option, the panel expands.

#### **Constant Efficiency**

#### Friction parametrization

Select how to characterize the friction between gear threads. The default is Friction coefficient and geometrical parameters.

 Friction coefficient and geometrical parameters — Friction is determined by contact friction between surfaces.

### Lead angle

Thread helix angle  $\lambda = \arctan[L/(\pi d)]$ . d is the mean thread diameter. Must be greater than zero. The default is 15.

From the drop-down list, choose units. The default is degrees (deg).

### Acme thread half angle

Half-angle of the acme thread  $\alpha$  in the normal plane. If a square thread is simulated,  $\alpha = 0$ . Must be greater than zero. The default is 14.5.

From the drop-down list, choose units. The default is degrees (deg).

#### Friction coefficient

Dimensionless coefficient of kinetic friction in the thread. Must be greater than zero. The default is 0.08.

• Efficiencies — Friction is determined by constant efficiencies  $0 < \eta < 1$ . If you select this option, the panel changes from its default.

#### **Efficiencies**

## Screw-nut efficiency

Efficiency  $\eta_{\rm SN}$  of the power transfer from screw to nut.

## **Nut-screw efficiency**

Efficiency  $\eta_{\rm NS}$  of the power transfer from nut to screw.

#### Power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default value is  $0.001\,\mathrm{W}$ .

#### With Thermal Port

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase from left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

#### **Screw-nut efficiency**

Array of component efficiencies with the screw as the driver—that is, with power flowing from the screw to the nut. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is  $[0.75 \ 0.7 \ 0.65]$ .

#### **Nut-screw efficiency**

Array of component efficiencies with the nut as the driver—that is, with power flowing from the nut to the screw. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.5 0.45 0.4].

#### Power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is  $0.001\,\mathrm{W}$ .

### **Viscous Losses**

#### Viscous friction coefficient

Viscous friction coefficient  $\mu_S$  for the screw. The default is 0.

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

# **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

#### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Friction Losses** > **Friction model** parameter default setting, No friction losses - Suitable for HIL simulation.

# See Also

#### **Simscape Blocks**

Rack & Pinion | Worm Gear

# **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Ratchet Leadscrew Mechanism"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Limited-Slip Differential**

Reduce velocity difference between two connected shafts **Library:** Gears



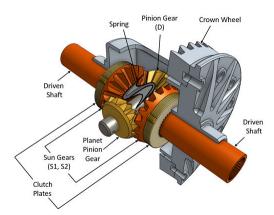
# **Description**

The Limited-Slip Differential block represents a limited-slip differential (LSD), which is a gear assembly that can reduce the velocity difference between two connected shafts. The block models the LSD mechanism as a structural component that combines a differential gear and a clutch.

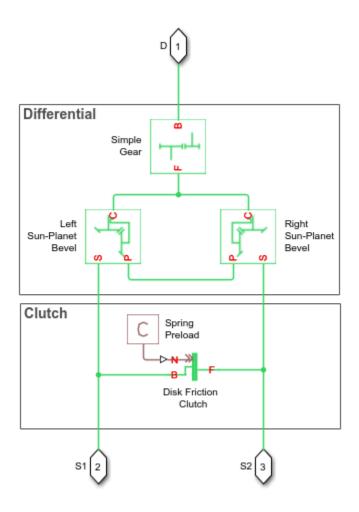
The differential component in the LSD block is an open differential. An open differential is a gear mechanism that allows two driven shafts to spin at different speeds. In an automobile, a differential allows the inner wheels to spin more slowly than the outer wheels when the vehicle is cornering. A vehicle that has wheel shafts that are connected by an open differential can get stuck when only one of the wheels slips and then spins freely due to traction loss. This vehicle stops moving because the driveshaft supplies less power to the wheel with traction than it supplies to the spinning wheel.

In the same scenario, a vehicle that has an LSD is less likely to get stuck because it contains a clutch assembly that can transmit power to the wheel that retains traction. The clutch component in the LSD block is a friction clutch that has two sets of flat friction plates. The clutch engages when applied pressure exceeds the engagement threshold pressure. In an LSD, a spring preload that separates the sun gears presses the plates in both sets together. When the wheels experience a traction differential, the planet pinion gears exert an additional force in the direction of the high-traction wheel. If the additional pressure exceeds the engagement threshold, the clutch assembly engages. The engagement allows the driveshaft to transmit more power to the slower-spinning high-traction wheel. The additional power reduces the difference in velocity of the two shafts. Because the high-traction wheel continues to rotate, the vehicle continues to move.

The figure shows the orientation of the major components in an LSD mechanism.



The Limited-Slip Differential block models the LSD mechanism as a structural component based on the Simscape Driveline Differential and Disk Friction Clutch blocks. The differential mechanism modeled by the Differential block is a structural component based on two other Simscape Driveline blocks, the Simple Gear and the Sun-Planet Bevel. The block diagram shows the structural components of the LSD.



The ports of the Limited-Slip Differential block are associated with the driveshaft (port D) and the two driven shafts (ports S1 and S2), which connect the sun-gears to the wheels.

The block enables you to specify inertias only for the gear carrier and internal planet gears. By default, the inertias of the outer gears are assumed negligible. To model the inertias of the outer gears, connect Simscape Inertia blocks to the D, S1, and S2 ports.

The table shows the rotation direction of the driven shaft ports for different block parameterizations and input conditions.

Rotation Direction of the driven shaft ports (S1 and S2)	Crown Wheel Location Relative to the Centerline	Rotation Direction of Driveshaft Port (D)	Relative Slippage Across the Differential
Positive	Right	Positive	0
<ul><li>Positive for the nonslipping port</li><li>Negative the slipping port</li></ul>	Right	Positive	> 0
Negative	Right	Negative	0
<ul><li>Negative for the nonslipping port</li><li>Positive the slipping port</li></ul>	Right	Negative	> 0
Negative	Left	Positive	0
<ul><li>Negative for the nonslipping port</li><li>Positive the slipping port</li></ul>	Left	Positive	> 0
Positive	Left	Negative	0
<ul><li>Positive for the nonslipping port</li><li>Negative the slipping port</li></ul>	Left	Negative	> 0

# Model

To examine the mathematical models for the structural components of the Limited-Slip Differential block, see:

- · Disk Friction Clutch
- Differential
- · Simple Gear
- Sun-Planet Bevel

# **Port Options**

The Limited-Slip Differential block offers these port options:

- No thermal port (default)
- Show thermal port

To model thermal losses, select Show thermal port. Thermal ports are conserving ports that you can connect to thermal conserving ports on Simscape Foundation Thermal Library blocks for simulating heat flow and temperature changes. For more information, see "Model Thermal Losses in Driveline Components".

To view or select a port option, use one of these methods:

- Use the block context menu:
  - 1 Left-click the block.
  - 2 From the context menu, select Simscape > Block choices.
  - **3** Select option from the drop-down menu.
- Use the Property Inspector:
  - 1 From the Simulink® Editor menu, select **View > Property Inspector**.
  - **2** Click the block.
  - 3 In the Property Inspector pane, click the **Block Choice VALUE**.
  - 4 Select an option from the drop-down menu.

These parameters are enabled only if you select No thermal port:

- Friction Model
- Static friction coefficient

These parameters are enabled only if you select Show thermal port:

- Temperature Sun-sun efficiency
- · Sun-sun efficiency
- · Carrier-driveshaft efficiency
- Sun-carrier and driveshaft-casing power thresholds
- · Sun-carrier and driveshaft-casing viscous friction coefficients
- Kinetic friction coefficient matrix
- Static friction coefficient vector

- Thermal mass
- Initial temperature

# **Ports**

# Conserving

#### D — Driving shaft interface

mechanical rotational

Port associated with the driveshaft.

#### S2, S2 — Driven shaft interfaces

mechanical rotational

Ports associated with the two sun-gear shafts.

#### **H** — Heat exchange

thermal

Port associated with heat flow. The thermal port is optional and is hidden by default.

### **Dependencies**

To enable this port, for **Block Choice**, select Show thermal port.

# **Parameters**

#### **Differential**

#### Crown wheel location — Driveshaft location

To the right of centerline (default) | To the left of centerline

Location of the bevel crown gear regarding the centerline of the gear assembly.

Carrier (C) to driveshaft (D) teeth ratio (NC/ND) — Gear ratio  $4 \, (default)$ 

Fixed ratio,  $g_{\mathrm{D}}$ , of the carrier gear to the longitudinal driveshaft gear.

#### Friction model — Frictional loss

No meshing losses — Suitable for HIL simulation (default) | Constant efficiency

Select whether to consider frictional losses from nonideal meshing of gear teeth:

- No meshing losses Suitable for HIL simulation Gear meshing is ideal and losses are assumed negligible.
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ .

You can increase the fidelity of your model by specifying meshing losses. For hardware-inthe-loop simulation, however, if your model is not real-time capable, consider ignoring the frictional losses. For more information on balancing speed and fidelity for real-time simulation using Simscape models, see "Improving Speed and Accuracy" (Simscape).

#### **Dependencies**

To enable this parameter, for **Block Choice**, select No thermal port.

Selecting Constant efficiency enables these parameters:

- Sun-sun and carrier-driveshaft ordinary efficiencies
- · Sun-carrier and driveshaft-casing power thresholds
- · Sun-carrier and driveshaft-casing viscous friction coefficients

# ${\bf Sun-sun\ and\ carrier-driveshaft\ ordinary\ efficiencies-Torque\ transfer\ efficiency}$

[0.85, 0.92] (default)

Vector of torque transfer efficiencies [ $\eta_{SS}$   $\eta_{D}$ ] for sun-sun and carrier-longitudinal driveshaft gear wheel pair meshings, respectively.

#### **Dependencies**

To enable this parameter:

- 1 For **Block choice**, select No thermal port.
- 2 For Friction model, select Constant efficiency.

# Temperature — Component temperature

[280.0, 300.0, 320.0] W (default)

Array of temperatures used to construct 1-D temperature-efficiency lookup tables. The array values must increase left to right. The temperature array must be the same size as each efficiency array.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

# Sun-sun efficiency — Mechanical efficiency

[0.95, 0.9, 0.85] (default)

Array of mechanical efficiencies with power flowing from one of the sun gears to the other. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

### Carrier-driveshaft efficiency — Mechanical efficiency

[0.95, 0.9, 0.85] (default)

Array of mechanical efficiencies with power flowing from the gear carrier to the longitudinal driveshaft. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

# Sun-carrier and driveshaft-casing power thresholds — Efficiency boundary

[0.001, 0.001] W (default)

Vector of power thresholds  $p_{th}$  above which full efficiency loss is applied, for sun-carrier and longitudinal driveshaft-casing  $[p_{\rm S} \ p_{\rm D}]$ , respectively. A hyperbolic tangent function smooths the efficiency factors between zero when at rest and the values provided by the temperature-efficiency lookup tables at the power thresholds.

#### **Dependencies**

To enable this parameter:

- 1 For **Block choice**, select No thermal port.
- 2 For Friction model, select Constant efficiency.

or for **Block choice**, select Show thermal port.

# Sun-carrier and driveshaft-casing viscous friction coefficients — Component viscosity

[0.0, 0.0] N\*m/(rad/s) (default)

Vector of viscous friction coefficients [ $\mu_S \mu_D$ ] for the sun-carrier and longitudinal driveshaft-casing gear motions, respectively.

#### **Dependencies**

To enable this parameter:

- 1 For **Block choice**, select No thermal port.
- **2** For **Friction model**, select Constant efficiency.

or for **Block choice**, select Show thermal port.

### Carrier inertia — Moment of inertia

0 kg\*m^2 (default)

Moment of inertia of the planet gear carrier. This value must be positive or zero. To ignore carrier ring inertia, enter  $\theta$ .

### Planet inertia — Moment of inertia

0 kg\*m^2 (default)

Moment of inertia of the combined planet gears. This value must be positive or zero. To ignore planet gear inertia, enter  $\theta$ .

#### Clutch

# Number of friction surfaces — Number of contact surfaces 4 (default)

Number, N, of friction-generating contact surfaces inside the clutch.

# Effective torque radius — Friction force application radius

130 mm (default)

Effective moment arm radius,  $r_{eff}$ , that determines the kinetic friction torque inside the clutch.

# Preload force — Clutch plate engagement pressure 300 N (default)

Preload force that the spring exerts on the clutch plate assemblies. Must be greater than or equal to zero.

# Kinetic friction coefficient relative velocity vector — Absolute surface velocity

[0.0, 100.0, 1000.0] rad/s (default)

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension.

Kinetic friction coefficient vector — Coulomb coefficient of friction,  $k_K$  [0.3, 0.22, 0.19] (default) | . For a block choice that shows the thermal port, the default value is [0.3, 0.28, 0.25]

Specify the output values for the kinetic friction coefficient as a vector. All values must be greater than zero.

Kinetic friction coefficient matrix — Coulomb coefficient of friction,  $k_K$  [0.34, 0.32, 0.3; 0.3, 0.28, 0.25; 0.25, 0.2, 0.15] (default)

The coefficient of kinetic friction must be greater than zero.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

Static friction coefficient vector — Coulomb coefficient of friction,  $k_s$  [0.4, 0.38, 0.36] (default)

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

# Friction coefficient interpolation method — Output value approximation method

Linear (default) | Smooth

Interpolation methods for approximating the output value when the input value is between two consecutive grid points. To optimize performance, select Linear. To produce a continuous curve with continuous first-order derivatives, select Smooth.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

# Friction coefficient extrapolation method — Output value approximation method

Linear (default) | Nearest

Extrapolation methods for approximating the output value when the input value is outside the range specified in the argument list. To produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region, select Linear. To produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data, select Nearest.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

# Static friction coefficient — Coulomb coefficient of friction, $k_S$ 0.35 (default)

Dimensionless Coulomb static friction coefficient,  $k_{\rm S}$ , applied to the normal force across the clutch when the clutch is locked. The static friction coefficient,  $k_{\rm S}$ , must be larger than the kinetic friction coefficient,  $k_{\rm K}$ .

#### **Dependencies**

To enable this parameter, for **Block Choice**, select No thermal port.

# **Velocity tolerance** — **Slip velocity locking boundary** 0.001 rad/s (default)

Maximum slip velocity at which the clutch can lock. The slip velocity is the signed

difference between the base and follower shaft angular velocities, that is,  $w=w_F-w_B$ . When the kinetic friction torque is nonzero and the transferred torque is within the static

friction torque limits, then the clutch locks if the actual slip velocity falls below the velocity tolerance.

#### Initial state — Initial clutch state

Unlocked (default) | Locked

Clutch state at the start of simulation. The clutch can be in one of two states, locked and unlocked. A locked clutch constrains the base and follower shafts to spin at the same velocity, that is, as a single unit. An unlocked clutch allows the two shafts to spin at different velocities, resulting in slip between the clutch plates.

#### **Thermal Port**

# Thermal mass — Component resistance to temperature change 50 J/K (default)

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

# **Initial temperature — Component initial temperature** 300 K (default)

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses.

#### **Dependencies**

To enable this parameter, for **Block choice**, select Show thermal port.

# See Also

#### **Simscape Blocks**

Differential | Disk Friction Clutch | Simple Gear | Sun-Planet Bevel

# **Topics**

"Model Thermal Losses in Driveline Components"

"Basic Motion, Torque, and Force Modeling"

# Introduced in R2017a

# **Loaded-Contact Rotational Friction**

Loaded-contact friction between two rotating bodies



# Library

Brakes & Detents/Rotational

# **Description**

The Loaded-Contact Rotational Friction block simulates friction between two rotating bodies loaded with a normal force.

The block is implemented as a structural component based on the Fundamental Friction Clutch block. From the locked state, the clutch unlocks if the friction force exceeds the static friction, as defined by the static coefficient of friction and current normal force. For details on how the locking and unlocking are modeled, see the Fundamental Friction Clutch block reference page.

Friction torque is transmitted for normal forces larger than the **Threshold force** parameter.

# **Loaded-Contact Rotational Friction Model**

The block simulates friction between two rotating bodies loaded with a normal force. When the two rotating bodies are not locked, the friction torque is determined with the following equations:

$$\tau_{\rm fr} = N \cdot \mu \cdot r_{\rm eff} \cdot {\rm sign}(\omega) + \tau_{\rm visc}$$
,

$$r_{\text{eff}} = \frac{2}{3} \cdot \frac{r_0^3 - r_i^3}{r_0^2 - r_i^2}$$
,

$$\tau_{\rm visc} = \mu_{\rm visc} \cdot \omega$$
 ,

#### where:

$ au_{ m fr}$	Friction torque
N	Normal force
μ	Friction coefficient
$r_{ m eff}$	Effective radius
$r_{\rm o}$	Disk outside radius
$r_{ m i}$	Disk inside radius
ω	Relative angular velocity
$ au_{ m visc}$	Viscous drag torque
$\mu_{ m visc}$	Viscous drag torque coefficient

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# Limitations

- The model does not account for inertia. Add inertia terms externally to the B and F ports as required.
- The model computes the torque assuming a uniform distribution of the normal force.

# **Ports**

В

Rotational conserving ports associated with the driving shaft

F

Rotational conserving ports associated with the driven shaft

N

Physical signal terminal through which you import the normal force

Н

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

# **Parameters**

#### **Dimensions**

#### Force action region

Select a parameterization method to model the loaded-contact friction. The default method is Define effective radius.

Define effective radius — Provide a value for the friction effective radius.
 Effective torque radius

Effective radius  $r_{\rm eff}$ . Must be greater than zero. The default value is 130 mm.

 Define annular region — Define the friction effective radius in terms of the inside and outside diameters of the friction disk. If you select this option, the panel changes from its default.

### Define annular region

#### Friction disk outside diameter

Outside diameter  $r_{\rm o}$  of the friction disks. Must be greater than zero. The default value is 150 mm.

#### Friction disk inside diameter

Inside diameter  $r_i$  of the friction disks. Must be greater than zero, but less than the friction disk outside diameter. The default value is 100 mm.

#### **Friction**

#### Friction model

Select a parameterization method to model the kinetic friction coefficient. The options and default values for this parameter depend on the variant that you select for the block. The options are:

- Fixed kinetic friction coefficient Provide a fixed value for the kinetic friction coefficient. This option:
  - Is only visible if you use the default variant of the block
  - Is the default method for parameterizing the default variant of the block
  - Affects the visibility of other parameters

#### Fixed kinetic friction coefficient

#### Kinetic friction coefficient

The kinetic, or Coulomb, friction coefficient. The coefficient must be greater than zero. The default value is 0.3.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Table lookup kinetic friction coefficient Define the kinetic friction coefficient by one-dimensional table lookup based on the relative angular velocity between disks. This option:
  - Is only visible if you use the default variant of the block
  - · Affects the visibility of other parameters

# Table lookup kinetic friction coefficient

## Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient vector

Specify the output values for the kinetic friction coefficient as a vector. All values must be positive. The default value is [0.3, 0.22, 0.19].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go
  above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Temperature-dependent kinetic friction coefficient Define the kinetic friction coefficient by table lookup based on the temperature. This option:
  - Is only visible if you use a thermal variant of the block
  - Is the default method for parameterizing the thermal variant of the block
  - Affects the visibility of other parameters

#### Temperature-dependent kinetic friction coefficient

#### Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

#### Kinetic friction coefficient vector

Specify the output values for kinetic friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. All values must be greater than zero. The default value is [0.3, 0.28, 0.25].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

# Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

- Temperature and speed-dependent kinetic friction coefficient —
  Define the kinetic friction coefficient by table lookup based on the temperature
  and the relative angular velocity between disks. This option:
  - Is only visible if you use the thermal variant of the block
  - Affects the visibility of other parameters

# Temperature and speed-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

#### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is  $[0.0,\ 100.0,\ 1000.0]$  rad/s.

#### Kinetic friction coefficient matrix

Specify the output values for kinetic friction coefficient as a matrix. All the values must be greater than zero. The size of the matrix must equal the size of the matrix that is the result of the temperature vector  $\times$  the kinetic friction coefficient relative velocity vector. The default value is [0.34, 0.32, 0.3; 0.3, 0.28, 0.25; 0.25, 0.2, 0.15].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

### **Velocity tolerance**

Relative velocity below which the two surfaces can lock. The surfaces lock if the torque across the B and F rotational ports is less than the product of the effective radius, the static friction coefficient, and the applied normal force. The default value is 0.001 rad/s.

#### Threshold force

The normal force applied to the physical signal port N is applied to the contact only if the amount of force exceeds the value of the **Threshold force** parameter. Forces below the **Threshold force** are not applied, and there is consequently no transmitted frictional torque. The default value is  $1 \, N$ .

# **Viscous Drag**

#### Viscous drag torque coefficient

Viscous drag coefficient  $\mu_{\text{visc}}$  for computing the drag torque. The coefficient depends on the type of operating fluid, fluid temperature, and the maximum distance between the disks. The default value is 0 N\*m/(rad/s).

#### **Initial Conditions**

#### **Initial state**

Select the initial condition applied to the Fundamental Friction Clutch state inside the block:

- Locked Rotational ports B and F are initially locked together. This option is the
  default.
- Unlocked Rotational ports B and F are initially sliding relative to each other.

### **Thermal Port**

These thermal parameters are visible only when you select a block variant that includes a thermal port.

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 kJ/K.

#### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# See Also

Fundamental Friction Clutch | Loaded-Contact Translational Friction

# **Topics**

"Gear Coupling Control Using Clutches"

### Introduced in R2011a

# **Loaded-Contact Translational Friction**

Loaded-contact friction between two sliding bodies



# Library

Brakes & Detents/Translational

# **Description**

The Loaded-Contact Translational Friction block simulates friction between two sliding bodies loaded with a normal force.

The block is implemented as a structural component based on the Fundamental Friction Clutch block. From the locked state, the clutch unlocks if the friction force exceeds the static friction, as defined by the static coefficient of friction and current normal force. For details on how the locking and unlocking are modeled, see the Fundamental Friction Clutch block reference page.

Friction force is transmitted for normal forces larger than the **Threshold force** parameter.

# **Loaded-Contact Translational Friction Model**

The block simulates friction between two sliding bodies loaded with a normal force. When the two sliding bodies are not locked, the friction force is determined with the following equations:

$$F_{\rm fr} = N \cdot \mu \cdot {\rm sign}(v_{\rm rel}) + F_{\rm visc}$$
 ,

$$F_{\rm visc} = \mu_{\rm visc} \cdot \nu_{rel}$$
,

#### where:

$F_{ m fr}$	Friction force
N	Normal force
μ	Friction coefficient
$\nu_{ m rel}$	Relative velocity
$F_{ m visc}$	Viscous drag force
$\mu_{ m visc}$	Viscous drag force coefficient

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# Limitations

- The model does not account for body mass. Add mass terms externally to the B and F ports as required.
- The model computes the friction force assuming a uniform distribution of the normal force.

# **Ports**

В

Translational conserving ports associated with the driving shaft

F

Translational conserving ports associated with the driven shaft

N

Physical signal terminal through which you import the normal force

Н

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

# **Parameters**

#### **Friction**

#### Friction model

Select a parameterization method to model the kinetic friction coefficient. The options and default values for this parameter depend on the variant that you select for the block. The options are:

- Fixed kinetic friction coefficient Provide a fixed value for the kinetic friction coefficient. This option:
  - Is only visible if you use the default variant of the block
  - Is the default method for parameterizing the default variant of the block
  - · Affects the visibility of other parameters

#### Fixed kinetic friction coefficient

#### Kinetic friction coefficient

The kinetic, or Coulomb, friction coefficient. The coefficient must be greater than zero. The default value is 0.3.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Table lookup kinetic friction coefficient Define the kinetic friction coefficient by one-dimensional table lookup based on the relative angular velocity between disks. This option:
  - Is only visible if you use the default variant of the block
  - · Affects the visibility of other parameters

# Table lookup kinetic friction coefficient Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. [0.0, 0.1, 1.0] m/s.

#### Kinetic friction coefficient vector

Specify the output values for the kinetic friction coefficient as a vector. All values must be positive. The default value is [0.3, 0.22, 0.19].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

# Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go
  above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Temperature-dependent kinetic friction coefficient Define the kinetic friction coefficient by table lookup based on the temperature. This option:
  - Is only visible if you use a thermal variant of the block
  - Is the default method for parameterizing the thermal variant of the block
  - Affects the visibility of other parameters

# Temperature-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

#### Kinetic friction coefficient vector

Specify the output values for kinetic friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. All values must be greater than zero. The default value is [0.3, 0.28, 0.25].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

# Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

- Temperature and speed-dependent kinetic friction coefficient —
  Define the kinetic friction coefficient by table lookup based on the temperature
  and the relative angular velocity between disks. This option:
  - Is only visible if you use the thermal variant of the block
  - Affects the visibility of other parameters

# Temperature and speed-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. [0.0, 0.1, 1.0] m/s.

#### Kinetic friction coefficient matrix

Specify the output values for kinetic friction coefficient as a matrix. All the values must be greater than zero. The size of the matrix must equal the size of the matrix that is the result of the temperature vector  $\times$  the kinetic friction coefficient relative velocity vector. The default value is  $[0.34,\ 0.32,\ 0.3;\ 0.3,\ 0.28,\ 0.25;\ 0.25,\ 0.2,\ 0.15]$ .

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector.

Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

### Velocity tolerance

Relative velocity below which the two surfaces can lock. The surfaces lock if the torque across the B and F rotational ports is less than the product of the effective radius, the static friction coefficient, and the applied normal force. The default value is 0.001 rad/s.

#### Threshold force

The normal force applied to the physical signal port N is applied to the contact only if the amount of force exceeds the value of the **Threshold force** parameter. Forces below the **Threshold force** are not applied, and there is consequently no transmitted frictional torque. The default value is  $1 \, N$ .

# **Viscous Drag**

#### Viscous drag force coefficient

Viscous drag coefficient  $\mu_{\text{visc}}$  for computing the drag force. The coefficient depends on the type of operating fluid, fluid temperature, and the maximum distance between the sliding bodies. The default value is 0 N/(m/s).

#### **Initial Conditions**

#### **Initial state**

Select the initial condition applied to the Fundamental Friction Clutch state inside the block:

- Locked Translational ports B and F are initially locked together. This is the default option.
- Unlocked Translational ports B and F are initially sliding relative to each other.

### **Thermal Port**

These thermal parameters are visible only when you select a block variant that includes a thermal port.

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 kJ/K.

### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# See Also

Fundamental Friction Clutch | Loaded-Contact Rotational Friction

# **Topics**

"Gear Coupling Control Using Clutches"

### Introduced in R2011a

# **Logic-Controlled Clutch**

Friction clutch with binary input control **Library:** Clutches



# **Description**

The Logic-Controlled Clutch is based on the Fundamental Friction Clutch block, which transmits rotational power through friction. The Logic-Controlled Clutch block is controlled by a binary input. When the input is 1, the clutch engages, provides friction, and can lock. When the input is  $\theta$ , the clutch does not engage or provide friction and it cannot lock.

If the clutch is engaging and in motion, the block applies the dynamic torque. If the clutch is engaging and not in motion, it applies the static torque.

# **Ports**

## Input

### **E** — Control clutch engagement

physical signal

When the input is 1, the clutch engages. When the input is 0, the clutch does not engage.

# Conserving

#### **B** — Base interface

mechanical rotational

Mechanical rotational conserving port associated with the base interface.

#### F — Follower interface

mechanical rotational

Mechanical rotational conserving port associated with the follower interface.

# **Parameters**

# Dynamic friction torque — Rotational force for a moving clutch 10 N\*m (default)

Specify a value that is greater than or equal to zero for the nominal dynamic friction torque that the clutch applies when engaged and the clutch plates have relative motion.

# Static friction torque — Rotational force for a nonmoving clutch 20 N\*m (default)

Specify a value that is greater than or equal to the nominal dynamic friction torque. When the clutch is locked, this amount of clutch is required to break the lock and allow the clutch plates to slip.

# Clutch velocity tolerance — Motion boundary condition 0.001 rad/s (default)

Specify a value that is greater than or equal to zero.

# Initial State — Clutch condition at simulation start time Unlocked (default) | Locked

Indicate whether the clutch is locked or unlocked when the simulation starts.

# See Also

Cone Clutch | Disk Friction Clutch | Dog Clutch | Fundamental Friction Clutch

#### Introduced in R2016b

# **Nonlinear Rotational Damper**

Rotational damper based on polynomial or lookup-table parameterizations



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a nonlinear rotational damper. Polynomial and lookup-table parameterizations define the nonlinear relationship between damping torque and relative angular velocity. The damping torque can be symmetric or asymmetric about the zero velocity point. The block applies equal and opposite damping torques on the two rotational conserving ports.

The symmetric polynomial parameterization defines the damping torque for both positive and negative relative velocities according to the expression:

$$T = b_1\omega + sign(\omega) \cdot b_2\omega^2 + b_3\omega^3 + sign(\omega) \cdot b_4\omega^4 + b_5\omega^5 \,,$$

where:

- T Damping torque
- $b_1, b_2, ..., b_5$  Damping coefficients
- $\omega$  Relative angular velocity between ports R and C,  $\omega$  =  $\omega_R$   $\omega_C$
- $\omega_R$  Absolute angular velocity associated with port R
- $\omega_{\it C}$  Absolute angular velocity associated with port C

To avoid zero-crossings that slow simulation, eliminate the sign function from the polynomial expression by specifying an odd polynomial ( $b_2$ ,  $b_4$  = 0).

The two-sided polynomial parameterization defines the damping torque for both positive and negative relative velocities according to the expression:

$$T = \begin{cases} b_{1p}\omega + b_{2p}\omega^2 + b_{3p}\omega^3 + b_{4p}\omega^4 + b_{5p}\omega^5, & \omega \geq 0 \\ b_{1n}\omega + b_{2n}\omega^2 + b_{3n}\omega^3 + b_{4n}\omega^4 + b_{5n}\omega^5, & \omega < 0 \end{cases},$$

where:

- $b_{1p}$ ,  $b_{2p}$ , ...,  $b_{5p}$  Damping coefficients for positive relative velocities
- $b_{1n}$ ,  $b_{2n}$ , ...,  $b_{5n}$  Damping coefficients for negative relative velocities

Both polynomial parameterizations use a fifth-order polynomial expression. To use a lower-order polynomial, set the unneeded higher-order coefficients to zero. To use a higher-order polynomial, fit to a lower-order polynomial or use the lookup table parameterization.

The lookup table parameterization defines damping torque based on a set of torque and angular velocity vectors. If not specified, the block automatically adds a data point at the origin (zero angular velocity and zero torque).

# **Assumptions and Limitations**

The block assumes viscous damping. The damping force depends only on velocity.

## **Ports**

C

Rotational conserving port.

R

Rotational conserving port.

## **Parameters**

#### **Parameterization**

Select damping parameterization. Options are By polynomial and By lookup table.

### By polynomial

### **Symmetry**

Choose between symmetric and two-sided polynomial parameterizations.

• Symmetric — Specify a single set of polynomial coefficients governing damping for both positive and negative relative velocities.

### **Vector of damping coefficients**

Enter five-element vector with polynomial damping coefficients. Physical units are for the first coefficient.

The default vector is  $[1e-4 \ 0 \ 1e-5 \ 0 \ 1e-6]$ . The default unit is N\*m/(rad/s).

 Two-sided — Specify two sets of polynomial coefficients governing damping, one for positive relative velocities, the other for negative relative velocities.

## Vector of positive rotation damping coefficients

Enter five-element vector with polynomial damping coefficients for positive relative velocities. Physical units are for the first coefficient.

The default vector is [1e-4 0 1e-5 0 1e-6]. The default unit is N\*m/(rad/s).

## Vector of negative rotation damping coefficients

Enter five-element vector with polynomial damping coefficients for negative relative velocities. Physical units are for the first coefficient.

The default vector is [0.001 - 1e-5 1e-4 0 0].

## By lookup table

## Angular velocity vector

Enter vector with relative velocity values. The vector requires a minimum number of elements, based on the selected interpolation method — two for Linear, and three for Smooth. The number of elements must match the torque vector.

The default vector is  $[-1 -0.5 -0.3 -0.1 \ 0.1 \ 0.3 \ 0.5 \ 1]$ . The default unit is rad/s.

#### **Torque vector**

Enter vector with damping torque values corresponding to velocity vector. The vector requires a minimum number of elements, based on the selected interpolation method — two for Linear, three for Smooth. The number of elements must match the velocity vector.

The default vector is [-0.001 - 4e-4 - 2e-4 - 5e-5 5e-5 2e-4 4e-4 0.001]. The unit is N\*m.

#### **Interpolation Method**

Select method used to find velocity-torque values between specified data points.

- Linear Select this option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## **Extrapolation Method**

Select method used to calculate values outside the lookup-table data range.

- Linear Select this option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go
  above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

## See Also

Nonlinear Rotational Damper | Nonlinear Translational Damper | Rotational Damper | Translational Damper | Variable Translational Damper

# **Nonlinear Rotational Spring**

Torsional spring based on polynomial or lookup table parameterizations



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a torsional spring with nonlinear torque-displacement curve. The spring torque magnitude is a general function of displacement. It need not satisfy Hooke's law. Polynomial and lookup-table parameterizations provide two ways to specify the torque-displacement relationship. The spring torque can be symmetric or asymmetric with respect to zero deformation.

The symmetric polynomial parameterization defines spring torque according to the expression:

$$T = k_1\theta + sign(\theta) \cdot k_2\theta^2 + k_3\theta^3 + sign(\theta) \cdot k_4\theta^4 + k_5\theta^5,$$

where:

- *T* Spring force
- $k_1, k_2, ..., k_5$  Spring coefficients
- heta Relative displacement between ports R and C, heta =  $heta_{init}$  +  $heta_R$   $heta_C$
- $heta_{ ext{init}}$  Initial spring deformation
- $\theta_R$  Absolute angular position of port R
- $\theta_{\rm C}$  Absolute angular position of port C

At simulation start (t=0),  $\theta_R$  and  $\theta_C$  are zero, making  $\theta$  equal to  $\theta_{init}$ .

To avoid zero-crossings that slow simulation, eliminate the sign function from the polynomial expression by specifying an odd polynomial ( $b_2$ ,  $b_4$  = 0).

The two-sided polynomial parameterization defines spring torque according to the expression:

$$T = \begin{cases} k_{1t}\theta + k_{2t}\theta^2 + k_{3t}\theta^3 + k_{4t}\theta^4 + k_{5t}\theta^5, & \theta \geq 0 \\ k_{1c}\theta - k_{2c}\theta^2 + k_{3c}\theta^3 - k_{4c}\theta^4 + k_{5c}\theta^5, & \theta < 0 \end{cases},$$

where:

- $k_{1t}$ ,  $k_{2t}$ , ...,  $k_{5t}$  Spring tension coefficients
- $k_{1c}$ ,  $k_{2c}$ , ...,  $k_{5c}$  Spring compression coefficients

Both polynomial parameterizations use a fifth-order polynomial expression. To use a lower-order polynomial, set the unneeded higher-order coefficients to zero. To use a higher-order polynomial, fit to a lower-order polynomial or use the lookup table parameterization.

The lookup table parameterization defines spring torque based on a set of torque and angular velocity vectors. If not specified, the block automatically adds a data point at the origin (zero angular velocity and zero torque).

## **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

## **Ports**

C

Rotational conserving port

R

Rotational conserving port

# **Parameters**

#### **Parameterization**

Select spring parameterization. Options are By polynomial and By lookup table.

### By Polynomial

Specify nonlinear spring function in terms of polynomial coefficients.

### **Symmetry**

Choose between symmetric and two-sided polynomial parameterizations.

 Symmetric — Specify one set of polynomial coefficients governing spring torque in both tension and compression.

## **Vector of spring coefficients**

Enter five-element vector with polynomial spring coefficients. The highest non-zero order must be positive. Physical units are for the first coefficient.

The default vector is  $[1 \ 0 \ 0.1 \ 0 \ 0.01]$ . The default unit is N\*m/rad.

• Two-sided — Specify two sets of polynomial coefficients governing spring torque, one for positive deformation, the other for negative deformation.

## Vector of spring tension coefficients

Enter a five-element vector containing the coefficients of the polynomial spring *tension* function. The highest order non-zero coefficient must be positive. The specified physical unit is the unit of the first polynomial coefficient.

## **Vector of spring compression coefficients**

Enter a five-element vector containing the coefficients of the polynomial spring *compression* function. The highest order non-zero coefficient must

be positive. The specified physical unit is the unit of the first polynomial coefficient.

#### By lookup table

#### **Deformation vector**

Enter a vector containing the deformation values used in the lookup table. The vector must contain a minimum number of elements based on the interpolation method: two for Linear, and three for Smooth. The vector must also contain the same number of elements as the torque vector.

#### Torque vector

Enter a vector containing the torque values that correspond to the deformation vector values. The vector must contain a minimum number of elements based on the interpolation method: two for Linear, and three for Smooth. The vector must also contain the same number of elements as the deformation vector. If not included in the vectors, the block automatically adds a point at the (0,0) deformation-torque coordinate.

#### **Interpolation method**

Select method used to calculate deformation-torque values between lookup-table data points.

- Linear Select this option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## Extrapolation method

Select method used to calculate deformation-torque values outside the lookuptable data range.

- Linear Select this option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go
  above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

# **See Also**

Nonlinear Translational Spring | Variable Rotational Spring | Variable Translational Spring

Introduced in R2013a

# **Nonlinear Translational Damper**

Translational damper based on polynomial or lookup table parameterizations



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a nonlinear translational damper. Polynomial and lookup table parameterizations define the nonlinear relationship between damping force and relative linear velocity. The damping force can be symmetric or asymmetric about the zero velocity point. The block applies equal and opposite damping forces on the two translational conserving ports.

The symmetric polynomial parameterization defines the damping force for both positive and negative relative velocities according to the expression:

$$F = b_1 v + sign(v) \cdot b_2 v^2 + b_3 v^3 + sign(v) \cdot b_4 v^4 + b_5 v^5,$$

where:

- F Damping force
- $b_1$ ,  $b_2$ , ...,  $b_5$  Damping coefficients
- $^{\bullet}$  v Relative linear velocity between ports R and C, v =  $v_R$   $v_C$
- ν<sub>R</sub> Absolute linear velocity associated with port R
- $v_C$  Absolute linear velocity associated with port C

To avoid zero-crossings that slow simulation, eliminate the sign function from the polynomial expression by specifying an odd polynomial ( $b_2$ ,  $b_4$  = 0).

The two-sided polynomial parameterization defines the damping force for both positive and negative relative velocities according to the expression:

$$F = \begin{cases} b_{1e}v + b_{2e}v^2 + b_{3e}v^3 + b_{4e}v^4 + b_{5e}v^5, & v \geq 0 \\ b_{1c}v - b_{2c}v^2 + b_{3c}v^3 - b_{4c}v^4 + b_{5c}v^5, & v < 0 \end{cases},$$

where:

- $b_{1e}$ ,  $b_{2e}$ , ...,  $b_{5e}$  Damping coefficients for positive relative velocities
- $b_{1c}$ ,  $b_{2c}$ , ...,  $b_{5c}$  Damping coefficients for negative relative velocities

Positive relative velocities correspond to damper extension (ports R and C moving away from each other). Negative relative velocities correspond to damper contraction (ports R and C moving towards each other).

Both polynomial parameterizations use a fifth-order polynomial expression. To use a lower-order polynomial, set the unneeded higher-order coefficients to zero. For polynomials of order greater than five, fit to a polynomial of order smaller than or equal to five, or use the lookup table parameterization.

The lookup table parameterization defines damping force based on a set of velocity and force vectors. If not included in the vectors, the block automatically adds a data point at the origin (zero velocity and zero force).

# **Assumptions and Limitations**

The block assumes viscous damping. The damping force depends only on velocity.

# **Ports**

C

Rotational conserving port

R

Rotational conserving port

## **Parameters**

#### **Parameterization**

Select damping parameterization. Options are By polynomial and By lookup table.

### By polynomial

Specify coefficients of polynomial damping function.

### **Symmetry**

Choose between symmetric and two-sided polynomial parameterizations.

• Symmetric — Specify a single set of polynomial coefficients governing damping for both positive and negative relative velocities.

### **Vector of damping coefficients**

Enter five-element vector with polynomial damping coefficients. Physical units are for the first coefficient.

The default vector is [10 0 1 0 0.1]. The default unit is N/(m/s).

• Two-sided — Specify two sets of polynomial coefficients governing damping, one for positive relative velocities, the other for negative relative velocities.

## Vector of extension damping coefficients

Enter five-element vector with polynomial damping coefficients for positive relative velocities. Physical units are for the first coefficient.

The default vector is [10 0 1 0 0.1]. The default unit is N/(m/s).

## Vector of contraction damping coefficients

Enter five-element vector with polynomial damping coefficients for negative relative velocities. Physical units are for the first coefficient.

The default vector is [10 0 1 0 0.1]. The default unit is N/(m/s).

## By lookup table

## Velocity vector

Enter vector with relative velocity values. The vector requires a minimum number of elements, based on the selected interpolation method — two for Linear, and three for Smooth. The number of elements must match the force vector.

The default vector is  $[-1 -0.5 -0.3 -0.1 \ 0.1 \ 0.3 \ 0.5 \ 1]$ . The default unit is m/s.

#### Force vector

Enter vector with damping force values corresponding to velocity vector. The vector requires a minimum number of elements, based on the selected interpolation method — two for Linear, three for Smooth. The number of elements must match the velocity vector.

The default vector is [-100 - 40 - 20 - 5 5 20 40 100]. The default unit is N.

#### **Interpolation Method**

Select method used to find intermediate velocity-force values between lookuptable data points.

- Linear Select this option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## **Extrapolation Method**

Select method used to calculate values outside the lookup-table data range.

- Linear Select this option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

## See Also

Nonlinear Rotational Damper | Rotational Damper | Translational Damper | Variable Rotational Damper | Variable Translational Damper

# **Nonlinear Translational Spring**

Translational spring based on polynomial or lookup table parameterizations

# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a translational spring with nonlinear force-displacement curve. The spring force magnitude is a general function of displacement. It need not satisfy Hooke's law. Polynomial and lookup-table parameterizations provide two ways to specify the force-displacement relationship. The spring force can be symmetric or asymmetric with respect to zero deformation.

The symmetric polynomial parameterization defines spring force according to the expression

$$F = k_1 x + sign(x) \cdot k_2 x^2 + k_3 x^3 + sign(x) \cdot k_4 x^4 + k_5 x^5,$$

where:

- F Spring force
- $k_1, k_2, ..., k_5$  Spring coefficients
- x Relative displacement between ports R and C,  $x = x_{init} + x_R x_C$
- $x_{init}$  Initial relative displacement
- $x_{\rm C}$  Absolute displacement associated with port C

At simulation start (t=0),  $x_R$  and  $x_C$  are zero, making x equal to  $x_{init}$ .

To avoid zero-crossings that slow simulation, eliminate the sign function from the polynomial expression by specifying an odd polynomial ( $b_2$ ,  $b_4$  = 0).

The asymmetric polynomial parameterization defines spring force according to the expression:

$$F = \begin{cases} k_{1t}x + k_{2t}x^2 + k_{3t}x^3 + k_{4t}x^4 + k_{5t}x^5, & x \geq 0 \\ k_{1c}x + k_{2c}x^2 + k_{3c}x^3 + k_{4c}x^4 + k_{5c}x^5, & x < 0 \end{cases},$$

where:

- $k_1$ ,  $k_2$ , ...,  $k_5$  Spring tension coefficients
- $k_1, k_2, ..., k_5$  Spring compression coefficients

Both polynomial parameterizations use a fifth-order polynomial expression. To use a lower-order polynomial, set the unneeded higher-order coefficients to zero. To use a higher-order polynomial, fit to a lower-order polynomial or use the lookup table parameterization.

The lookup table parameterization defines damping torque based on a set of torque and angular velocity vectors. If not specified, the block automatically adds a data point at the origin (zero angular velocity and zero torque).

## **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

# **Ports**

C

Rotational conserving port

R

Rotational conserving port

## **Parameters**

#### **Parameterization**

Select spring parameterization. Options are By polynomial and By lookup table.

### By polynomial

Specify coefficients of polynomial spring function.

### **Symmetry**

Choose between symmetric and two-sided polynomial parameterizations.

• Symmetric — Specify one set of polynomial coefficients governing spring force in both tension and compression.

## Vector of spring coefficients

Enter five-element vector with polynomial spring coefficients. The highest non-zero order must be positive. Physical units are for the first coefficient.

The default vector is [100 0 10 0 1]. The default unit is N/m.

 Two-sided — Specify two sets of polynomial coefficients governing spring force, one for positive relative displacements, the other for negative relative displacements.

## **Vector of spring tension coefficients**

Enter five-element vector with polynomial spring tension coefficients. Physical units are for the first coefficient.

The default vector is [100 0 10 0 1]. The default unit is N/m.

#### **Vector of spring compression coefficients**

Enter five-element vector with polynomial spring compression coefficients. Physical units are for the first coefficient.

The default vector is  $[1000 -10 \ 100 \ 0]$ . The default unit is N/m.

#### By lookup table

#### **Deformation vector**

Enter vector with relative displacement values. the vector requires a minimum number of elements, based on the selected interpolation method — two for Linear, and three for Smooth. The number of elements must match the force vector. If not included in the vector, the block automatically adds a point at the origin, corresponding to zero displacement and zero force. If the vector includes a zero value, then the force vector must contain a corresponding zero value.

#### Force vector

Enter a vector containing the force values that correspond to the deformation vector values. The vector must contain a minimum number of elements based on the interpolation method: two for Linear, and three for Smooth. The vector must also contain the same number of elements as the deformation vector. If not included in the vectors, the block automatically adds a point at the (0,0) deformation-force coordinate.

## **Interpolation Method**

Select method used to find intermediate velocity-force values between lookuptable data points.

- Linear Select this option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## **Extrapolation Method**

Select method used to calculate values outside the lookup-table data range.

 Linear — Select this option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region. • Nearest — Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

# See Also

Nonlinear Rotational Spring | Variable Rotational Spring | Variable Translational Spring

# **Piston**

Piston mechanism of reciprocating combustion engine

# Library

**Engines** 

# **Description**

This block represents the piston mechanism of a reciprocating combustion engine. The piston model accounts for the instantaneous torque transmitted to the engine crankshaft. The instantaneous torque enables you to model vibrations in the drivetrain due to piston revolution. To model a multipiston engine, use the Piston Engine block.

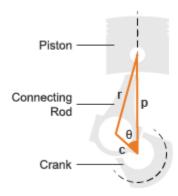
Port B represents the translating piston and port F the rotating crankshaft. The piston force follows from the cylinder pressure and cross-sectional area. The block obtains the combustion pressure from a lookup table parameterized in terms of the crank angle and, optionally, the crank angular velocity and engine throttle level.

The crank torque follows from the piston force and crank angle as well as the crank and connecting rod lengths. In terms of these inputs, the ratio of the piston force and crank torque is

$$\frac{T_{\rm F}}{F_{\rm B}} = -{\rm c} \left( sin(\theta) + \frac{sin(2\theta)}{2\sqrt{\left(\frac{{\rm r}}{{\rm c}}\right)^2 - \sin^2(\theta)}} \right),$$

#### where:

- $F_{\rm B}$  is the instantaneous piston force associated with the base port.
- $T_{\rm F}$  is the instantaneous crank torque associated with the follower port.
- *c* is the crank length.
- $\theta$  is the instantaneous crank angle.
- *r* is the connecting rod length.



#### **Piston Dimensions**

Physical signal port T lets you specify the engine throttle level as a fraction between 0 and 1. This fraction corresponds to the percentage of full power generated. The block uses the physical signal input whenever the pressure lookup table in the block dialog box is parameterized only in terms of the crank angle.

## **Parameters**

## Cylinder bore

Internal diameter of the engine cylinder that the piston travels in. The default value is 0.10 m.

#### Piston stroke

Distance between the top dead center and bottom dead center piston positions. The default value is 0.06 m.

### Piston rod length

Length of the connecting rod located between the engine piston and the crankshaft. The default value is 0.10 m.

### Number of strokes per cycle

Number of strokes required to complete one engine cycle. One stroke corresponds to a full extension or retraction of the engine piston. A typical automobile engine is based on a four-stroke cycle with induction, compression, power, and exhaust stages. The default value is 4

### Pressure parameterization

Engine variables that the cylinder pressure depends on. Options include By crank angle, By crank angle and throttle, By crank angle, throttle, and crank velocity. The default setting is By crank angle.

### Crank angle vector

M-element vector of crank angles at which to specify the cylinder pressure. A zero angle corresponds to a piston at top dead center. The vector must range from -S\*180 to +S\*180 degrees, where S is the number of strokes per cycle. The default vector is an eight-element vector ranging in value from -360 to +360 deg, corresponding to a four-stroke cycle.

#### Throttle vector

N-element vector of engine throttle settings at which to specify the cylinder pressure. A value of 0 corresponds to no throttle and a value of 1 to full throttle. This parameter is active only when **Pressure parameterization** is set to By crank angle and throttle and By crank angle, throttle, and crank velocity. The default vector is [0.0, 0.3, 0.8, 1.0].

## Crank velocity vector

L-element vector of crankshaft angular velocities at which to specify the cylinder pressure. This parameter is active only when **Pressure parameterization** is set to By crank angle, throttle, and crank velocity. The default vector is [0.0, 1000.0, 6000.0] rpm.

#### Pressure vector

*M*-element vector of cylinder pressures corresponding to the crank angles specified in the **Crank angle vector** parameter. This parameter is active only when **Pressure parameterization** is set to By crank angle.

## Pressure matrix (gauge)

*M*-by-*N* matrix of cylinder pressures corresponding to the crank angles and throttle settings specified in the **Crank angle vector** and **Throttle vector** parameters. This

parameter is active only when **Pressure parameterization** is set to By crank angle and throttle. The default matrix is an 8-by-4 matrix ranging in value from 0 to 50 bar.

### Pressure matrix 3D (gauge)

M-by-N-by-L matrix of cylinder pressures corresponding to the crank angles, throttle settings, and crank angular velocity values specified in the **Crank angle vector**, **Throttle vector**, and **Crank velocity vector** parameters. This parameter is active only when **Pressure parameterization** is set to By crank angle, throttle, and crank velocity. The default matrix is an 8-by-4-by-3 matrix ranging in value from 0 to 50 bar.

### Bearing viscous friction coefficient

Aggregate viscous friction coefficient of the main and rod bearings. The block uses this parameter to compute the viscous power losses between the base and follower shafts. The default value is  $0.001 \, N^*m/(rad/s)$ .

### Offset angle

Point in the engine cycle when the piston reaches top dead center. The engine cycle spans in angle from -S\*180 to +S\*180 degrees, where S is the number of strokes per cycle. The default value is 0 deg, corresponding to a zero offset.

## Initial crank angle

Crank angle at time zero relative to a top dead center position. The default value is 90 deg.

# **Ports**

- B Conserving rotational port representing the engine block
- ${\bf F}$  Conserving rotational port representing the engine crankshaft
- T Physical signal input port for specifying the engine throttle setting

# See Also

Generic Engine | Piston Engine

# **Topics**

"Troubleshoot Engine Issues"

# **Piston Engine**

Reciprocating combustion engine with variable number of pistons



# Library

**Engines** 

# **Description**

This block represents a reciprocating combustion engine with multiple cylinders. The piston model accounts for the instantaneous torque transmitted to the engine drive shaft. The instantaneous torque enables you to model vibrations in the drivetrain due to piston revolution. To model just the piston mechanism of a combustion engine, use the Piston block.

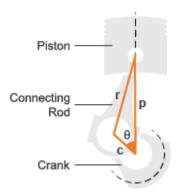
Port B represents the translating piston and port F the rotating crankshaft. The piston force follows from the cylinder pressure and cross-sectional area. The block obtains the combustion pressure from a lookup table parameterized in terms of the crank angle and, optionally, the crank angular velocity and engine throttle level.

The crank torque follows from the piston force and crank angle as well as the crank and connecting rod lengths. In terms of these inputs, the ratio of the piston force and crank torque is

$$\frac{T_{\rm F}}{F_{\rm B}} = -{\rm c} \left( sin(\theta) + \frac{sin(2\theta)}{2\sqrt{\left(\frac{{\rm r}}{{\rm c}}\right)^2 - \sin^2(\theta)}} \right),$$

#### where:

- $F_{\rm B}$  is the instantaneous piston force associated with the base port.
- $T_{\rm F}$  is the instantaneous crank torque associated with the follower port.
- c is the crank length.
- $\theta$  is the instantaneous crank angle.
- *r* is the connecting rod length.



#### **Piston Dimensions**

Physical signal port T lets you specify the engine throttle level as a fraction between 0 and 1. This fraction corresponds to the percentage of full power generated. The block uses the physical signal input whenever the pressure lookup table in the block dialog box is parameterized only in terms of the crank angle.

## **Parameters**

## **Pistons**

## **Number of pistons**

Number of pistons in the combustion engine. The default number is 4.

#### Offset angle vector

Vector of piston offset angles. The offset angle specifies the point in the engine cycle when the piston reaches top dead center. The engine cycle spans in angle from -S\*180 to +S\*180 degrees, where S is the number of strokes per cycle.

The vector size must be the same as the number of pistons. The default vector is [0.0, 180.0, 360.0, -180.0], corresponding to a four-stroke, four-piston engine.

### Cylinder bore

Internal diameter of the engine cylinder that the piston travels in. The default value is 0.10 m.

#### Piston stroke

Distance between the top dead center and bottom dead center piston positions. The default value is  $0.06\ m.$ 

### Piston rod length

Length of the connecting rod located between the engine piston and the crankshaft. The default value is 0.10 m.

### Number of strokes per cycle

Number of strokes required to complete one engine cycle. One stroke corresponds to a full extension or retraction of the engine piston. A typical automobile engine is based on a four-stroke cycle with induction, compression, power, and exhaust stages. The default value is 4

## Pressure parameterization

Engine variables that the cylinder pressure depends on. Options include By crank angle, By crank angle and throttle, By crank angle, throttle, and crank velocity. The default setting is By crank angle.

## Crank angle vector

M-element vector of crank angles at which to specify the cylinder pressure. A zero angle corresponds to a piston at top dead center. The vector must range from -S\*180 to +S\*180 degrees, where S is the number of strokes per cycle. The default vector is an eight-element vector ranging in value from -360 to +360 deg, corresponding to a four-stroke cycle.

#### Throttle vector

N-element vector of engine throttle settings at which to specify the cylinder pressure. A value of 0 corresponds to no throttle and a value of 1 to full throttle. This parameter

is active only when **Pressure parameterization** is set to By crank angle and throttle and By crank angle, throttle, and crank velocity. The default vector is [0.0, 0.3, 0.8, 1.0].

#### Crank velocity vector

L-element vector of crankshaft angular velocities at which to specify the cylinder pressure. This parameter is active only when **Pressure parameterization** is set to By crank angle, throttle, and crank velocity. The default vector is [0.0, 1000.0, 6000.0] rpm.

#### Pressure vector

*M*-element vector of cylinder pressures corresponding to the crank angles specified in the **Crank angle vector** parameter. This parameter is active only when **Pressure parameterization** is set to By crank angle.

### Pressure matrix (gauge)

*M*-by-*N* matrix of cylinder pressures corresponding to the crank angles and throttle settings specified in the **Crank angle vector** and **Throttle vector** parameters. This parameter is active only when **Pressure parameterization** is set to By crank angle and throttle. The default matrix is an 8-by-4 matrix ranging in value from 0 to 50 bar.

### Pressure matrix 3D (gauge)

M-by-N-by-L matrix of cylinder pressures corresponding to the crank angles, throttle settings, and crank angular velocity values specified in the **Crank angle vector**, **Throttle vector**, and **Crank velocity vector** parameters. This parameter is active only when **Pressure parameterization** is set to By crank angle, throttle, and crank velocity. The default matrix is an 8-by-4-by-3 matrix ranging in value from 0 to 50 bar.

## Crankshaft

## **Shaft dynamics**

Optional shaft dynamics parameters. Options include No shaft dynamics — Suitable for HIL simulation and Specify shaft stiffness, damping, and inertia

#### Stiffness

Stiffness coefficient of the engine crankshaft. This parameter accounts for resistance to shaft deformation. This parameter is active only when the **Shaft dynamics** parameter is set to Specify shaft stiffness, damping, and inertia. The default value is  $1e6\ N*m/rad$ .

### **Damping**

Damping coefficients of the engine crankshaft. This parameter accounts for energy dissipation due to shaft deformation. This parameter is active only when the **Shaft dynamics** parameter is set to Specify shaft stiffness, damping, and inertia. The default value is 1000 N\*m/(rad/s).

#### Inertia

Moment of inertia of the crankshaft about its rotational axis. This parameter accounts for resistance to sudden changes in motion. This parameter is active only when the **Shaft dynamics** parameter is set to Specify shaft stiffness, damping, and inertia. The default value is  $0.02 \text{ kg*m}^2$ .

### Initial angular deflection

Deflection angle between the base and follower ends of the crankshaft at time zero. The deflection angle measures the angular deformation of the crankshaft due to torsion. This parameter is active only when the **Shaft dynamics** parameter is set to Specify shaft stiffness, damping, and inertia. The default value is  $\theta$  deg.

#### Initial angular velocity

Angular velocity of the crankshaft at time zero. This parameter is active only when the **Shaft dynamics** parameter is set to Specify shaft stiffness, damping, and inertia. The default value is  $\theta$  rpm.

## Base and follower bearing viscous friction coefficients

Two-element vector with the viscous friction coefficients of the base and follower shaft bearings. The block uses viscous friction to account for energy losses between the base and follower shafts. The default vector is [0.0, 0.0] N\*m/(rad/s), corresponding to zero damping.

## Initial crank angle

Crank angle at time zero relative to a top dead center position. The default value is 90 deg.

## **Ports**

- ${\bf B}$  Conserving rotational port representing the engine block
- F Conserving rotational port representing the engine crankshaft
- T Physical signal input port for specifying the engine throttle setting

Generic Engine | Piston <examplesgroup role="model"></examplesgroup>

# **More About**

"Troubleshoot Engine Issues"

# **Planetary Gear**

Gear train with sun, planet, and ring gears

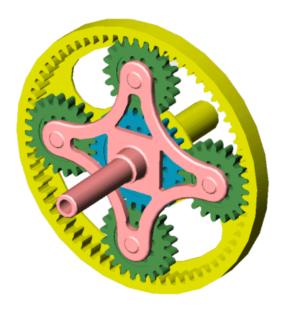


# Library

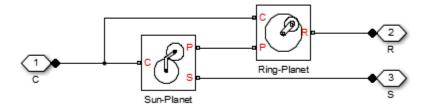
Simscape / Driveline / Gears

# **Description**

This block models a gear train with sun, planet, and ring gears. Planetary gears are common in transmission systems, where they provide high gear ratios in compact geometries. A carrier connected to a drive shaft holds the planet gears. Ports C, R, and S represent the shafts connected to the planet gear carrier, ring gear, and sun gear.



The block models the planetary gear as a structural component based on Sun-Planet and Ring-Planet Simscape Driveline blocks. The figure shows the block diagram of this structural component.



To increase the fidelity of the gear model, you can specify properties such as gear inertia, meshing losses, and viscous losses. By default, gear inertia and viscous losses are assumed negligible. The block enables you to specify the inertias of the internal planet gears only. To model the inertias of the carrier, sun, and ring gears, connect Simscape Inertia blocks to ports C, S, and R.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Planetary Gear Model**

### **Ideal Gear Constraints and Gear Ratios**

Planetary Gear imposes two kinematic and two geometric constraints on the three connected axes and the fourth, internal gear (planet):

$$r_{\rm C}\omega_{\rm C} = r_{\rm S}\omega_{\rm S} + r_{\rm P}\omega_{\rm P}$$
 ,  $r_{\rm C} = r_{\rm S} + r_{\rm P}$  ,   
 $r_{\rm R}\omega_{\rm R} = r_{\rm C}\omega_{\rm C} + r_{\rm P}\omega_{\rm P}$  ,  $r_{\rm R} = r_{\rm C} + r_{\rm P}$  .

The ring-sun gear ratio  $g_{RS} = r_R/r_S = N_R/N_S$ . N is the number of teeth on each gear. In terms of this ratio, the key kinematic constraint is:

$$(1 + g_{RS})\omega_C = \omega_S + g_{RS}\omega_R$$
.

The four degrees of freedom reduce to two independent degrees of freedom. The gear pairs are (1,2) = (S,P) and (P,R).

**Warning** The gear ratio  $g_{RS}$  must be strictly greater than one.

The torque transfer is:

$$g_{\rm RS}\tau_{\rm S}+\tau_{\rm R}-\tau_{\rm loss}=0\;,$$

with  $\tau_{loss} = 0$  in the ideal case.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . See "Model Gears with Losses".

# Limitations

- · Gears are assumed rigid.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port that represents the planet gear carrier
R	Rotational conserving port that represents the ring gear
S	Rotational conserving port that represents the sun gear
Н	Thermal conserving port for thermal modeling

# **Parameters**

### Main

## Ring (R) to sun (S) teeth ratio (NR/NS)

Ratio  $g_{RS}$  of the ring gear wheel radius to the sun gear wheel radius. This gear ratio must be strictly greater than 1. The default is 2.

# **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

• No meshing losses — Suitable for HIL simulation — Gear meshing is ideal.

• Constant efficiency — Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

### **Constant Efficiency**

#### Sun-planet and ring-planet ordinary efficiencies

Vector of torque transfer efficiencies [ $\eta_{SP}$   $\eta_{RP}$ ] for sun-planet and ring-planet gear wheel pair meshings, respectively.

### Sun-carrier and planet-carrier power thresholds

Vector of power thresholds  $p_{\rm th}$  above which full efficiency loss is applied, for sun-carrier and planet-carrier, respectively.

#### With Thermal Port

### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as each efficiency array. The default array is [280 300 320] K.

### **Sun-planet efficiency**

Array of mechanical efficiencies with power flowing from the sun gear to the planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is  $[0.95 \ 0.9 \ 0.85]$ .

## Ring-planet efficiency

Array of mechanical efficiencies with power flowing from the ring gear to the planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is  $[0.95 \ 0.9 \ 0.85]$ .

## Sun-carrier and planet-carrier velocity thresholds

Array of power thresholds above which the full efficiency factors apply. Enter the thresholds for the sun and planet gears relative to the gear carrier, in this order. A hyperbolic tangent function smooths the efficiency factors between zero at rest and the values provided by the temperature-efficiency lookup tables at the power thresholds. The default array is [0.001 0.001] W.

#### Viscous Losses

#### Sun-carrier and planet-carrier viscous friction coefficients

Vector of viscous friction coefficients  $[\mu_S \mu_P]$  for the sun-carrier and planet-carrier gear motions, respectively. The default is  $[0 \ 0]$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

### Inertia

### Planet gear inertia

Moment of inertia of the combined planet gears. This value must be positive or zero. Enter 0 to ignore gear inertia. The default value is 0 kg\*m^2.

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

## Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, **No meshing losses** - **Suitable for HIL simulation**.

# **See Also**

## **Simscape Blocks**

Compound Planetary Gear | Double-Pinion Planetary Gear | Ravigneaux Gear

# **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Planet-Planet**

Planetary gear set of carrier, inner planet, and outer planet wheels with adjustable gear ratio and friction losses

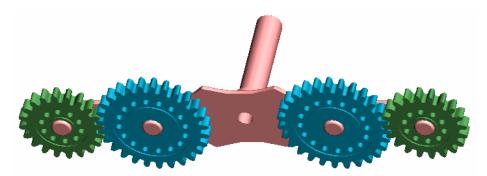


# Library

Simscape / Driveline / Gears / Planetary Subcomponents

# **Description**

The Planet-Planet gear block represents a set of carrier, inner planet, and outer planet gear wheels. Both planetary gears are connected to and rotate with respect to the carrier. The planets corotate with a fixed gear ratio that you specify. For model details, see "Planet-Planet Gear Model" on page 1-283.



# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal

port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Planet-Planet Gear Model**

### **Ideal Gear Constraints and Gear Ratios**

Planet-Planet imposes one kinematic and one geometric constraint on the three connected axes:

$$r_{\rm C}\omega_{\rm C} = r_{\rm Po}\omega_{\rm Po} + r_{\rm Pi}\omega_{\rm Pi}$$
 ,  $r_{\rm C} = r_{\rm Po} + r_{\rm Pi}$  .

The outer planet-to-inner planet gear ratio  $g_{\rm oi} = r_{\rm Po}/r_{\rm Pi} = N_{\rm Po}/N_{\rm Pi}$ . N is the number of teeth on each gear. In terms of this ratio, the key kinematic constraint is:

$$(1 + g_{oi})\omega_{C} = \omega_{Pi} + g_{oi}\omega_{Po}$$
.

The three degrees of freedom reduce to two independent degrees of freedom. The gear pair is (1,2) = (Pi,Po).

The torque transfer is:

$$g_{\rm oi}\tau_{\rm Pi}+\tau_{\rm Po}-\tau_{\rm loss}=0\;,$$

with  $\tau_{loss} = 0$  in the ideal case.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . See "Model Gears with Losses".

## Limitations

- Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port representing the planet carrier
Ро	Rotational conserving port representing the outer planet gear
Pi	Rotational conserving port representing the inner planet gear
Н	Thermal conserving port for thermal modeling

## **Parameters**

#### Main

### Outer planet (Po) to inner planet (Pi) teeth ratio (NPo/NPi)

Ratio  $g_{oi}$  of the outer planet gear radius wheel to the inner planet gear wheel radius. This gear ratio must be strictly positive. The default is 2.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

#### Constant Efficiency

### **Ordinary efficiency**

Torque transfer efficiency  $\eta_{PP}$  for planet-planet gear wheel pair meshing.

### Inner planet-carrier power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default value is  $0.001\,\mathrm{W}$ .

#### With Thermal Port

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

### **Efficiency**

Array of component efficiencies used to construct a 1-D temperature-efficiency lookup table. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.95 0.9 0.85].

## Inner planet-carrier power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is  $0.001 \, \text{W}$ .

## **Viscous Losses**

## Inner planet-carrier viscous friction coefficient

Viscous friction coefficient  $\mu_{Pi}$  for the inner planet-carrier gear motion. The default is  $\theta$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

## **Simscape Blocks**

Planetary Gear | Ravigneaux Gear | Ring-Planet | Sun-Planet | Sun-Planet Bevel

## **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Rack & Pinion**

Rack and pinion gear coupling translational and rotational motion, with adjustable pinion radius and friction losses



# Library

Simscape / Driveline / Gears / Rotational-Translational

# **Description**

The Rack & Pinion block represents rack and pinion gear that converts between translational and rotational motion. The rotational-translational gear constrains the pinion (P) and rack (R) to, respectively, rotate and translate together in a fixed ratio that you specify. You can choose whether the rack axis translates in a positive or negative direction, as the pinion rotates in a positive direction, by using the **Rack direction** parameter.

## Thermal Modeling

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Gear Model**

## **Model Variables**

$R_{\mathrm{RP}}$	Rack-pinion gear ratio
$\omega_{ ext{P}}$	Angular velocity of the pinion shaft
$\nu_{ m R}$	Translational velocity of the rack
$r_{ m P}$	Effective radius of the pinion
$N_{ m P}$	Number of teeth on the pinion
$x_{\rm R}$	Rack tooth spacing
$ au_{ m P}$	Pinion shaft torque
$F_{ m R}$	Rack force
$F_{ m loss}$	Total loss force
$F_{ m Coul}$	Friction force
η	Torque transfer efficiency
$p_{ m th}$	Power threshold
$\mu_{ m P}$	Viscous friction coefficient for the pinion shaft
$\mu_{ m R}$	Viscous friction coefficient for the rack motion

## **Ideal Gear Constraint and Gear Ratio**

Rack & Pinion imposes one kinematic constraint on the two connected axes:

$$\omega_{\rm P} = R_{\rm RP} v_{\rm R} \; .$$

The transmission ratio is:

$$R_{\rm RP}=1$$
 /  $r_{\rm P}=\omega_{\rm P}$  /  $v_{\rm N}=\pm\,2\pi$  /  $N_{\rm P}v_{\rm R}$  .

The two degrees of freedom are reduced to one independent degree of freedom. The forward-transfer gear pair convention is (1,2) = (P,R).

The torque-force transfer is:

$$R_{\rm RP}\tau_{\rm P}+F_{\rm R}-F_{\rm loss}=0\;,$$

with  $F_{loss} = 0$  in the ideal case.

### **Nonideal Gear Constraint**

In the nonideal case,  $F_{loss} \neq 0$ . For general considerations on nonideal gear modeling, see "Model Gears with Losses".

In a nonideal pinion-rack pair (P,R), the angular velocity and geometric constraints are unchanged. But the transferred torque, force, and power are reduced by:

- Coulomb friction between teeth surfaces on P and R, characterized by constant efficiency  $\eta$
- Viscous coupling of drives hafts with bearings, parametrized by viscous friction coefficients  $\mu$

## **Meshing Efficiency**

The efficiency  $\eta$  of meshing between pinion and rack is fully active only if the transmitted power is greater than the power threshold.

If the power is less than the threshold, the actual efficiency is automatically regularized to unity at zero velocity.

Efficiency is assumed equal for both the forward and reverse power flow.

## **Viscous Friction Force**

The viscous friction coefficients  $\mu_P$  and  $\mu_R$  control the viscous friction torque and force experienced by the rack and pinion from lubricated, nonideal bearings. The viscous friction torque on the pinion axis is  $-\mu_P\omega_P$ . The viscous friction force on the rack motion is  $-\mu_R\nu_R$ .

## Limitations

- · Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
P	Rotational conserving port representing the pinion
R	Translational conserving port representing the rack
Н	Thermal conserving port for modeling heat transfer

P is a rotational conserving port. R is a translational conserving port. They represent the pinion and the rack, respectively.

## **Parameters**

### Main

## Parameterize by

Select how to parameterize the rack and pinion gear. The default is Pinion radius.

ullet Pinion radius — Gear ratio is defined by the effective radius of the pinion.

#### Pinion radius

Effective radius of the pinion  $r_{\rm P}$ . Must be greater than zero. The default is 100.

From the drop-down list, choose units. The default is millimeters (mm).

 Tooth parameters — Gear ratio is defined by the number of teeth on the pinion gear and the rack tooth spacing. If you select this option, the panel changes from its default.

### Tooth parameters

## Number of pinion teeth

Number of teeth on the pinion  $N_{\rm P}$ . Must be greater than zero. The default is 20.

#### Rack tooth spacing

Spacing between the teeth on the rack  $x_R$ . Must be greater than zero. The default is 5.

From the drop-down list, choose units. The default is millimeters (mm).

#### **Rack direction**

Choose whether the rack axis translates in a positive or negative direction when the pinion rotates in a positive direction. The default is Positive for positive pinion rotation.

## **Meshing Losses**

Parameters for meshing and friction losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### Friction model

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque and force between pinion and rack is reduced by constant efficiency  $0 < \eta \le 1$ . If you select this option, the panel expands.

## **Constant Efficiency**

## **Efficiency**

Torque transfer efficiency  $\eta$  for the rack-pinion gear meshing, which is the same for the forward and reverse power flows. Must be greater than zero but less than, or equal to, one. The default is 0.8.

## Rack power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default value is  $0.001\,\mathrm{W}$ .

#### With Thermal Port

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

### **Efficiency**

Array of component efficiencies used to construct a 1-D temperature-efficiency lookup table. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.95 0.9 0.85].

### Rack power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is 0.001 W.

#### Viscous Losses

#### Pinion rotational viscous friction coefficient

Viscous friction coefficient  $\mu_P$  for the pinion shaft. The default is 0.

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

#### Rack translational viscous friction coefficient

Viscous friction coefficient  $\mu_R$  for the rack motion. The default is 0.

From the drop-down list, choose units. The default is newton/(meters/second) (N/(m/s)).

## **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

#### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

#### **Simscape Blocks**

Leadscrew | Simple Gear

## **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Ravigneaux Gear**

Planetary gear with two sun gears and two planet gear sets



# Library

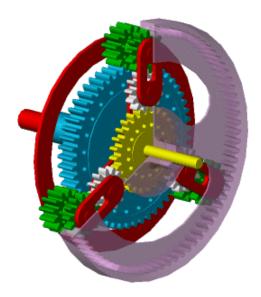
Simscape / Driveline / Gears

# **Description**

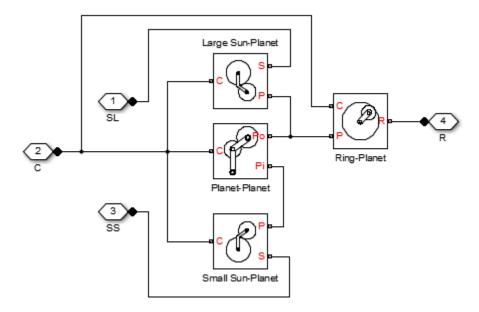
This block represents a planetary gear train with dual sun and planet gear sets. The two sun gears are centrally located and separated longitudinally along a common rotation axis. The smaller of these gears engages an inner planet gear set, which in turn engages an outer planet gear set. The outer planet gear set, whose length spans the distance between the two sun gears, engages both the larger sun gear and the ring gear.

A carrier holds the planet gear sets in place at different radii. The carrier, which rigidly connects to a drive shaft, can spin as a unit with respect to the sun and ring gears. Revolute joints, each located between a planet gear and the carrier, enable the gears to spin about their individual longitudinal axes.

The relative angular velocities of the sun, planet, and ring gears follow from the kinematic constraints between them. For more information, see "Ravigneaux Gear Model" on page 1-297.



The block models the Ravigneaux gear as a structural component based on Sun-Planet, Planet-Planet, and Ring-Planet Simscape Driveline blocks. The figure shows the block diagram of this structural component.



To increase the fidelity of the gear model, you can specify properties such as gear inertia, meshing losses, and viscous losses. By default, gear inertia and viscous losses are assumed negligible. The block enables you to specify the inertias of the internal planet gears only. To model the inertias of the carrier, large sun, small sun, and ring gears, connect Simscape Inertia blocks to ports C, SL, SS, and R.

## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Ravigneaux Gear Model**

### **Ideal Gear Constraints and Gear Ratios**

Ravigneaux imposes four kinematic and four geometric constraints on the four connected axes and the two internal wheels (inner and outer planets):

$$\begin{split} r_{\text{Ci}}\omega_{\text{C}} &= r_{\text{SS}}\omega_{\text{SS}} + r_{\text{Pi}}\omega_{\text{Pi}} \,,\, r_{\text{Ci}} = r_{\text{SS}} + r_{\text{Pi}} \,,\\ r_{\text{Co}}\omega_{\text{C}} &= r_{\text{SL}}\omega_{\text{SL}} + r_{\text{Po}}\omega_{\text{Po}} \,,\, r_{\text{Co}} = r_{\text{SL}} + r_{\text{Po}} \,,\\ (r_{\text{Co}} - r_{\text{Ci}})\omega_{\text{C}} &= r_{\text{Pi}}\omega_{\text{Pi}} + r_{\text{Po}}\omega_{\text{Po}} \,,\, r_{\text{Co}} - r_{\text{Ci}} = r_{\text{Po}} + r_{\text{Pi}} \,,\\ r_{\text{R}}\omega_{\text{R}} &= r_{\text{Co}}\omega_{\text{C}} + r_{\text{Po}}\omega_{\text{Po}} \,,\, r_{\text{R}} = r_{\text{Co}} + r_{\text{Po}} \,. \end{split}$$

The ring-small sun ratio  $g_{\rm RSS} = r_{\rm R}/r_{\rm SS} = N_{\rm R}/N_{\rm SS}$  and ring-large sun gear ratio  $g_{\rm RSL} = r_{\rm R}/r_{\rm SL}$  =  $N_{\rm R}/N_{\rm SL}$ . N is the number of teeth on each gear. In terms of these ratios, the key kinematic constraints are:

$$(g_{RSS} - 1)\omega_{C} = g_{RSS}\omega_{R} - \omega_{SS} ,$$
  
$$(g_{RSI} + 1)\omega_{C} = g_{RSI}\omega_{R} + \omega_{SI} .$$

The six degrees of freedom reduce to two independent degrees of freedom. The gear pairs are (1,2) = (LS,P), (SS,P), (P,R), and (P,P).

**Warning** The gear ratio  $g_{RSS}$  must be strictly greater than the gear ratio  $g_{RSL}$ . The gear ratio  $g_{RSL}$  must be strictly greater than one.

The torque transfers are:

$$g_{\rm RSS}\tau_{\rm SS}+\tau_{\rm R}-\tau_{\rm loss}({\rm SS,R})=0\;,\;g_{\rm RSL}\tau_{\rm SL}+\tau_{\rm R}-\tau_{\rm loss}({\rm SL,R})=0\;,$$
 with  $\tau_{\rm loss}=0$  in the ideal case.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . See "Model Gears with Losses".

# **Limitations**

- · Gears are assumed rigid.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port representing the planet gear carrier
R	Rotational conserving port representing the ring gear
SL	Rotational conserving port representing the large sun gear
SS	Rotational conserving port representing the small sun gear
Н	Thermal conserving port for thermal modeling

## **Parameters**

## Main

## Ring (R) to large sun (SL) teeth ratio (NR/NSL)

Ratio  $g_{\rm RSL}$  of the ring gear wheel radius to the large sun gear wheel radius. This gear ratio must be strictly greater than 1. The default is 2.

## Ring (R) to small sun (SS) teeth ratio (NR/NSS)

Ratio  $g_{\rm RSS}$  of the ring gear wheel radius to the small sun gear wheel radius. This gear ratio must be strictly greater than the ring-large sun gear ratio. The default is 3.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### Friction model

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

#### **Constant Efficiency**

# Large sun-planet, small sun-planet, ring-planet, and planet-planet ordinary efficiencies

Vector of torque transfer efficiencies [ $\eta_{\text{LSP}}$   $\eta_{\text{RSP}}$   $\eta_{\text{RP}}$   $\eta_{\text{PP}}$ ] for large sun-planet, small sun-planet, ring-planet, and planet-planets gear wheel pair meshings, respectively.

# Large sun-carrier, small sun-carrier, large sun planet-carrier, and small sun planet-carrier power thresholds

Vector of power thresholds  $p_{\rm th}$  above which full efficiency loss is applied, for large sun-carrier, small sun-carrier, large sun planet-carrier, and small sun planet-carrier velocities, respectively. The default is [0.001 0.001 0.001 0.001] W.

#### With Thermal Port

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as each efficiency array. The default array is [280 300 320] K.

## Large sun-planet efficiency

Array of mechanical efficiencies with power flowing from the large sun gear to the large sun planet gears. Each array value is the ratio of output power to input power at

one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

### Small sun-planet efficiency

Array of mechanical efficiencies with power flowing from the small sun gear to the small sun planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

### Ring-planet efficiency

Array of mechanical efficiencies with power flowing from the ring gear to the large sun planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

### **Planet-planet efficiency**

Array of mechanical efficiencies with power flowing from the small sun planet gears to the large sun planet gears. Each array value is the ratio of output power to input power at one of the temperatures in the temperature array. The temperature and efficiency arrays must be the same size. The default array is [0.95 0.9 0.85].

# Large sun-carrier, small sun-carrier, large sun planet-carrier and small sun planet-carrier power thresholds

Array of power thresholds above which the full efficiency factors apply. Enter the thresholds for the large sun gear, small sun gear, large sun planet gears, and small sun planet gears, all relative to the gear carrier, in this order. A hyperbolic tangent function smooths the efficiency factors between zero at rest and the values provided by the temperature-efficiency lookup tables at the power thresholds. The default array is [0.001 0.001 0.001 0.001] W.

## **Viscous Losses**

# Large sun-carrier, small sun-carrier, large sun planet-carrier, and small sun planet-carrier viscous friction coefficients

Vector of viscous friction coefficients [ $\mu_{LS}$   $\mu_{SS}$   $\mu_{LSP}$   $\mu_{SSP}$ ] for the large sun-carrier, small sun-carrier, large sun planet-carrier, and small sun planet-carrier gear motions, respectively. The default is [0 0 0 0].

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

#### Inertia

### Inner planet gear inertia

Moment of inertia of the planet gear carrier. This value must be positive or zero. Enter 0 to ignore carrier inertia. The default value is 0 kg\*m^2.

### Outer planet gear inertia

Moment of inertia of the combined planet gears. This value must be positive or zero. Enter 0 to ignore gear inertia. The default value is 0 kg\*m^2.

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

# **See Also**

## Simscape Blocks

Compound Planetary Gear | Planet-Planet | Planetary Gear | Ring-Planet | Sun-Planet

## **Topics**

"Basic Motion, Torque, and Force Modeling"

<sup>&</sup>quot;Ravigneaux Four-Speed Transmission"

<sup>&</sup>quot;Model Thermal Losses in Driveline Components"

<sup>&</sup>quot;Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Ring-Planet**

Planetary gear set of carrier, planet, and ring wheels with adjustable gear ratio and friction losses

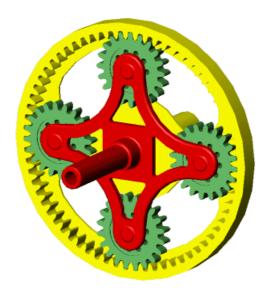


# Library

Simscape / Driveline / Gears / Planetary Subcomponents

# **Description**

The Ring-Planet gear block represents a set of carrier, planet, and ring gear wheels. The planet is connected to and rotates with respect to the carrier. The planet and ring corotate with a fixed gear ratio that you specify. A ring-planet and a sun-planet gear are basic elements of a planetary gear set. For model details, see "Ring-Planet Gear Model" on page 1-304.



## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Ring-Planet Gear Model**

## **Ideal Gear Constraints and Gear Ratios**

Ring-Planet imposes one kinematic and one geometric constraint on the three connected axes:

$$r_{\rm R}\omega_{\rm R}=r_{\rm C}\omega_{\rm C}+r_{\rm P}\omega_{\rm P}$$
 ,  $r_{\rm R}=r_{\rm C}+r_{\rm P}$  .

The ring-planet gear ratio  $g_{\rm RP} = r_{\rm R}/r_{\rm P} = N_{\rm R}/N_{\rm P}$ . N is the number of teeth on each gear. In terms of this ratio, the key kinematic constraint is:

$$g_{\rm RP}\omega_{\rm R}=\omega_{\rm P}+(g_{\rm RP}-1)\omega_{\rm C}$$
.

The three degrees of freedom reduce to two independent degrees of freedom. The gear pair is (1,2) = (P,R).

**Warning** The ring-planet gear ratio  $g_{RP}$  must be strictly greater than one.

The torque transfer is:

$$g_{\rm RP}\tau_{\rm P}+\tau_{\rm R}-\tau_{\rm loss}=0\;,$$

with  $\tau_{loss} = 0$  in the ideal case.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . See "Model Gears with Losses".

# **Limitations**

- Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
	Rotational conserving port representing the planet carrier
	Rotational conserving port representing the planet gear
R	Rotational conserving port representing the ring gear

Port	Description
	Thermal conserving port for thermal modeling

## **Parameters**

#### Main

#### Ring (R) to planet (P) teeth ratio (NR/NP)

Ratio  $g_{RP}$  of the ring gear wheel radius to the planet gear wheel radius. This gear ratio must be strictly greater than 1. The default value is 2.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

## **Constant Efficiency**

### Ordinary efficiency

Torque transfer efficiency  $\eta_{RP}$  for ring-planet gear wheel pair meshing.

## Planet-carrier power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the

efficiency losses to zero when no power is transmitted. The default value is  $0.001~\mathrm{W}$ 

#### With Thermal Port

### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

### **Efficiency**

Array of component efficiencies used to construct a 1-D temperature-efficiency lookup table. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.95 0.9 0.85].

### Planet-carrier power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is  $0.001\,\mathrm{W}$ .

### **Viscous Losses**

#### Planet-carrier viscous friction coefficient

Viscous friction coefficient  $\mu_P$  for the planet-carrier gear motion. The default is  $\theta$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

## **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

## **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

#### **Simscape Blocks**

Compound Planetary Gear | Planet-Planet | Planetary Gear | Sun-Planet | Sun-Planet Bevel

## **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Adjust Model Fidelity"
- "Epicyclic Gear Efficiency Measurement"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Rolling Resistance**

Model rolling resistance



# Library

Tires & Vehicles/Tire Subcomponents

# **Description**

The block models the resistance force that acts on the wheel hub due to the rolling resistance at the road-wheel contact surface. The model can use a constant resistance coefficient or the pressure and velocity dependence of the SAE J2452 standard. The resistance force is zero when the normal force acting at the wheel-road surface is less than or equal to zero.

## **Constant Resistance Coefficient Model**

In the constant coefficient model, the rolling resistance is directly proportional to the resistance coefficient:

F=Nu

where parameters represent the following quantities:

- F Rolling resistance force
- *N* Normal Force
- μ Rolling resistance coefficient

The rolling resistance coefficient has a hyperbolic form that eliminates discontinuity at  $v_{hub}$ =0:

 $\mu = \mu_0 \tanh(4v_{\text{hub}}/v_{\text{threshold}})$ 

where parameters represent the following quantities:

- $\mu_0$  Asymptotic rolling resistance coefficient
- $v_{hub}$  Hub velocity
- $v_{threshold}$  Threshold velocity

## **Pressure and Velocity Dependent Model**

The pressure- and velocity-dependent model uses the following formula:

$$F = \left(\frac{P}{P_0}\right)^{\alpha} \left(\frac{N}{N_0}\right)^{\beta} N_0 \cdot \left(A + B \left|v_{hub}\right| + C v_{hub}^2\right)$$

where parameters represent the following quantities:

- P Tire pressure
- $v_{hub}$  Hub velocity
- $\alpha$ ,  $\beta$ , A, B, C Approximating coefficients
- $P_0 1$  Pascal (Pa)
- $N_0 1$  Newton (N)

In the previous equation, parameters  $P_0$  and  $N_0$  remove the physical units from each exponential expression base.

Connection H is a mechanical translational conserving port that represents the hub of the tire. Connection N is a physical signal input port that represents the normal force acting on the tire. Normal force is positive if it points downward.

## **Parameters**

## **Resistance Model**

Select the model used to compute the rolling resistance on a wheel hub. The parameter provides two options:

- Constant coefficient
- Pressure and velocity dependent

The default value is Constant coefficient.

## **Constant Coefficient**

Selecting the Constant coefficient option exposes two model parameters: Constant coefficient and Velocity threshold.

#### Constant Coefficient

Coefficient that sets the proportionality between the normal force and the rolling resistance force. The parameter must be greater than zero. The default value is 0.015.

### **Velocity Threshold**

Velocity at which the full rolling resistance force is transmitted to the rolling hub. The parameter ensures the force remains continuous during velocity direction changes, which increases the numerical stability of the simulation. The parameter must be greater than zero. The default value is  $0.001 \, \text{m/s}$ .

## **Pressure and Velocity Dependent**

### Tire pressure

Inflation pressure of the tire. The parameter must be greater than zero. The default value is 250e+3 Pa.

## **Alpha**

Exponent of the tire pressure in the model equation. See "Pressure and Velocity Dependent Model" on page 1-310. The default value is -0.003.

#### Beta

Exponent of the normal force model equation. The default value is 0.97.

#### **Coefficient A**

Velocity independent force component in the model equation. The parameter must be greater than zero. The default value is 84e-4.

#### Coefficient B

Velocity dependent force component in the model equation. The parameter must be greater than zero. The default value is  $6.2e-4\,$  s/m.

#### **Coefficient C**

Force component that depends on the square of the velocity term in the model equation. The parameter must be greater than zero. The default value is 1.6e-4 s^2/m^2.

### **Velocity Threshold**

Velocity at which the full rolling resistance force is transmitted to the rolling hub. The parameter ensures the force remains continuous during velocity direction changes, which increases the numerical stability of the simulation. The parameter must be greater than zero. The default value is 1e-3 m/s.

## **Ports**

Port	Description
N	Physical signal input port that represents the normal force
Н	Conserving translational port that represents the wheel hub

## **See Also**

Tire (Friction Parameterized) | Tire (Magic Formula) | Tire-Road Interaction (Magic Formula)

# **Rope Drum**

Power transmission system with tightly wound rope around cylindrical drum



# Library

Couplings & Drives

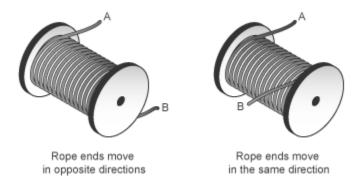
# **Description**

This block represents a power transmission system with two key components:

- Rope
- Drum

The rope is tightly wound around the cylindrical drum, at a sufficient tension level to prevent slipping between the two components. The rope can be wound such that its ends point in equal or opposite directions. Depending on the rope configuration, the two rope ends can move in equal or opposite directions. The rope windup types that you specify in the block dialog box are:

- If the rope ends point in the same direction, they translate in opposite directions.
- If the rope ends point in opposite directions, they translate in the same direction.



During normal operation, a driving torque causes the cylindrical drum to rotate about its symmetry axis. The rotating drum transmits a tensile force to the rope ends, which translate with respect to the drum centerline. The relative direction of translation between the two rope ends depends on the rope windup type. However, a positive drum rotation always corresponds to a positive translation at rope end A.

The rope drum model assumes that each rope end remains taut during simulation. This assumption is important since slack rope ends do not transmit force. An optional tension warning indicates the failure of this assumption. The warning, which appears at the MATLAB command prompt, prompts careful analysis of the simulation results.

Optional effects in the rope drum model include:

- Drum inertia
- · Viscous friction at the drum bearing

The net torque acting on the cylinder satisfies the force balance equation

$$T = F_B \cdot R \cdot \delta - F_A \cdot R + \mu \cdot \omega,$$

#### where:

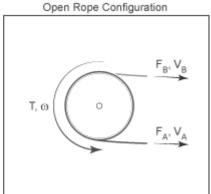
- *T* is the net torque acting on the drum.
- $F_{\rm A}$  and  $F_{\rm B}$  are the external forces pulling on rope ends A and B.
- R is the drum radius.
- $\mu$  is the viscous friction coefficient at the drum bearings.

- $\omega$  is the drum angular velocity.
- $\delta$  is the rope windup type according to the table.

Rope Windup Type  $\delta$  Ends move in the same direction -1 Ends move in opposite +1 directions

The figure shows the equation variables.

F<sub>A</sub>, V<sub>A</sub>



The translational velocities of the two rope ends are functions of the drum radius and angular velocity. Each translational velocity is equal to the tangential velocity of a point at the drum periphery according to the expressions:

$$\begin{aligned} V_A &= -\omega {\cdot} R, \\ V_B &= +\omega {\cdot} R, \end{aligned}$$

#### where:

- $V_{\rm A}$  is the translational velocity of rope end A.
- $V_{\rm B}$  is the translational velocity of rope end B.

## **Assumptions and Limitations**

- Slip does not occur at the rope-drum contact surface.
- Rope compliance is ignored.

## **Parameters**

## Rope Winding

#### Drum radius

Distance between the drum center and its periphery. The drum periphery coincides with the contact surface between the drum and the rope. The default value is  $0.1 \, \text{m}$ .

### Rope windup type

Relative direction of the translation motion of the two rope ends, A and B. Options include:

- The ends move in the same direction
- The ends move in opposite direction

### Tension warning

Optional warning at the MATLAB command line indicating that at least one rope end has become slack. A rope end becomes slack when the net tensile forces responsible for keeping it taut fall below zero. Since slack cables do not transmit force, you must interpret simulation results carefully if a tension warning appears at the MATLAB command line. Warning options include:

- Do not check rope tension
- Warn if either rope end loses tension

## **Drum Dynamics**

## Bearing viscous friction coefficient

Linear damping coefficient in effect at the drum bearing. At a given drum angular velocity, this coefficient determines the power losses due to viscous friction. The default value is  $0.001 \, (N*m)/(rad/s)$ .

#### Inertia

Optional parameter accounting for drum inertia, its resistance to angular acceleration. Options include:

- No inertia Default mode. Keep this mode if drum inertia has a negligible impact on driveline dynamics. Selecting this mode sets drum inertia to zero.
- Specify drum inertia and initial velocity Select this mode if drum inertia has a significant impact on driveline dynamics. Selecting this mode exposes additional parameters enabling you to specify the drum inertia and initial angular velocity.

#### Drum inertia

Moment of inertia of the drum about its rotation axis. In the simple case of a solid cylindrical drum, the moment of inertia is

$$I=\frac{1}{2}MR^2,$$

where M is the drum mass and R is the drum radius.

The default value of the drum inertia is 0.01 kg\*m^2.

## **Drum initial velocity**

Angular velocity of the drum at simulation time zero. The default value is 0 rad/s.

## **Ports**

Port	Description
S	Conserving rotational port associated with the drum shaft
A	Conserving translational port associated with rope end A
В	Conserving translational port associated with rope end B

# **Example**

To see how you can use the Rope Drum block in a model, open sdl\_power\_window.

# **See Also**

Wheel and Axle

# **Topics**

"Basic Motion, Torque, and Force Modeling"

## **Rotational Damper**

Faultable linear rotational damper

**Library:** Couplings & Drives / Springs & Dampers

RIC

## **Description**

The Rotational Damper block models a faultable linear rotational viscous damper. From the start of the simulation, the block uses the nominal damping coefficient. If you enable faults for the block, the damping coefficient changes in response to one or both of these triggers:

- Simulation time A fault occurs at a specified time.
- Simulation behavior If the magnitude of the rotational acceleration exceeds a
  specified maximum value, the block increments the number of shocks by one. A fault
  occurs if the number of shocks exceeds a specified maximum number of shocks.

If a fault trigger event occurs, the block uses the faulted damping coefficient for the remainder of the simulation. You can program the block to issue a fault report as a warning or error message.

The defining equations are

$$T = D\omega$$

and

$$\omega = \omega_R - \omega_C$$

where

- *T* is the torque transmitted through the damper.
- *D* is the damping (viscous friction) coefficient.
- $\omega$  is the relative velocity.

•  $\omega_R$  and  $\omega_C$  are the absolute velocities of terminals R and C, respectively.

The positive block direction is from port R to port C. Therefore, the torque is positive if it acts in the direction from R to C.

## **Ports**

## Conserving

#### R — Rod interface

mechanical rotational

Mechanical rotational conserving port associated with the rod interface.

#### C — Case interface

mechanical rotational

Mechanical rotational conserving port associated with the case interface.

## **Parameters**

#### Main

# Damping coefficient — Damping coefficient for the no-fault condition 1e-3 N\*m/(rad/s) (default)

The oscillation-reducing torque due to viscous friction that the block applies if no trigger event occurs. Specify a value that is greater than or equal to zero.

#### **Faults**

## Enable faults — Fault mode capability

No (default) | Yes

To enable the block to use a different damping coefficient based on the simulation time or when the magnitude of the rotational acceleration exceeds the specified number of shocks, select Yes.

#### **Dependencies**

Selecting Yes makes these parameters visible:

- Faulted damping coefficient
- Enable temporal fault trigger
- Enable behavioral fault trigger
- Reporting when fault occurs

# Faulted damping coefficient — Damping coefficient for the fault condition 100 N\*m/(rad/s) (default)

The oscillation-reducing torque due to viscous friction that the block applies if a trigger event occurs. Specify a value that is greater than or equal to zero.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

# **Enable temporal fault trigger — Fault trigger capability**Disabled (default) | Enabled

To enable the block to use the faulted damping coefficient starting at a specified time in the simulation, select Enabled.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

Selecting Enabled makes the Simulation time for fault event parameter visible.

# **Simulation time for fault event — Temporal fault trigger** 5 s (default)

Specify the time during the simulation that you want the block to start using the faulted damping coefficient.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter and **Enabled** for the **Enable temporal fault trigger** parameter.

# Enable behavioral fault trigger — Fault trigger capability Disabled (default) | Enabled

To use the faulted damping coefficient when the number of sustained shocks exceeds a specified maximum number of shocks, select Enabled.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

Selecting Enabled makes these parameters visible:

- Maximum permissible acceleration
- Maximum number of shocks

## Maximum permissible acceleration — Behavioral fault trigger

100 rad/s^2 (default)

The maximum value that the magnitude of the rotational acceleration can reach without causing the block to increment the number of sustained shocks.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter and **Enabled** for the **Enable behavioral fault trigger** parameter.

## Maximum number of shocks — Behavioral fault trigger

1 (default)

The maximum number of shocks that can be sustained without triggering the block to use the faulted damping coefficient.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter and **Enabled** for the **Enable behavioral fault trigger** parameter.

## Reporting when fault occurs — Fault reporting

None (default) | Warning | Error

Select your reporting preference for the fault condition.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

## **See Also**

Nonlinear Rotational Damper | Nonlinear Translational Damper | Translational Damper | Variable Rotational Damper | Variable Translational Damper

Introduced in R2016b

## **Rotational Detent**

Double-sided, spring-loaded rotational detent



## Library

Brakes & Detents/Rotational

## **Description**

The Rotational Detent block represents a double-sided, spring-loaded rotational detent.

The detent rod rotates over the detent case. The case has notches or magnets that create a net relative torque with the rod as the rod rotates. With the block, you can model rotational detents with peak torque and notch width, or with a lookup table. The model also includes viscous damping and kinetic friction between the rod and case. You can set the friction to zero.

## **Ports**

 ${f R}$  and  ${f C}$  are rotational conserving ports associated with the rod and case, respectively.

## **Parameters**

## **Detent Characteristics**

#### **Parameterization**

Select how to specify the detent characteristics. The default is By peak torque and notch width.

• By peak torque and notch width — Specify detent characteristics by the peak torque and the notch width.

#### **Peak Torque and Notch Width**

#### Peak torque

The peak torque developed inside the detent. The default is 0.25.

From the drop-down list, choose units. The default is newton-meters (N\*m).

#### Notch width

The width of the region where the torque develops. The default is 5.

From the drop-down list, choose units. The default is degrees (deg).

• By lookup table — Define the detent characteristics by one-dimensional table lookup based on the relative displacement between the slider and case. If you select this option, the panel changes from its default option.

#### **Lookup Table**

#### Relative rotation vector

Specify the vector of input relative rotations that correspond to the values in **Torque vector**. These two vectors must be of the same size. The angles must be specified in strictly increasing order. The default values are [-5.0 -4.0 -3.0 -1.0 3.0 4.0 5.0].

From the drop-down list, choose units. The default is degrees (deg).

#### Torque vector

Specify the vector of input values for the developed torque that correspond to the values in **Relative rotation vector**. The default values are  $[0\ 0\ -0.25\ -0.10\ 0.10\ 0.25\ 0\ 0]$ .

From the drop-down list, choose units. The default is newton-meters (N\*m).

#### Initial relative rotation

The relative angle of the rod and case when simulation starts. The default is  $\theta$ .

From the drop-down list, choose units. The default is degrees (deg).

### Interpolation method

Select one of these interpolation methods for approximating the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## **Spacing**

#### **Detent spacing**

Select how to specify the detent spacing. The default is Regularly spaced.

• Regularly spaced — Specify detent spacing by regular intervals.

#### Regular spacing

#### Number of detents

Specify the number of identical, regularly spaced detents. Must be greater than or equal to 1. The default is 1.

Creates a number of detents evenly spaced from -180 to +180 degrees, with one detent center at 0 degrees. Non-integer values are rounded to the nearest integer.

• By angle vector — Specify detent spacing by custom intervals. If you select this option, the panel changes from its default option.

#### **Custom intervals**

#### Vector of detent centers

Specify the locations of the centers of identical detents as a vector of angles. These values must lie between -180 and +180 degrees. The minimum spacing between the detents must be greater than the **Notch width** parameter. The default values are [-40 0 30 85].

From the drop-down list, choose units. The default is degrees (deg).

#### **Friction**

#### Viscous friction coefficient

Specify the viscous friction coefficient for the rod-case contact. Must be greater than or equal to 0. The default is 0.1.

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

#### Friction to peak torque ratio

Specify the kinetic friction coefficient for the rod-case contact. Must be greater than or equal to 0. The default is 0.01.

The kinetic friction is this ratio multiplied by the peak torque.

#### Friction velocity threshold

Specify the relative angular velocity required for peak kinetic friction in the detent. Must be greater than 0. The default is 10.

From the drop-down list, choose units. The default is revolutions/minute (rpm).

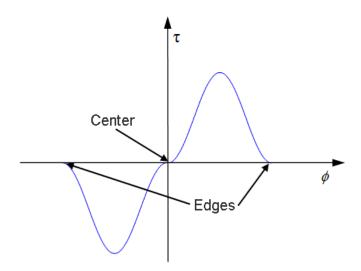
## **Rotational Detent Model**

As the rod rotates over the case, the relative rotation  $\phi = \phi_R - \phi_C$  causes a torque  $\tau$  to develop. Depending on your choice of parameterization, the torque model is defined by the peak torque and notch width, or by a lookup table specifying relative rotation versus torque.

Regardless of the parameterization, if you specify multiple detents, all detents have the same torque-relative rotation function.

## **Peak Torque and Notch Width**

If you choose the peak torque and notch width parameterization, the block ensures that the torque-relative rotation curve provides a continuous torque and torque derivative over the detent region. The peak torques are halfway between the detent center and detent edge, as shown in the following figure.



## **Lookup Table**

With the lookup table parameterization, you can create an arbitrary function relating torque to relative rotation. If you create such a function, consider the following best practices.

If you want to ensure that the detent conserves energy, the total integral of the torquerelative rotation curve (area under the curve) must be zero.

To stabilize simulation of the detent, avoid discontinuities in the torque-relative rotation function.

## **Limitations**

- The model does not account for inertia. Add inertia terms externally to the R and C ports as required.
- If you use the peak torque-notch width or the lookup table parameterization, the kinetic friction is independent of the detent normal force.

## See Also

Loaded-Contact Rotational Friction | Tire (Friction Parameterized) | Translational Detent

## **Topics**

"Clutches, Clutch-Like Elements, and Coulomb Friction"

## **Rotational Power Sensor**

Mechanical sensor used to measure average or instantaneous rotational power



## Library

Sensors

## **Description**

The block represents a sensor that measures the rotational power change due to one or more driveline components connected between ports R and C. The power output can be an instantaneous or average value. Three averaging options are available: period, vibration, and revolution averaging.

The instantaneous power is the product of the current angular velocity and torque. Use the instantaneous power to analyze peak power transmission and identify heavily loaded components.

The time-averaged power is the integral of the instantaneous power over one sample period, divided by that period. For simulation times smaller than the sample period, the average power is zero. The power output is constant for each sample period.

The vibration-averaged power is the integral of the power over one vibration period, divided by that period. The vibration period is the time between two consecutive crossings from negative to positive velocity values. If the vibration has a variable frequency, the averaging period can change. For simulation times smaller than the vibration period, the average power is zero. The power output is constant for each vibration period.

The revolution-averaged power is the integral of the instantaneous power over one revolution period, divided by that period. The revolution period is defined as the time between two consecutive crossings of zero angular position. If the revolution has a variable frequency, the averaging period can change. For simulation times smaller than the revolution period, the average power is zero. The power output is constant for each revolution period.

## **Parameters**

#### **Measurement Type**

Select either instantaneous or average power measurement. The default type is Instantaneous Power.

- Instantaneous power Output the rotational power measured for the current simulation time step.
- Average power over a specified period Output the rotational power averaged over a fixed time period.

#### Averaging period

Enter the time period used to compute the average power. Typical values include the cycle length of a rotating device.

The default value is 1. The default unit is s.

 Average power over a vibration — Output the rotational power averaged over one vibration period.

### Maximum vibration frequency

Enter the maximum vibration frequency over which to average the rotational power. Very high values can reduce simulation speed. Very low values can result in lower power measurements.

The default value is 1000. The default unit is Hz.

• Average power over a revolution — Output the rotational power averaged over one revolution period.

#### Maximum rotational speed

Enter the maximum speed over which to average the rotational power. Very high values can reduce simulation speed. Very low values can result in lower power measurements.

The default value is 1000. The default unit is rpm.

## **Ports**

Port	Description
P	Physical signal output port for rotational power
S	Rotational conserving port associated with driving source
R	Rotational conserving port associated with loaded driveline components
С	Rotational conserving port associated with case holding loaded driveline components

## **See Also**

Translational Power Sensor

#### Introduced in R2013a

## **Rotational Velocity Noise Source**

Produce zero-mean normally (Gaussian) distributed rotational velocity **Library:** Sources



## **Description**

The Rotational Velocity Source block generates zero-mean normally (Gaussian) distributed rotational velocity using the Random Number source in the Simscape Foundation library. The rotational velocity produced by the block depends on two factors:

- The noise power spectral density input to the block
- A random number seed that you control using the Repeatability and, as applicable,
   Seed parameters

The defining equation for the rotational velocity that the block generates is

$$v = \sqrt{PSD/2} \frac{N(0,1)}{\sqrt{h}},$$

#### where:

- *v* is the output rotational velocity.
- PSD is the single-sided noise power spectral density.
- N is a Gaussian random number with zero mean and standard deviation of one.
- *h* is the sampling interval.

## **Ports**

## Input

#### P - Single-sided noise power spectral density

physical signal

The power spectral density (PSD) of noise is the average noise power per unit of bandwidth, in  $(rad/s)^2/Hz$ .

## Conserving

#### **B** — Base interface

mechanical rotational

Mechanical rotational conserving port associated with the base interface.

#### F — Follower interface

mechanical rotational

Mechanical rotational conserving port associated with the follower interface.

## **Parameters**

### Sample time — Time step period and offset

1e-3 s (default) | [step, offset] s

The values of the time step period and the initial time offset. If you specify a scalar value for step, the block assumes an offset value of 0. To specify a nonzero value for the initial time offset, specify the parameter values using the vector [step, offset]. The offset value must be less than the step value and greater than or equal to zero.

### Repeatability — Random number seed control

Not repeatable (default) | Repeatable | Specify seed

The random number seed is the number that initializes the random number generator. The seed is  $\theta$  or a positive integer. To control the random number seed, set this parameter to:

• Not repeatable — The seed changes every time you simulate your model. The block resets the random seed using the MATLAB random number generator command:

```
seed = randi(2^32-1);
```

Repeatable — The seed is the same random number at the start of every simulation.
 The block sets the value using the same MATLAB random number generator command used by the Not repeatable parameter.

When you add a Rotational Velocity Noise Source block to your model from the Sources library, the block generates and stores a random value for the repeated seed. When you make a copy of the Rotational Velocity Noise Source block from an existing block in a model, the copy generates a new random value for the repeated seed.

Specify seed — The seed is a number that you specify using the Seed parameter.
 The Seed parameter is only available when you choose Specify seed for the Repeatability parameter.

## Seed — Random number generation seed value

0 (default)

The seed must be 0 or a positive integer. This parameter is only available when you select Specify seed for the **Repeatability** parameter.

## See Also

### **Simscape Blocks**

Force Noise Source | Random Number | Sinusoidal Rotational Velocity Source | Torque Noise Source | Translational Velocity Noise Source

#### **Functions**

randi

#### Introduced in R2016b

## **Shock Absorber**

Mechanism for damping translational vibrations

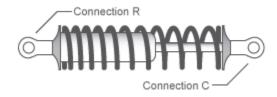


## Library

Simscape / Driveline / Couplings & Drives

## **Description**

The Shock Absorber block represents a spring-damper system commonly used to dampen vibration in mechanical systems. An internal force acts between ports R and C. This force is the sum of spring stiffness, damping, Coulomb friction, and hard-stop contributions. All force contributions are optional.



The Shock Absorber block uses the models of these blocks:

Block	Contribution	Library
Loaded-Contact Translational Friction	Coulomb friction	Simscape / Driveline / Brakes & Detents / Translational
Rotational Damper	Damping	Simscape / Foundation
Rotational Spring	Spring	Library / Mechanical / Translational Elements

Block	Contribution	Library
Rotational Hard Stop	Hard stop	

## **Assumptions and Limitations**

• Including hard-stop and Coulomb friction enhances model fidelity, but reduces simulation speed. For more information, see "Driveline Simulation Performance".

### **Ports**

## Conserving

C

Mechanical translational port associated with the slider that travels between stops installed on the case.

R

Mechanical translational port associated with the rod.

## **Parameters**

## **Spring-Damper**

### **Restoring spring stiffness**

Enter the value of the viscous spring stiffness constant, k. The default value is 1e4 N/m. The value must be greater than or equal to zero.

#### Viscous friction coefficient

Enter the value of the viscous damping constant, b. The default value is 1e2 m/s. The value must be greater than or equal to zero.

#### Coulomb friction force

Enter the value of the Coulomb friction force. Setting the value to  $\theta$  eliminates the Coulomb friction force contribution. This enhances simulation speed, making the model more suitable for HIL testing. The default value is  $\theta$  N. The value must be greater than or equal to zero.

#### Ratio of static to kinetic friction

Enter the value of the static/kinetic friction ratio, that is  $F_s/F_k$ . The value must be greater than one. The default value is 1.1. The value must be greater than or equal to one.

#### **Velocity tolerance**

Enter the value of the relative velocity below which ports R and C lock and translate together. The default value is  $0.001 \, \text{m/s}$ . The value must be greater than zero.

## **Hard Stops**

#### Hard stop

Include or exclude hard-stop force by selecting one of these options:

- No hard stops Suitable for HIL simulation To enhance simulation speed by excluding the hard-stop force contribution, select this default option.
- Compliant hard stops To enhance model fidelity by including the hard-stop force contribution, select this option. Selecting this option enables other parameters.

### Upper bound

Upper hard-stop position, UB. Positive displacement beyond the upper bound activates the hard-stop contact force. The default value is  $0.1\,\text{m}$ . The value must be greater than the lower bound.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

#### Lower bound

Lower hard-stop position, LB. Negative displacement beyond the lower bound activates the hard-stop contact force. The default value is  $-0.1 \, \text{m}$ . The value must be smaller than the upper bound.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

#### **Contact stiffness**

Enter the value of the hard-stop stiffness constant,  $k_{HS}$ . The default value is 1e6 N/m. The value must be greater than or equal to zero.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

### **Contact damping**

Enter the value of the hard-stop damping constant,  $b_{HS}$ . This parameter specifies dissipating property of colliding bodies. The greater the value of the parameter, the more energy dissipates during an interaction. The default value is 1e4 N/(m/s). The value must be greater than zero.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

#### Hard stop model

Select the hard-stop model:

 Stiffness and damping applied smoothly through transition region, damped rebound — Specify a transition region, in which the force is scaled from zero. At the end of the transition region, the full stiffness and damping are applied. This model has damping applied on the rebound, but it is limited to the value of the stiffness force. In this sense, damping can reduce or eliminate the force provided by the stiffness, but never exceed it. All equations are smooth and produce no zero crossings.

Selecting this option enables the Transition region parameter.

- Full stiffness and damping applied at bounds, undamped rebound
   — This model has full stiffness and damping applied with impact at upper and lower bounds, with no damping on the rebound. Equations produce no zero crossings when velocity changes sign, but there is a position-based zero crossing at the bounds. Having no damping on rebound helps to push the slider past this position quickly. This model has nonlinear equations.
- Full stiffness and damping applied at bounds, damped rebound —
   This model has full stiffness and damping applied with impact at upper and lower
   bounds, with damping applied on the rebound as well. Equations are switched
   linear, but produce position-based zero crossings. Use this hard-stop model if
   simscape.findNonlinearBlocks indicates that this is the block that prevents
   the whole network from being switched linear.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

#### **Transition region**

Region where the force is ramped up from zero to the full value. At the end of the transition region, the full stiffness and damping are applied. The default value is  $0.1\,$ mm.

Selecting Stiffness and damping applied smoothly through transition region, damped rebound for the **Hard stop model** enables this parameter.

#### **Initial Conditions**

#### **Initial deformation**

Enter the initial value of the spring deformation. The default value is 0 m.

## **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Hard Stops** > **Hard stop** parameter default setting, No hard stops - Suitable for HIL simulation.

## **See Also**

### **Simscape Blocks**

Nonlinear Translational Damper | Nonlinear Translational Spring | Rotational Hard Stop | Variable Translational Damper | Variable Translational Spring

## **Topics**

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Simple Gear**

Simple gear of base and follower wheels with adjustable gear ratio and friction losses



## Library

Simscape / Driveline / Gears

## **Description**

The Simple Gear block represents a gearbox that constrains the two connected driveline axes, base (B) and follower (F), to corotate with a fixed ratio that you specify. You can choose whether the follower axis rotates in the same or opposite direction as the base axis. If they rotate in the same direction,  $\omega_F$  and  $\omega_B$  have the same sign. If they rotate in opposite directions,  $\omega_F$  and  $\omega_B$  have opposite signs. For model details, see "Simple Gear Model" on page 1-342.

## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Simple Gear Model**

#### **Ideal Gear Constraint and Gear Ratio**

Simple Gear imposes one kinematic constraint on the two connected axes:

$$r_{\rm F}\omega_{\rm F}=r_{\rm B}\omega_{\rm B}$$
.

The follower-base gear ratio  $g_{\rm FB} = r_{\rm F}/r_{\rm B} = N_{\rm F}/N_{\rm B}$ . N is the number of teeth on each gear. The two degrees of freedom reduce to one independent degree of freedom.

The torque transfer is:

$$g_{\rm FB}\tau_{\rm B} + \tau_{\rm F} - \tau_{\rm loss} = 0$$
,

with  $\tau_{loss} = 0$  in the ideal case.

#### **Nonideal Gear Constraint and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . For general considerations on nonideal gear modeling, see "Model Gears with Losses".

In a nonideal gear pair (B,F), the angular velocity, gear radii, and gear teeth constraints are unchanged. But the transferred torque and power are reduced by:

- Coulomb friction between teeth surfaces on gears B and F, characterized by efficiency  $\eta$
- Viscous coupling of drives hafts with bearings, parametrized by viscous friction coefficients  $\mu$

In the constant efficiency case,  $\eta$  is constant, independent of load or power transferred.

In the load-dependent efficiency case,  $\eta$  depends on the load or power transferred across the gears. For either power flow,  $\tau_{\text{Coul}} = g_{\text{FB}}\tau_{\text{idle}} + k\tau_{\text{F}}$ . k is a proportionality constant.  $\eta$  is related to  $\tau_{\text{Coul}}$  in the standard, preceding form but becomes dependent on load:

$$\eta = \tau_{\rm F}/[g_{\rm FB}\tau_{\rm idle} + (k+1)\tau_{\rm F}] \; . \label{eq:eta_fb}$$

## Limitations

- Gear inertia is assumed negligible.
- · Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
В	Rotational conserving port representing the base shaft
F	Rotational conserving port representing the follower shaft
Н	Thermal conserving port for thermal modeling

## **Parameters**

### Main

### Follower (F) to base (B) teeth ratio (NF/NB)

Fixed ratio  $g_{\rm FB}$  of the follower axis to the base axis. The gear ratio must be strictly positive. The default is 2.

### **Output shaft rotates**

Direction of motion of the follower (output) driveshaft relative to the motion of the base (input) driveshaft. The default is In opposite direction to input shaft.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### Friction model

List of friction models at various precision levels for estimating power losses due to meshing.

- No meshing losses Suitable for HIL simulation Neglect friction between gear cogs. Meshing is ideal.
- Constant efficiency Reduce torque transfer by a constant efficiency factor. This factor falls in the range  $0 < \eta \le 1$  and is independent of load. Selecting this option exposes additional parameters.

#### **Constant efficiency**

#### **Efficiency**

Torque transfer efficiency  $(\eta)$  between base and follower shafts. This parameter is inversely proportional to the meshing power losses. Values can range from 0 to 1. The default value is 0.95.

• Load-dependent efficiency — Reduce torque transfer by a variable efficiency factor. This factor falls in the range  $0 < \eta < 1$  and varies with the torque load. Selecting this option exposes additional parameters.

### **Load-Dependent Efficiency**

### Input shaft torque at no load

Net torque  $(\tau_{idle})$  acting on the input shaft in idle mode, e.g., when torque transfer to the output shaft equals zero. For nonzero values, the power input in idle mode completely dissipates due to meshing losses. The default value is  $0.1~\mathrm{N*m}$ .

### Nominal output torque

Output torque  $(\tau_F)$  at which to normalize the load-dependent efficiency. The default value is 5 N\*m.

### Efficiency at nominal output torque

Torque transfer efficiency ( $\eta$ ) at the nominal output torque. Efficiency values must fall in the interval [0, 1]. Larger efficiency values correspond to greater torque transfer between the input and output shafts. The default value is 0.95.

## Follower angular velocity threshold

Absolute value of the follower shaft angular velocity above which the full efficiency factor is in effect ( $\omega_F$ ). Below this value, a hyperbolic tangent

function smooths the efficiency factor to one, lowering the efficiency losses to zero when at rest.

As a guideline, the angular velocity threshold should be lower than the expected angular velocity during simulation. Higher values might cause the block to underestimate efficiency losses. Very low values might, however, raise the computational cost of simulation.

The default value is 0.01 rad/s.

#### With Thermal Port

#### Friction model

Choice of model for representing friction. The model can incorporate the temperature and load dependences of friction or just the temperature dependence. The default setting is Temperature-dependent efficiency.

#### **Temperature**

Array of temperatures used to construct an efficiency lookup table. The array values must increase from left to right. The temperature array must be the same size as the efficiency array in temperature-dependent models. It must be the same size as a single row of the efficiency matrix in temperature-and-load-dependent models. The default array is [280 300 320] K.

### Load at base gear

Array of base-gear loads used to construct a 2-D temperature-load-efficiency lookup table for temperature-and-load-dependent efficiency models. The array values must increase left to right. The load array must be the same size as a single column of the efficiency matrix. The default array is [1 5 10] N\*m.

### **Efficiency**

Array of efficiencies used to construct a 1-D temperature-efficiency lookup table for temperature-dependent efficiency models. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size.

This parameter appears only when you select a temperature-dependent friction model. The default array is [0.95 0.9 0.85].

### Efficiency matrix

Matrix of component efficiencies used to construct a 2-D temperature-load-efficiency lookup table. The matrix elements are the efficiencies at the temperatures given by the **Temperature** array and at the loads given by the **Load at base gear** array.

The number of rows must be the same as the number of elements in the **Temperature** array. The number of columns must be the same as the number of elements in the **Load at base gear** array.

This parameter appears only when you select a temperature-and-load-dependent efficiency model. The default matrix is [0.85 0.8 0.75; 0.95 0.9 0.85; 0.85 0.8 0.71.

#### Follower power threshold

Visible only if you select Temperature-dependent efficiency as the friction model. Absolute value of the follower shaft power above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero when at rest and the value provided by the temperature-efficiency lookup table when at the power threshold. The default value is 0.001 W.

#### Follower angular velocity threshold

Visible only if you select Temperature and load-dependent efficiency as the friction model. Absolute value of the follower shaft angular velocity above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor to one, lowering the efficiency losses to zero when at rest. The default value is  $0.01 \, \mathrm{rad/s}$ .

### **Viscous Losses**

### Viscous friction coefficients at base (B) and follower (F)

Two-element array with the viscous friction coefficients in effect at the base and follower shafts. The default array,  $[0 \ 0]$ , corresponds to zero viscous losses.

## **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

## **Extended Capabilities**

## **Real-Time and Hardware-in-the-Loop Simulation**

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

#### **Simscape Blocks**

Variable Ratio Transmission

## **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Gearbox Efficiency Measurement"
- "Simple Gear"
- "Gear with Backlash"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Simple Gear with Variable Efficiency**

Gear set with parallel-axis rotation and variable meshing efficiency



## Library

Gears

## **Description**

The block represents a simple gear train with variable meshing efficiency. The gear train transmits torque at a specified ratio between base and follower shafts arranged in a parallel configuration. Shaft rotation can occur in equal or opposite directions. Gear losses are optional. They include meshing and viscous bearing losses. To specify the variable meshing efficiency, the block contains a physical signal port that you can use to input a general time-varying signal. Inertia and compliance effects are ignored.

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Specify the associated thermal parameters for the component.

## **Parameters**

## Main

### Follower (F) to base (B) teeth ratio (NF/NB)

Enter the gear ratio. This is the fraction of follower over base gear teeth numbers, NF/NB. The ratio must be positive. The default value is 2.

#### **Output shaft rotates**

Select the relative rotation between shafts. This is the rotation direction of the output shaft with respect to the input shaft. Options include equal or opposite directions. The default setting is In opposite direction to input shaft.

## **Meshing Losses**

#### Minimum efficiency

Enter the smallest efficiency value allowed for the gear. The efficiency is the power ratio between output and input shafts. The physical signal input saturates for values below the minimum efficiency or above 1. The minimum efficiency must be positive. The default value is 0.01.

#### Follower power threshold

Enter the follower shaft power above which full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero when at rest and the value provided by the temperature-efficiency lookup table when at the power threshold. The default value is  $0.001\,\mathrm{W}$ .

## **Viscous Losses**

### Viscous friction coefficients at base (B) and follower (F)

Enter a two-element vector with the viscous friction coefficients of the base and follower gears. Coefficients must be positive. The default vector is  $[0 \ 0]$ . The default unit is N\*m/(rad/s).

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### Initial temperature

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

## Simple Gear Model

#### **Ideal Gear Constraint and Gear Ratio**

Simple Gear imposes one kinematic constraint on the two connected axes:

$$r_{\rm F}\omega_{\rm F}=r_{\rm B}\omega_{\rm B}$$
.

The follower-base gear ratio  $g_{\rm FB} = r_{\rm F}/r_{\rm B} = N_{\rm F}/N_{\rm B}$ . N is the number of teeth on each gear. The two degrees of freedom reduce to one independent degree of freedom.

The torque transfer is:

$$g_{\rm FB}\tau_{\rm B}+\tau_{\rm F}-\tau_{\rm loss}=0\;,$$

with  $\tau_{loss} = 0$  in the ideal case.

#### **Nonideal Gear Constraint and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . For general considerations on nonideal gear modeling, see "Model Gears with Losses".

## Limitations

- Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

### **Ports**

Port	Description
В	Rotational conserving port representing the base shaft
F	Rotational conserving port representing the follower shaft
Н	Thermal conserving port for thermal modeling

## **See Also**

Simple Gear | Variable Ratio Transmission

## **Topics**

"Basic Motion, Torque, and Force Modeling"

## **Sinusoidal Force Source**

Produce sinusoidal force **Library:** Sources



## **Description**

The Sinusoidal Force Source block produces sinusoidal force with a constant offset. A positive force value generates force acting from port B to port F.

The defining equation for the sinusoidal force that the block generates is

$$F = F_o + A * \sin(2\pi f t + \varphi),$$

#### where:

- *F* is the output force.
- $F_o$  is the offset force of the output.
- A is the peak amplitude of the sinusoid.
- f is frequency of the sinusoid in Hz.
- t is time.
- $\phi$  is phase shift of the sinusoid.

## **Ports**

## Conserving

#### **B** — Base interface

mechanical translational

Mechanical translational conserving port associated with the base interface.

#### F — Follower interface

mechanical translational

Mechanical translational conserving port associated with the follower interface.

## **Parameters**

#### Offset — Output average value

0 N (default)

Average value that the output sinusoidal force oscillates about.

### Sinusoid peak amplitude — Output peak amplitude

1 N (default)

Peak amplitude of the output sinusoidal force.

#### Phase shift — Output phase shift

0 deg (default)

Phase shift of the output sinusoidal force.

### Frequency — Output frequency

1 Hz (default)

Frequency of the output sinusoidal force. The frequency must be greater than or equal to 0.

## See Also

Force Noise Source | Sinusoidal Translational Velocity Source | Sinusoidal Rotational Velocity Source | Sinusoidal Torque Source

#### Introduced in R2016b

# **Sinusoidal Rotational Velocity Source**

Produce sinusoidal rotational velocity **Library:** Sources



# **Description**

The Sinusoidal Rotational Velocity Source block produces sinusoidal rotational velocity with a constant offset.

The relative rotational velocity between the base and follower interfaces is

$$v_{FB} = v_F - v_B,$$

#### where:

- $v_{FB}$  is the relative rotational velocity.
- $v_F$  is the absolute rotational velocity at the follower interface.
- $v_B$  is the absolute rotational velocity at the base interface.

The defining equation for the sinusoidal rotational velocity that the block generates is

$$v = v_o + A * \sin(2\pi f t + \varphi),$$

#### where:

- *v* is the output rotational velocity.
- $v_o$  is the offset rotational velocity of the output.
- ullet A is the peak amplitude of the sinusoid.
- *f* is frequency of the sinusoid in Hz.
- t is time.
- $\phi$  is phase shift of the sinusoid.

## **Ports**

## **Conserving**

#### **B** — Base interface

mechanical rotational

Mechanical rotational conserving port associated with the base interface.

#### F — Follower interface

mechanical rotational

Mechanical rotational conserving port associated with the follower interface.

## **Parameters**

### Offset — Output average value

0 rad/s (default)

Average value that the output sinusoidal rotational velocity oscillates about.

## Sinusoid peak amplitude — Output peak amplitude

1 rad/s (default)

Peak amplitude of the output sinusoidal rotational velocity.

## Phase shift — Output phase shift

0 deg (default)

Phase shift of the output sinusoidal rotational velocity.

## Frequency — Output frequency

1 Hz (default)

Frequency of the output sinusoidal rotational velocity. The frequency must be greater than or equal to 0.

# **See Also**

Rotational Velocity Noise Source | Sinusoidal Translational Velocity Source | Sinusoidal Force Source | Sinusoidal Torque Source

Introduced in R2016b

# **Sinusoidal Torque Source**

Produce sinusoidal torque **Library:** Sources



# **Description**

The Sinusoidal Torque Source block produces sinusoidal torque with a constant offset. A positive torque value generates torque acting from port B to port F.

The defining equation for the sinusoidal torque that the block generates is

$$T = T_o + A * \sin(2\pi f t + \varphi),$$

#### where:

- T is the output torque.
- $T_o$  is the offset torque of the output.
- *A* is the peak amplitude of the sinusoid.
- f is frequency of the sinusoid in Hz.
- t is time.
- $\phi$  is phase shift of the sinusoid.

# **Ports**

# Conserving

#### **B** — Base interface

mechanical rotational

Mechanical rotational conserving port associated with the base interface.

#### F — Follower interface

mechanical rotational

Mechanical rotational conserving port associated with the follower interface.

## **Parameters**

### Offset — Output average value

0 N\*m (default)

Average value that the sinusoidal output torque oscillates about.

### Sinusoid peak amplitude — Output peak amplitude

1 N\*m (default)

Peak amplitude of the sinusoidal output torque.

### Phase shift — Output phase shift

0 deg (default)

Peak amplitude of the sinusoidal output torque.

### Frequency — Output frequency

1 Hz (default)

Frequency of the sinusoidal output torque. The frequency must be greater than or equal to 0.

# **See Also**

Sinusoidal Force Source | Sinusoidal Rotational Velocity Source | Sinusoidal Translational Velocity Source | Torque Noise Source

#### Introduced in R2016b

# **Sinusoidal Translational Velocity Source**

Produce sinusoidal translational velocity **Library:** Sources



# **Description**

The Sinusoidal Translational Velocity Source block produces sinusoidal translational velocity with a constant offset.

The relative translational velocity between the base and follower interfaces is

$$v_{FB} = v_F - v_B,$$

#### where:

- $v_{FB}$  is the relative translational velocity.
- $v_F$  is the absolute translational velocity at the follower interface.
- $v_B$  is the absolute translational velocity at the base interface.

The defining equation for the sinusoidal translational velocity that the block generates is

$$v = v_o + A * \sin(2\pi f t + \varphi),$$

#### where:

- v is the output translational velocity.
- $v_o$  is the offset translational velocity of the output.
- A is the peak amplitude of the sinusoid.
- *f* is frequency of the sinusoid in Hz.
- t is time.
- $\phi$  is phase shift of the sinusoid.

# **Ports**

## Conserving

#### **B** — Base interface

mechanical translational

Mechanical translational conserving port associated with the base interface.

#### F — Follower interface

mechanical translational

Mechanical translational conserving port associated with the follower interface.

### **Parameters**

### Offset — Output average value

0 m/s (default)

Average value that the output sinusoidal translational velocity oscillates about.

## Sinusoid peak amplitude — Output peak amplitude

1 m/s (default)

Peak amplitude of the output sinusoidal translational velocity.

## Phase shift — Output phase shift

0 deg (default)

Phase shift of the output sinusoidal translational velocity

## Frequency — Output frequency

1 Hz (default)

Frequency of the output sinusoidal translational velocity. The frequency must be greater than or equal to 0.

# **See Also**

Sinusoidal Force Source | Sinusoidal Rotational Velocity Source | Sinusoidal Torque Source | Translational Velocity Noise Source

Introduced in R2016b

# **Sun-Planet**

Planetary gear set of carrier, planet, and sun wheels with adjustable gear ratio and friction losses



# Library

Simscape / Driveline / Gears / Planetary Subcomponents

# **Description**

The Sun-Planet gear block represents a set of carrier, planet, and sun gear wheels. The planet is connected to and rotates with respect to the carrier. The planet and sun corotate with a fixed gear ratio that you specify and in the same direction with respect to the carrier. A sun-planet and a ring-planet gear are basic elements of a planetary gear set. For model details, see "Sun-Planet Gear Model" on page 1-363.

## Thermal Modeling

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Sun-Planet Gear Model**

### **Ideal Gear Constraints and Gear Ratios**

Sun-Planet imposes one kinematic and one geometric constraint on the three connected axes:

$$r_{\rm C}\omega_{\rm C}=r_{\rm S}\omega_{\rm S}+r_{\rm P}\omega_{\rm P}$$
 ,  $r_{\rm C}=r_{\rm P}+r_{\rm S}$  .

The planet-sun gear ratio  $g_{PS} = r_P/r_S = N_P/N_S$ . N is the number of teeth on each gear. In terms of this ratio, the key kinematic constraint is:

$$\omega_{\rm S} = -g_{\rm PS}\omega_{\rm P} + (1 + g_{\rm PS})\omega_{\rm C}$$
.

The three degrees of freedom reduce to two independent degrees of freedom. The gear pair is (1,2) = (S,P).

**Warning** The planet-sun gear ratio  $g_{PS}$  must be strictly greater than one.

The torque transfer is:

$$g_{\rm PS}\tau_{\rm S}+\tau_{\rm P}-\tau_{\rm loss}=0$$
 ,

with  $\tau_{loss} = 0$  in the ideal case.

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$  . See "Model Gears with Losses".

## Limitations

- Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port representing the planet carrier
P	Rotational conserving port representing the planet gear
S	Rotational conserving port representing the sun gear
Н	Thermal conserving port for thermal modeling

## **Parameters**

#### Main

### Ring (R) to sun (S) teeth ratio (NP/NS)

Ratio  $g_{\rm RS}$  of the ring gear wheel radius to the sun gear wheel radius. This gear ratio must be strictly greater than 1. The default value is 2.

## **Meshing Losses**

Parameters for meshing losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### Friction model

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

### Constant Efficiency

#### **Ordinary efficiency**

Torque transfer efficiency  $\eta_{SP}$  for sun-planet gear wheel pair meshing.

### Sun-carrier power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default value is  $0.001 \ W$ .

#### With Thermal Port

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

#### **Efficiency**

Array of component efficiencies used to construct a 1-D temperature-efficiency lookup table. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.95 0.9 0.85].

### Sun-carrier power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is  $0.001 \, \text{W}$ .

### **Viscous Losses**

#### Sun-carrier viscous friction coefficient

Viscous friction coefficient  $\mu_S$  for the sun-carrier gear motion. The default is 0.

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

## **Simscape Blocks**

Compound Planetary Gear | Planet-Planet | Planetary Gear | Ring-Planet | Sun-Planet Bevel

## **Topics**

"Basic Motion, Torque, and Force Modeling"

"Model Thermal Losses in Driveline Components"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Sun-Planet Bevel**

Planetary gear set of carrier, beveled planet, and sun wheels with adjustable gear ratio, assembly orientation, and friction losses



# Library

Simscape / Driveline / Gears / Planetary Subcomponents

# **Description**

The Sun-Planet Bevel gear block represents a set of carrier, planet, and sun gear wheels. The planet is connected to and rotates with respect to the carrier. The planet and sun corotate with a fixed gear ratio. You control the direction of rotation by setting the assembly orientation, left or right. A sun-planet and a ring-planet gear are basic elements of a planetary gear set. For model details, see "Sun-Planet Bevel Gear Model" on page 1-368.

# Thermal Modeling

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Sun-Planet Bevel Gear Model**

### **Ideal Gear Constraints and Gear Ratios**

Sun-Planet Bevel imposes one kinematic and one geometric constraint on the three connected axes.

$$r_C \omega_C = r_S \omega_S \pm r_P \omega_P$$

$$r_C = r_S \pm r_P$$

Where:

- $r_C$  is the radius of the carrier gear.
- $\omega_C$  is the angular velocity of the carrier gear.
- $r_S$  is the radius of the sun gear.
- $\omega_S$  is the angular velocity of the sun gear.
- $r_P$  is the radius of the planet gear.
- $\omega_P$  is the angular velocity of the planet gear.

The planet-sun gear ratio is defined as

$$g_{PS} = \frac{r_P}{r_S} = \frac{N_P}{N_S},$$

where:

- $g_{PS}$  is the planet-sun gear ratio. As  $r_P > r_S$  ,  $g_{PS} > 1$  .
- $N_P$  is the number of teeth in the planet gear.
- $N_S$  is the angular velocity of the sun gear.

In terms of this ratio, the key kinematic constraint is:

•  $\omega_S = g_{PS}\omega_P - \omega_C$  for a left-oriented bevel assembly

•  $\omega_S = g_{PS}\omega_P + \omega_C$  for a right-oriented bevel assembly

The three degrees of freedom reduce to two independent degrees of freedom. The gear pair is (1,2) = (S,P).

**Warning** The planet-sun gear ratio,  $g_{PS}$ , must be strictly greater than one.

The torque transfer is defined as

$$\tau_P = \tau_{loss} - g_{PS} \tau_S,$$

where:

- $\tau_{loss}$  is the torque loss.
- $\tau_s$  is the torque for the sun gear.
- $\tau_p$  is the torque for the planet gear.

For the ideal case, there is no torque loss, that is  $\tau_{loss} = 0$ . Then the torque transfer equation is  $\tau_P = g_{PS} \tau_S$ .

## **Nonideal Gear Constraints and Losses**

In the nonideal case,  $\tau_{loss} \neq 0$ . See "Model Gears with Losses".

# Limitations

- Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port representing the gear carrier
P	Rotational conserving port representing the planet gear
S	Rotational conserving port representing the sun gear
Н	Thermal conserving port for thermal modeling

# **Parameters**

### Main

### Planet (P) to sun (S) teeth ratio (NP/NS)

Ratio  $g_{PS}$  of the planet gear wheel radius to the sun gear wheel radius. This gear ratio must be strictly greater than 1. The default value is 2.

## **Assembly orientation**

Relative orientation of sun and planet gears, controlling their corotation direction. Left or right orientation imply, respectively, that the gears corotate in the same or opposite direction.

The default is Left  $\,-\,$  Sun and planet gears rotate in same direction.

# **Meshing Losses**

Parameters for meshing and friction losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear teeth. The default is No meshing losses.

- No meshing losses Suitable for HIL simulation Gear meshing is ideal
- Constant efficiency Transfer of torque between gear wheel pairs is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

### **Constant Efficiency**

### **Ordinary efficiency**

Torque transfer efficiency  $\eta_{\rm SP}$  for sun-planet gear wheel pair meshing.

### Sun-carrier power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default value is  $0.001\,\mathrm{W}$ .

#### **With Thermal Port**

### Temperature

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

### **Efficiency**

Array of component efficiencies used to construct a 1-D temperature-efficiency lookup table. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.95 0.9 0.85].

### Sun-carrier power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is 0.001 W.

### Viscous Losses

#### Sun-carrier viscous friction coefficient

Viscous friction coefficient  $\mu_S$  for the sun-carrier gear motion. The default is 0.

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Meshing Losses** > **Friction model** parameter default setting, No meshing losses - Suitable for HIL simulation.

## See Also

## Simscape Blocks

Differential | Planet-Planet | Planetary Gear | Ring-Planet | Sun-Planet | Sun-Planet Worm Gear

### **Topics**

"Basic Motion, Torque, and Force Modeling"

"Limited Slip Differential with Clutches"

<sup>&</sup>quot;Custom Planetary Gear"
"Model Thermal Losses in Driveline Components"
"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Sun-Planet Worm Gear**

Planetary gear set of carrier, worm planet, and sun wheels with adjustable gear ratio, worm thread type, and friction losses

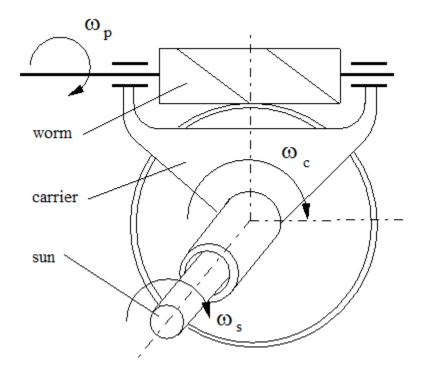


# Library

Simscape / Driveline / Gears / Planetary Subcomponents

# **Description**

The Sun-Planet Worm Gear block represents a two-degree-of-freedom planetary gear built from carrier, sun, and planet gears. By type, the sun and planet gears are crossed helical spur gears arranged as a worm-gear transmission, in which the planet gear is a worm. Such transmissions are used in the Torsen type 1 differential. When transmitting power, the sun gear can be independently rotated by the worm (planet) gear, or by the carrier, or both.



You specify a fixed gear ratio, which is determined as the ratio of the worm angular velocity to the sun gear angular velocity. You control the direction by setting the worm thread type, left-handed or right-handed. Rotation of the right-handed worm in positive direction causes the sun gear to rotate in positive direction too. The positive directions of the sun gear and the carrier are the same.

## **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Sun-Planet Worm Gear Model**

# **Model Variables**

$R_{ m WG}$	Gear, or transmission, ratio determined as the ratio of the worm angular velocity to the gear angular velocity.  The ratio is positive for the right-hand worm and negative for the left-hand worm.
$\omega_{ ext{S}}$	Angular velocity of the sun gear
$\omega_{ ext{P}}$	Planet (that is, worm) angular velocity
$\omega_{ m C}$	Carrier angular velocity
$\omega_{ ext{SC}}$	Angular velocity of the sun with respect to the carrier
α	Normal pressure angle
λ	Worm lead angle
L	Worm lead
d	Worm pitch diameter
$ au_{ m S}$	Torque applied to the sun shaft
$ au_{ m P}$	Torque applied to the planet shaft
$ au_{ m C}$	Torque applied to the carrier shaft
$ au_{ m loss}$	Torque loss due to meshing friction. The loss depends on the device efficiency and the power flow direction. To avoid abrupt change of the friction torque at $\omega_S = 0$ , the friction torque is introduced via the hyperbolic function.
$ au_{ ext{instfr}}$	Instantaneous value of the friction torque added to the model to simulate friction losses
$ au_{ m fr}$	Steady-state value of the friction torque
k	Friction coefficient
$\eta_{ m WG}$	Efficiency for worm-gear power transfer
$\eta_{ m GW}$	Efficiency for gear-worm power transfer
$p_{ m th}$	Power threshold
$\mu_{ m SC}$	Sun-carrier viscous friction coefficient

|--|

### Ideal Gear Constraints and Gear Ratio

Sun-planet worm gear imposes one kinematic constraint on the three connected axes:

$$\omega_{\rm S} = \omega_{\rm P}/R_{\rm WG} + \omega_{\rm C}$$
.

The gear has two independent degrees of freedom. The gear pair is (1,2) = (S,P).

The torque transfer is:

$$R_{\rm WG}\tau_{\rm P} + \tau_{\rm S} - \tau_{\rm loss} = 0 ,$$

$$\tau_{\rm C}$$
 = -  $\tau_{\rm S}$ ,

with  $\tau_{loss} = 0$  in the ideal case.

## **Nonideal Gear Constraints**

For general considerations on nonideal gear modeling, see "Model Gears with Losses".

In a nonideal gear, the angular velocity and geometric constraints are unchanged. But the transferred torque and power are reduced by:

- Coulomb friction between thread surfaces on W and G, characterized by friction coefficient k or constant efficiencies  $[\eta_{\text{WG}}, \eta_{\text{GW}}]$
- Viscous coupling of driveshafts with bearings, parametrized by viscous friction coefficients  $\mu_{\rm SC}$  and  $\mu_{\rm WC}$

Because the transmission incorporates a worm gear, the efficiencies are different for the direct and reverse power transfer. The following table shows the value of the efficiency for all combinations of the power transfer.

Driving shaft	Driven shaft			
	Planet	Sun	Carrier	
Planet	n/a	$\eta_{ m WG}$	$\eta_{ m WG}$	
Sun	$\eta_{ m GW}$	n/a	No loss	

Carrier  $\eta_{\rm GW}$  No loss n/a

In the contact friction case,  $\eta_{\rm WG}$  and  $\eta_{\rm GW}$  are determined by:

- The worm-gear threading geometry, specified by lead angle  $\lambda$  and normal pressure angle  $\alpha.$
- The surface contact friction coefficient *k*.

```
\eta_{\rm WG} = (\cos\alpha - k \cdot \tan\lambda)/(\cos\alpha + k/\tan\lambda) ,
\eta_{\rm GW} = (\cos\alpha - k/\tan\lambda)/(\cos\alpha + k \cdot \tan\alpha) .
```

In the constant efficiency case, you specify  $\eta_{\rm WG}$  and  $\eta_{\rm GW}$ , independently of geometric details.

If you set efficiency for the reverse power flow to a negative value, the train exhibits *self-locking*. Power cannot be transmitted from sun gear to worm and from carrier to worm unless some torque is applied to the worm to release the train. In this case, the absolute value of the efficiency specifies the ratio at which the train is released. The smaller the train lead angle, the smaller the reverse efficiency.

# Meshing Efficiency

The efficiencies  $\eta$  of meshing between worm and gear are fully active only if the transmitted power is greater than the power threshold.

If the power is less than the threshold, the actual efficiency is automatically regularized to unity at zero velocity.

## **Viscous Friction Force**

The viscous friction coefficients of the worm-carrier and sun-carrier bearings control the viscous friction torque experienced by the carrier from lubricated, nonideal gear threads. For details, see "Nonideal Gear Constraints" on page 1-377.

# **Limitations**

- · Gear inertia is assumed negligible.
- · Gears are treated as rigid components.
- · Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
С	Rotational conserving port representing the gear carrier
W	Rotational conserving port representing the worm gear
S	Rotational conserving port representing the sun gear
Н	Thermal conserving port for thermal modeling

# **Parameters**

### Main

#### Gear ratio

Gear or transmission ratio  $R_{WG}$  determined as the ratio of the worm angular velocity to the gear angular velocity. The default is 25.

## Worm thread type

Choose the directional sense of gear rotation corresponding to positive worm rotation. The default is Right-handed. If you select Left-handed, rotation of the worm in the generally-assigned positive direction results in the gear rotation in negative direction.

### **Friction Losses**

Parameters for meshing and friction losses vary with the block variant chosen—one with a thermal port for thermal modeling and one without it.

#### Without Thermal Port

#### Friction model

Select how to implement friction losses from nonideal meshing of gear threads. The default is No friction losses.

- No friction losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque and force between worm and gear is reduced by friction. If you select this option, the panel expands.

#### **Constant Efficiency**

#### Friction parametrization

Select how to characterize the friction between gear threads. The default is Friction coefficient and geometrical parameters.

 Friction coefficient and geometrical parameters — Friction is determined by contact friction between surfaces.

### Normal pressure angle

The thread pressure angle  $\alpha$  in the normal plane. Must be greater than zero and less than 90 degrees. The default is 17.5.

From the drop-down list, choose units. The default is degrees (deg).

### Lead angle

Thread helix angle  $\lambda = \arctan[L/(\pi d)]$ . L is the worm lead, d is the worm pitch diameter. Must be greater than zero. The default is 20.

From the drop-down list, choose units. The default is degrees (deg).

#### **Friction coefficient**

Dimensionless coefficient of normal friction in the thread. Must be greater than zero. The default is 0.08.

• Efficiencies — Friction is determined by constant efficiencies  $0 < \eta < 1$ . If you select this option, the panel changes from its default.

#### **Efficiencies**

### Worm-gear efficiency

Efficiency  $\eta_{WG}$  of the power transfer from worm to gear.

### **Gear-worm efficiency**

Efficiency  $\eta_{GW}$  of the power transfer from gear to worm.

#### Power threshold

Power threshold above which the full efficiency factor is in effect. Below this value, a hyperbolic tangent function smooths the efficiency factor, lowering the efficiency losses to zero when no power is transmitted. The default value is  $0.001 \, \text{W}$ .

#### **With Thermal Port**

#### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

### Worm-gear efficiency

Array of component efficiencies with the worm as the driver—that is, with power flowing from the worm to the gear. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is  $[0.75 \ 0.7 \ 0.65]$ .

### **Gear-worm efficiency**

Array of component efficiencies with the gear as the driver—that is, with power flowing from the gear to the worm. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.5 0.45 0.4].

#### Power threshold

Absolute value of the angular velocity above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is 0.001 W.

### **Viscous Losses**

#### Worm-carrier and sun-carrier viscous friction coefficients

Vector of viscous friction coefficients [ $\mu_{WC}$   $\mu_{SC}$ ], for the worm-carrier and sun-carrier shafts, respectively. The default is [0 0].

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

#### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Friction Losses** > **Friction model** parameter default setting, No friction losses - Suitable for HIL simulation.

# **See Also**

### **Simscape Blocks**

Leadscrew | Sun-Planet | Sun-Planet Bevel | Worm Gear

## **Topics**

"Basic Motion, Torque, and Force Modeling"

<sup>&</sup>quot;Torsen Differential"

<sup>&</sup>quot;Model Thermal Losses in Driveline Components"
"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Synchronizer**

Cone clutch, dog clutch, and translational detent assembled to provide smooth gear engagement  $% \left( 1\right) =\left( 1\right) +\left( 1$ 

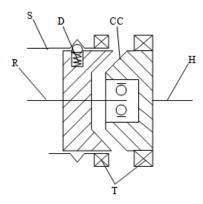


# Library

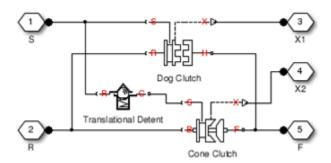
Simscape / Driveline / Clutches

# **Description**

The block represents a synchronizer that contains a dog clutch, a cone clutch, and a translational detent. The shift linkage first translates to engage the cone clutch. Frictional torque causes the shift linkage and cone clutch shaft to rotate at equal speed. When the force acting on the shift linkage exceeds the detent force, the dog clutch can engage.



The schematic illustrates a synchronizer in the disengaged state. In this state, the ring (R) and hub (H) shafts can spin independently at different speeds. To synchronize ring and hub shaft speeds, the shift linkage (S) translates toward the hub shaft to engage the cone clutch. The friction surfaces of the cone clutch produce a frictional torque that equalizes the rotational speeds of the ring and hub shafts. The dog clutch teeth (T) can engage when the translational force acting on the shift linkage exceeds the peak detent force. The peak detent force should allow sufficient time and normal force to equalize ring and hub shaft speeds so that the dog clutch can engage.



The model implements Dog Clutch, Translational Detent and a modified version of Cone Clutch blocks. Refer to each block reference page for more information on the corresponding block function. You can use a similar approach to model customized versions of the synchronizer. One example is the Transmission (Detailed) subsystem in the model sdl\_vehicle\_manual\_transmission.

Connections R and H are mechanical rotational conserving ports that represent the ring (R) and hub (H), respectively. Connection S is a mechanical translational conserving port that represents the ring shifter handle.

Connections X1 and X2 are physical signal outputs that report the shift linkage positions of the dog clutch and cone clutch, respectively. The shift linkage positions are zero when the clutch is fully disengaged. When the dog clutch is fully engaged, the dog clutch shift linkage position has a magnitude equal to the sum of the dog clutch ring-hub gap and the tooth height. When cone clutch is fully engaged, the cone clutch shift linkage position has a magnitude equal to the cone clutch ring-hub gap.

# **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

# **Assumptions and Limitations**

• The model does not account for inertia effects. You can add a Simscape Inertia block at each port to add inertia to the synchronizer model.

## **Ports**

S

Conserving translational port that represents the shift linkage

R

Conserving rotational port that represents the ring shaft

Н

Conserving rotational port that represents the hub shaft

X1

Physical signal output port that measures the magnitude of the dog clutch translation

X2

Physical signal output port that measures the magnitude of the cone clutch translation

Τ

Thermal conserving port. The thermal port is optional and is hidden by default. To expose the port, select a variant that includes a thermal port.

## **Parameters**

## **Dog Clutch**

The methods that are available for parameterizing the torque transmission depend on the variant of the block that you use. If you use the default variant, which has no thermal port, you parameterize the block using one of the options for the **Torque Transmission Model** parameter. If you select a variant that has a thermal port, you parameterize the block based on temperature.

#### Clutch teeth mean radius

Mean radius of the clutch teeth. The parameter must be greater than zero. The default value is 50 mm.

#### Maximum engagement speed

The relative angular speed between the ring and hub shafts above which the dog clutch cannot engage. The value is specific to the specific gearbox or transmission and must be minimized to avoid high dynamic impact during engagement. The default value is inf rad/s.

#### Additional Parameters for the Default Block Variant

### **Torque Transmission Model**

Model used to represent torque transmission. The default setting is Friction clutch approximation - Suitable for HIL and linearization.

# Friction clutch approximation - Suitable for HIL and linearization

### Maximum transmitted torque

Maximum expected torque across the clutch. The default value is 1000 N\*m.

### Dynamic with Backlash

#### Number of teeth

Number of teeth in the clutch. The parameter must be greater than or equal to one. The default value is 6.

#### Rotational backlash

Angular play of the ring with respect to the hub. Greater backlash values correspond to wider tooth gaps that makes engagement easier. The parameter must be greater than zero. The default value is 10 deg.

#### Torsional stiffness

Stiffness of the tooth contact. The model assumes deformation due to tooth interaction is elastic. The angular deformation at the contact surface is proportional to the applied torque and the reciprocal of the contact stiffness. The parameter must be greater than zero. The default value is 1e+7 N\*m/rad.

### Torsional damping

Damping at the tooth contact surface. The value of the parameter is inversely proportional to the number of oscillations following impact. The parameter must be greater than zero. The default value is  $100 \, N*m/(rad/s)$ .

#### Tooth-tooth friction coefficient

Friction coefficient for the translational relative motion between the hub and ring teeth. The value of the parameter depends on the tooth material, lubrication, and quality of contacting surfaces. The parameter must be greater than zero. The default value is 0.05.

#### **Additional Parameters for the Thermal Block Variant**

#### **Temperature vector**

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Maximum transmitted torque vector

Largest torque that the clutch can transmit, corresponding to a nonslip engaged configuration, specified as a vector. If the torque transmitted between the ring and the hub exceeds this value, the two components begin to slip with respect to each other. This torque determines the static friction limit in the friction clutch approximation. The vector has the same number of elements as the temperature vector. The default value is [1000.0, 1050.0, 1000.0] N\*m.

### Interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous firstorder derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### **Extrapolation method**

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous firstorder derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above
  the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

### **Cone Clutch**

Common parameters for the cone clutch are:

#### Contact surface maximum diameter

Outer diameter of the friction material linen that lines the cone clutch disks. The parameter must be greater than zero. The default value is  $150\,$  mm.

#### Contact surface minimum diameter

Inner diameter of the friction material linen that lines the cone clutch disks. The parameter must be greater than zero but smaller than the value of **Contact surface maximum diameter**.

### Cone half angle

Half angle of the clutch cone. The parameter must be greater than zero and less than or equal to 90 degrees. The default value is 12 deg.

## Velocity tolerance

Relative velocity below which the two surfaces can lock. The surfaces lock if the torque across the B and F rotational ports is less than the product of the effective

radius, the static friction coefficient, and the applied normal force. The default value is 0.001 rad/s.

#### Threshold force

The normal force applied to the physical signal port N is applied to the contact only if the amount of force exceeds the value of the **Threshold force** parameter. Forces below the **Threshold force** are not applied, and there is consequently no transmitted frictional torque. The default value is  $1 \, N$ .

#### Friction model

Select a parameterization method to model the kinetic friction coefficient. The options and default values for this parameter depend on the variant that you select for the block. The options are:

- Fixed kinetic friction coefficient Provide a fixed value for the kinetic friction coefficient. This option:
  - · Is visible only if you use the default variant of the block
  - Is the default method for parameterizing the default variant of the block
  - Affects the visibility of other parameters

#### Fixed kinetic friction coefficient

#### Kinetic friction coefficient

The kinetic, or Coulomb, friction coefficient. The coefficient must be greater than zero. The default value is 0.3.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Table lookup kinetic friction coefficient Define the kinetic friction coefficient by one-dimensional table lookup based on the relative angular velocity between disks. This option:
  - Is visible only if you use the default variant of the block
  - Affects the visibility of other parameters

## Table lookup kinetic friction coefficient Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values

depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient vector

Specify the output values for the kinetic friction coefficient as a vector. All values must be positive. The default value is [0.3, 0.22, 0.19].

#### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### Static friction coefficient

The static, or peak, value of the friction coefficient. The static friction coefficient must be greater than the kinetic friction coefficient. The default value is 0.35.

- Temperature-dependent kinetic friction coefficient Define the kinetic friction coefficient by table lookup based on the temperature. This option:
  - Is visible only if you use a thermal variant of the block

- Is the default method for parameterizing the thermal variant of the block
- Affects the visibility of other parameters

# Temperature-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

#### Kinetic friction coefficient vector

Specify the output values for kinetic friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. All values must be greater than zero. The default value is [0.3, 0.28, 0.25].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

## Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

## Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

• Linear — Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.

• Nearest — Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

- Temperature and speed-dependent kinetic friction coefficient —
  Define the kinetic friction coefficient by table lookup based on the temperature
  and the relative angular velocity between disks. This option:
  - Is visible only if you use the default variant of the block
  - Affects the visibility of other parameters

# Temperature and speed-dependent kinetic friction coefficient Temperature vector

Specify the input values for the temperature as a vector. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The values in the vector must increase from left to right. The default value is [280.0, 300.0, 320.0] K.

### Kinetic friction coefficient relative velocity vector

Specify input values for the relative velocity as a vector. The values in the vector must increase from left to right. The minimum number of values depends on the interpolation method that you select. For linear interpolation, provide at least two values per dimension. For smooth interpolation, provide at least three values per dimension. The default value is [0.0, 100.0, 1000.0] rad/s.

#### Kinetic friction coefficient matrix

Specify the output values for kinetic friction coefficient as a matrix. All the values must be greater than zero. The size of the matrix must equal the size of the matrix that is the result of the temperature vector  $\times$  the kinetic friction coefficient relative velocity vector. The default value is [0.34, 0.32, 0.3; 0.3, 0.28, 0.25; 0.25, 0.2, 0.15].

#### Static friction coefficient vector

Specify the static, or peak, values of the friction coefficient as a vector. The vector must have the same number of elements as the temperature vector. Each value must be greater than the value of the corresponding element in the kinetic friction coefficient vector. The default value is [0.4, 0.38, 0.36].

### Friction coefficient interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

### Friction coefficient extrapolation method

Select one of these extrapolation methods to determine the output value when the input value is outside the range specified in the argument list:

- Linear Select this, default, option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

## **Detent**

#### Peak force

Peak shear force of the detent. The default value is 500 N.

#### Notch width

Width of the region where the detent exhibits shear force. The default value is 3 mm.

#### Viscous friction coefficient

Viscous friction coefficient at the contact surface of the detent. The parameter must be greater than or equal to zero. The default value is  $0.1\ N/(m/s)$ .

## Friction to peak force ratio

Ratio of the kinetic friction to the peak shear force of the detent. The parameter is used to set the value of the kinetic friction. The parameter must be greater than or equal to zero. The default value is 0.01.

#### Friction velocity threshold

Velocity required for peak kinetic friction at the contact surface of the detent. The parameter ensures the force is continuous when the travel direction changes, increasing the numerical stability of the simulation. The parameter must be greater than zero. The default value is  $0.05\,\text{m/s}$ .

# **Shift Linkages**

### Linkage travel direction

Direction the shift linkage must translate along to engage the clutch. The default setting is Positive shift linkage displacement engages clutch

### Ring-hub clearance when dog clutch disengaged

Distance between ring and dog clutch hub with the ring fully retracted. The parameter specifies the maximum travel distance if engagement requirements are not met. The parameter must be greater than the value of **Ring-hub clearance when cone clutch disengaged**. The default value is 5 mm.

### Tooth overlap to engage

Minimum value of the tooth overlap beyond which the dog clutch is considered engaged. The parameter must be greater than zero. The default value is 3 mm.

## Tooth height

Height of dog clutch teeth. The parameter must be greater than zero. The default value is 10 mm.

# Ring-hub clearance when cone clutch disengaged

Distance between the ring and cone clutch hub when the ring is fully retracted. The cone clutch can begin to engage once the slider has translated this distance. The ring can travel only this distance if the engagement requirements are not satisfied. The parameter must be greater than zero. The default value is 3 mm.

## Hard stop at back of shift linkage

Hard stop that prevents the shift linkage from traveling beyond the fully disengaged position. Choices include:

- No hard stop when fully disengaged
- Hard stop when fully disengaged

The default setting is Hard stop when fully disengaged.

## Dog clutch ring stop stiffness

Stiffness of the hard stops on both sides of the dog clutch ring. The model assumes the ring and stops behave elastically. Contact deformation is proportional to the applied force and the reciprocal of the contact stiffness. The value of the stiffness must be assigned with reference to the parameter **Tooth overlap to engage**. Too low a stiffness could cause the deformation to exceed the required overlap and initiate a false engagement. The parameter must be greater than zero. The default value is 1e + 6 N/m.

### Cone clutch ring stop stiffness

Stiffness of the hard stops on both sides of the cone clutch ring. The model assumes the ring and stops behave elastically. Contact deformation is proportional to the applied force and the reciprocal of the contact stiffness. The parameter must be greater than zero. The default value is 1e+6 N/m.

#### Dog clutch ring stop damping

Translational contact damping between the dog clutch ring and the hub. The value of the damping is inversely proportional to the number of oscillations that occur after impact. The parameter must be greater than zero. The default value is 1e+3 N/(m/s).

## Cone clutch ring stop damping

Translational contact damping between the cone clutch ring and the hub. The value of damping is inversely proportional to the number of oscillations that occur after impact. The parameter must be greater than zero. The default value is 1e+3 N/(m/s).

#### Viscous friction coefficient

Viscous friction coefficient for the relative translational motion between the hub and the ring. The value of the parameter depends on lubrication state and quality of contacting surfaces. The coefficient must be greater than or equal to zero. The default value is  $100 \, \text{N/(m/s)}$ .

## **Initial Conditions**

#### **Initial state**

Beginning configuration of cone and dog clutches. Choices include:

• Both clutches unlocked—Cone and dog clutches transmit zero torque between the ring and hub shafts.

- Cone clutch locked—Cone clutch transmits torque between the ring and hub shafts.
- Both clutches locked—Cone and dog clutches transmit torque between the ring and hub shafts.

The default value is Both clutches unlocked.

## Dog clutch initial shift linkage position

Initial position of the shift linkage section that attaches to the dog clutch. The value of the parameter has the following restrictions:

Linkage Travel Direction	Dog Clutch State	Parameter Restriction
Positive shift linkage displacement engages clutch	Initially engaged	Parameter must be greater than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage
	Initially disengaged	Parameter must be smaller than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage
Negative shift linkage displacement engages clutch	Initially engaged	Negative of the parameter must be greater than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage

Linkage Travel Direction	Dog Clutch State	Parameter Restriction
	Initially disengaged	Negative of the parameter must be smaller than the sum of parameters Ring-hub clearance when dog clutch disengaged and Tooth overlap to engage

The default value is  $\mathbf{0}$  mm.

## Cone clutch initial shift linkage position

Initial position of the shift linkage section that attaches to the cone clutch. The value of the parameter has the following restrictions:

Linkage Travel Direction	Dog Clutch State	Parameter Restriction
Positive shift linkage displacement engages clutch	Initially engaged	Parameter must be greater than the value of Ring-hub clearance when cone clutch disengaged
	Initially disengaged	Parameter must be smaller than the value of Ring-hub clearance when cone clutch disengaged
Negative shift linkage displacement engages clutch	Initially engaged	Negative of the parameter must be greater than the value of Ring-hub clearance when dog cone disengaged

Linkage Travel Direction	Dog Clutch State	Parameter Restriction
	Initially disengaged	Negative of the parameter must be smaller than the value of Ring-hub clearance when dog cone disengaged

The default value is 0 mm.

### Initial dog clutch ring-hub offset angle

Initial angle between the ring and hub portions of the dog clutch. If the clutch is disengaged, the initial angle must lie in the range  $-\pi/N \le \theta \le +\pi/N$ , where N denotes the number of teeth in the dog clutch. If the clutch is engaged, the initial angle must be in the range  $-\delta/2 \le \theta \le +\delta/2$ , where  $\delta$  is the backlash angle. The default value is  $\theta$  deg.

This parameter is only visible if you select a block variant that does not include a thermal port and set **Dog Clutch** > **Torque transmission model** to Dynamic with backlash.

## **Thermal Port**

These thermal parameters are visible only when you select a block variant that includes a thermal port.

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50~kJ/K.

## **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

# **Extended Capabilities**

#### Linearization

To optimize your model for linearization, use the **Dog Clutch > Torque transmission model** parameter default setting, Friction clutch approximation - Suitable for HIL and linearization.

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Dog Clutch > Torque transmission model** parameter default setting, Friction clutch approximation - Suitable for HIL and linearization.

# See Also

Cone Clutch | Dog Clutch | Double-Sided Synchronizer | Translational Detent

# **Topics**

- "Vehicle with Manual Transmission"
- "Model Thermal Losses in Driveline Components"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Tire (Friction Parameterized)**

Tire with friction parameterized in terms of static and kinetic coefficients



# Library

Simscape / Driveline / Tires & Vehicles

# **Description**

This block models a tire with friction parameterized in terms of static and kinetic coefficients. The static friction coefficient determines the applied torque at which the tire loses traction and begins to slip. The kinetic friction coefficient determines the amount of torque that the tire transmits to the pavement once it begins to slip. The tire regains traction once its relative velocity over the pavement falls below the traction velocity tolerance specified.

Port A represents the axle on which the tire sits. Port H represents the wheel hub that transmits the thrust generated by the tire to the remainder of the vehicle. Port N accepts a physical signal input of the normal force acting on the tire. The normal force is positive if it acts downward on the tire, pressing it against the pavement. Port S outputs a physical signal with the tire slip measured during simulation.

The block provides two friction variants. The default variant, Fixed friction coefficients, accepts the static and kinetic friction coefficients as block parameters. This variant treats the static coefficient as a constant. It treats the kinetic coefficient as a constant or function of tire slip. Use this variant to model tire dynamics under constant pavement conditions.

The alternative variant, Variable friction coefficients, accepts the static and kinetic friction coefficients as a physical signal input. Use this variant to model tire

dynamics under variable pavement conditions. Selecting this variant exposes physical signal port M. Use this port to provide the static and kinetic friction coefficients as a two-element vector, specified in this order.

To change block variants:

- 1 Right-click the tire block.
- 2 In the context-sensitive menu, select **Simscape > Block choice**.
- **3** Select the desired block variant.

To increase the fidelity of the tire model, the block enables you to specify properties such as tire compliance, inertia, and rolling resistance. However, these properties increase the complexity of the tire model and can slow down simulation. Consider ignoring tire compliance and inertia if simulating the model in real time or if preparing the model for Hardware-in-Loop (HIL) simulation.

The traction state model of this block is based on the traction state model of the Fundamental Friction Clutch block. For more information on the state model, see "Clutch States" on page 1-177.

# **Ports**

Port	Description
A	Conserving mechanical rotational port associated with the axle of the tire
Н	Conserving mechanical translational port associated with the hub of the tire
N	Physical signal input port associated with the normal force on the tire
M	Physical signal input associated with the static and kinetic friction coefficients of the tire
S	Physical signal output port associated with the relative slip between the tire and road

# **Parameters**

#### **Tire Parameters**

Use the **Tire Parameters** pane to specify characteristics of the tire, such as the rolling radius or static friction coefficient.

#### Rolling radius

Distance between the pavement and the center of the tire. This distance must be positive. The default value is  $0.30\,$  m.

#### Static friction coefficient

Ratio of the allowable longitudinal force to the normal force allowed before the tire begins to slip  $(\mu_s)$ . he parameter must be greater than either the kinetic friction coefficient or the largest value in the kinetic friction coefficient vector. The default is 0.9.

This parameter is visible when the block variant is set to Fixed friction coefficients. For more information about the block variants, see the block description.

#### **Friction model**

Parameterization through which to specify the kinetic friction coefficient. Options include:

- Fixed kinetic friction coefficient (Default) Uses a constant kinetic function coefficient. Exposes **Kinetic friction coefficient** parameter.
- Table lookup kinetic friction coefficient Uses a function of slip.
   Exposes Tire slip vector and Kinetic friction coefficient vector parameters.

This parameter is visible when the block variant is set to Fixed friction coefficients. For more information about the block variants, see the block description.

#### **Kinetic friction coefficient**

Ratio of the transmitted longitudinal force to the normal force allowed during tire slip  $(\mu_k)$ . The ratio must be greater than zero. Default 0.7.

This parameter is visible when the tire variant is set to Fixed friction coefficients and the **Friction model** parameter is set to Fixed kinetic

friction coefficient. For more information about the block variants, see the block description.

#### Tire slip vector

Vector that contains values of tire slip that correspond to the kinetic friction coefficients in the **Kinetic friction coefficient vector** parameter. The vectors must be the same size. If the **Tire slip vector** parameter contains only nonnegative values, the slip versus friction function is assumed to be symmetric about the slip axis. Default vector is [0 0.02 0.06 0.15 0.6 1].

This parameter is visible when the tire variant is set to Fixed friction coefficients and the **Friction model** parameter is set to Table lookup kinetic friction coefficient. For more information about the block variants, see the block description.

#### Kinetic friction coefficient vector

Vector that contains kinetic friction coefficients that correspond to the tire slip values specified in the **Tire slip vector** parameter. The vectors must be the same size. Default vector is [0.89 0.88 0.8 0.75 0.7 0.7].

This parameter is visible when the tire variant is set to Fixed friction coefficients and the **Friction model** parameter is set to Table lookup kinetic friction coefficient. For more information about the block variants, see the block description.

## Interpolation method

Interpolation method for the lookup table to use for processing the tire slip-kinetic friction coefficient characteristic. Interpolation options include:

- Linear Select this option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous firstorder derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

This parameter is visible when the tire variant is set to Fixed friction coefficients and the **Friction model** parameter is set to Table lookup kinetic friction coefficient. For more information about the block variants, see the block description.

### **Extrapolation method**

Extrapolation method for the lookup table to use for processing the tire slip-kinetic friction coefficient characteristic.

- Linear Select this option to produce a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Select this option to produce an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

This parameter is visible when the tire variant is set to Fixed friction coefficients and the **Friction model** parameter is set to Table lookup kinetic friction coefficient. For more information about the block variants, see the block description.

# **Dynamics**

## **Compliance**

Specifies whether the model includes longitudinal stiffness and damping.

- No compliance Suitable for HIL simulation (Default) Does not include longitudinal stiffness and damping.
- Specify stiffness and damping Includes longitudinal stiffness and damping. Exposes the Longitudinal stiffness and Longitudinal damping parameters.

# **Longitudinal stiffness**

The longitudinal stiffness of the tire. The parameter must be greater than zero. Default is 1e+6 N/m.

The **Longitudinal stiffness** parameter appears if the **Compliance** parameter is Specify stiffness and damping.

# Longitudinal damping

The longitudinal damping of the tire. The parameter must be greater than zero. Default is 1000 N/(m/s).

The **Longitudinal damping** parameter appears if the **Compliance** parameter is Specify stiffness and damping.

#### Inertia

Specifies whether the model the model includes tire inertia.

- No inertia (Default) Does not include tire inertia.
- Specify inertia and initial velocity Includes tire inertia and initial velocity. Exposes the **Tire inertia** and **Initial velocity** parameters.

#### Tire inertia

The rotational inertia of the tire. The parameter must be greater than zero. Default is  $1 \text{ kg*m}^2$ .

The **Tire inertia** parameter appears if the **Inertia** parameter is **Specify inertia** and initial velocity.

### **Initial velocity**

The initial rotational velocity of the tire. Default is 0 rad/s.

The **Initial velocity** parameter appears if the **Inertia** parameter is **Specify** inertia and initial velocity.

# **Rolling Resistance**

## Rolling resistance

Option to turn on and off rolling resistance modeling in the tire. Settings you can select include:

- No rolling resistance Ignore the effects of rolling resistance.
- Specify rolling resistance Model the effects of rolling resistance using the selected parameterization. Selecting this setting causes the block to expose the **Resistance model** parameter.

#### Resistance model

Parameterization with which to model rolling resistance in the tire. Options include Constant coefficient and Pressure and velocity dependent. The default setting is Constant coefficient.

#### Constant coefficient

#### **Constant Coefficient**

Coefficient that sets the proportionality between the normal force and the rolling resistance force. The parameter must be greater than zero. The default value is 0.015.

### **Velocity Threshold**

Velocity at which the full rolling resistance force is transmitted to the rolling hub. The parameter ensures the force remains continuous during velocity direction changes, which increases the numerical stability of the simulation. The parameter must be greater than zero. The default value is  $0.001 \, \text{m/s}$ .

## Pressure and velocity dependent

### Tire pressure

Inflation pressure of the tire. The parameter must be greater than zero. The default value is 250e+3 Pa.

### **Alpha**

Exponent of the tire pressure in the model equation. See "Pressure and Velocity Dependent Model" on page 1-310. The default value is -0.003.

#### Beta

Exponent of the normal force model equation. The default value is 0.97.

#### Coefficient A

Velocity independent force component in the model equation. The parameter must be greater than zero. The default value is 84e-4.

#### Coefficient B

Velocity dependent force component in the model equation. The parameter must be greater than zero. The default value is  $6.2e-4\,$  s/m.

#### Coefficient C

Force component that depends on the square of the velocity term in the model equation. The parameter must be greater than zero. The default value is 1.6e-4 s^2/m^2.

## **Velocity Threshold**

Velocity at which the full rolling resistance force is transmitted to the rolling hub. The parameter ensures the force remains continuous during velocity direction changes,

which increases the numerical stability of the simulation. The parameter must be greater than zero. The default value is 1e-3 m/s.

### **Advanced**

Use the **Advanced** tab to specify parameters that the state machine uses to determine the model of the tire.

### **Traction velocity tolerance**

The magnitude of the relative velocity between the tire and ground at which the tire regains traction. Setting this value too low prevents the tire from entering a state where it has traction. Setting it too high can cause the tire to suddenly change velocity when the tire gains traction, and can result in an unstable simulation. The parameter must be greater than zero. Default is  $0.01\,\text{m/s}$ .

#### **Engagement threshold force**

Normal force values below the **Engagement threshold force** are not applied to the tire. Setting this value too low can cause the tire to gain and lose traction rapidly. Setting this value too high can give unrealistically low static and dynamic friction forces. The parameter must be greater than zero. Default is 10 N.

#### **Initial traction state**

Specifies whether the tire is initially in traction or slipping.

- Tire is initially slipping (Default)
- Tire is initially in traction

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, set the **Dynamics > Compliance** parameter to **No** compliance - Suitable for HIL simulation.

# See Also

## **Simscape Blocks**

Fundamental Friction Clutch | Tire (Magic Formula) | Tire (Simple) | Tire-Road Interaction (Magic Formula)

# **Topics**

"Clutch States" on page 1-177

<sup>&</sup>quot;Vehicle with Four-Wheel Drive"

<sup>&</sup>quot;Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# Tire (Magic Formula)

Tire with longitudinal behavior given by magic formula coefficients



# Library

Simscape / Driveline / Tires & Vehicles

# **Description**

This block models a tire with longitudinal behavior given by the magic formula, an empirical equation based on four fitting coefficients. The longitudinal direction of the tire is the same as its direction of motion as it rolls on pavement. This block is a structural component based on the Tire-Road Interaction (Magic Formula) block.

Port A represents the axle on which the tire sits. Port H represents the wheel hub that transmits the thrust generated by the tire to the remainder of the vehicle. Port N accepts a physical signal input of the normal force acting on the tire. The normal force is positive if it acts downward on the tire, pressing it against the pavement. Port S outputs a physical signal with the tire slip measured during simulation.

The block provides two friction variants. The default variant, Fixed friction coefficients, accepts the magic formula coefficients as block parameters. This variant treats the coefficients as constants or load-dependent parameters. Use this variant to model tire dynamics under constant pavement conditions.

The alternative variant, Variable friction coefficients, accepts the magic formula coefficients as a physical signal input. Use this variant to model tire dynamics under variable pavement conditions. Selecting this variant exposes physical signal port M. Use this port to provide the magic formula coefficients as a four-element vector, specified in the order [b, c, d, e].

To change block variants:

- **1** Right-click the tire block.
- 2 In the context-sensitive menu, select **Simscape** > **Block choice**.
- **3** Select the desired block variant.

To increase the fidelity of the tire model, the block enables you to specify properties such as tire compliance, inertia, and rolling resistance. However, these properties increase the complexity of the tire model and can slow down simulation. Consider ignoring tire compliance and inertia if simulating the model in real time or if preparing the model for Hardware-in-Loop (HIL) simulation.

# **Tire Model**

The Tire block models the tire as a rigid wheel-tire combination in contact with the road and subject to slip. When torque is applied to the wheel axle, the tire pushes on the ground (while subject to contact friction) and transfers the resulting reaction as a force back on the wheel. This action pushes the wheel forward or backward. If you include the optional tire compliance, the tire also flexibly deforms under load.

The figure shows the forces acting on the tire. The table defines the tire model variables.



#### **Tire Model Variables**

Symbol	Description and Unit	
$r_{ m w}$	Wheel radius	
$V_{\mathrm{x}}$	Wheel hub longitudinal velocity	
u	Tire longitudinal deformation	
Ω	Wheel angular velocity	
Ω΄	Contact point angular velocity = $\Omega$ if $u = 0$	
$r_{ m w}\Omega'$	Tire tread longitudinal velocity	
$V_{\rm sx} = r_{\rm W}\Omega - V_{\rm x}$	Wheel slip velocity	
$V_{\rm sx} = r_{\rm W} \Omega' - V_{\rm x}$	Contact slip velocity = $V_{sx}$ if $u = 0$	
$\kappa = V_{\rm sx}/ V_{\rm x} $	Wheel slip	
$\kappa' = V_{SX}/ V_{X} $	Contact slip = $\kappa$ if $u = 0$	
$V_{ m th}$	Wheel hub threshold velocity	
$F_{\rm z}$	Vertical load on tire	
$F_{\mathrm{x}}$	Longitudinal force exerted on the tire at the contact point.	
$C_{\rm Fx} = (\partial F_{\rm x}/\partial u)_0$	Tire longitudinal stiffness under deformation	
$b_{Fx} = (\partial F_{x}/\partial \mathring{u})_{0}$	Tire longitudinal damping under deformation	
$I_{ m w}$	Wheel-tire inertia; effective mass = $I_w/r_w^2$	
$ au_{ m drive}$	Torque applied by the axle to the wheel	

# **Tire Kinematics and Response**

If the tire did not slip, it would roll and translate as  $V_{\rm x}=r_{\rm w}\Omega$ . But the tire actually does slip and develops a longitudinal force  $F_{\rm x}$  only in response to slip.

The wheel slip velocity is  $V_{\rm sx}=r_{\rm W}\Omega$  –  $V_{\rm x}$ . The wheel slip is  $\kappa=V_{\rm sx}/|V_{\rm x}|$ . For a locked, sliding wheel,  $\kappa=-1$ . For perfect rolling,  $\kappa=0$ .

For low speeds,  $|V_x| \le |V_{th}|$ , the wheel slip is modified to:

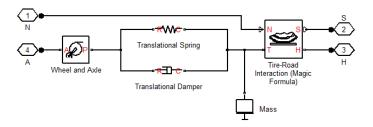
$$\kappa = 2V_{\rm sx}/(V_{\rm th} + V_{\rm x}^2/V_{\rm th})$$
 .

This modification allows for a nonsingular, nonzero slip at zero wheel velocity. For example, for perfect slipping (nontranslating spinning tire),  $V_{\rm x}=0$  while  $\kappa=2r_{\rm w}\Omega/V_{\rm th}$  is finite.

If the tire is modeled with compliance, it is also flexible. Because in this case, the tire deforms, the tire-road contact point turns at a slightly different angular velocity  $\Omega'$  from the wheel  $\Omega$  and requires, instead of the wheel slip, the *contact point* or *contact patch slip*  $\kappa'$ . The block models the deforming tire as a translational spring-damper of stiffness  $C_{\rm Fx}$  and damping  $b_{\rm Fx}$ .

If the tire is not modeled with compliance, then  $\Omega' = \Omega$ ,  $V'_{sx} = V_{sx}$ , and  $\kappa' = \kappa$ . In this case, the tire starts simulation undeformed and remains undeformed.

# **Tire and Wheel Dynamics**



The full tire model is equivalent to this Simscape-Simscape Driveline component diagram. It simulates both transient and steady-state behavior and correctly represents starting from, and coming to, a stop. The Translational Spring and Translational Damper are equivalent to the tire stiffness  $C_{\rm Fx}$  and damping  $b_{\rm Fx}$ . Tire-Road Interaction (Magic Formula) models the longitudinal force  $F_{\rm x}$  on the tire as a function of  $F_{\rm z}$  and  $\kappa'$  using the Magic Formula, with  $\kappa'$  as the independent slip variable [1].

The Wheel and Axle radius is the wheel radius  $r_{\rm w}$ . The Mass value is the effective mass,  $I_{\rm w}/r_{\rm w}^2$ . The tire characteristic function  $f(\kappa', F_{\rm z})$  determines the longitudinal force  $F_{\rm x}$ . Together with the driveshaft torque applied to the wheel axis,  $F_{\rm x}$  determines the wheel angular motion and longitudinal motion.

Without tire compliance, the Translational Spring and Translational Damper are omitted, and contact variables revert to wheel variables. In this case, the tire effectively has infinite stiffness, and port P of Wheel and Axle connects directly to port T of Tire-Road Interaction (Magic Formula).

Without tire inertia, the Mass is omitted.

# Limitations

The Tire (Magic Formula) block assumes longitudinal motion only and includes no camber, turning, or lateral motion.

# **Tire Compliance**

Tire compliance implies a time lag in the tire response to the forces on it. Time lag simulation increases model fidelity but reduces simulation performance. See "Adjust Model Fidelity".

# **Ports**

Port	Description
A	Conserving mechanical rotational port associated with the axle of the tire
Н	Conserving mechanical translational port associated with the hub of the tire
N	Physical signal input port associated with the normal force on the tire
M	Physical signal input associated with the static and kinetic friction coefficients of the tire
S	Physical signal output port associated with the relative slip between the tire and road

# **Parameters**

## **Tire Force**

# Parameterize by

Select how to use the Magic Formula to model the tire-road interaction. The default is Peak longitudinal force and corresponding slip. This tab appears only

when the block variant is set to Fixed friction coefficients. For more information about the block variants, see the block description.

• Peak longitudinal force and corresponding slip — Parametrize the Magic Formula with physical characteristics of the tire.

## **Peak Force and Corresponding Slip**

#### Rated vertical load

Rated vertical load force  $F_{z0}$ . The default is 3e+3.

From the drop-down list, choose units. The default is newtons (N).

#### Peak longitudinal force at rated load

Maximum longitudinal force  $F_{x0}$  that the tire exerts on the wheel when the vertical load equals its rated value  $F_{z0}$ . The default is 3500.

From the drop-down list, choose units. The default is newtons (N).

#### Slip at peak force at rated load (percent)

The value of the contact slip  $\kappa'_0$ , in percent (%), when the longitudinal force equals its maximum value  $F_{x0}$  and the vertical load equals its rated value  $F_{z0}$ . The default is 10.

 Constant Magic Formula coefficients — Parameterize the Magic Formula directly with its coefficients. If you select this option, the panel changes from its default.

## **Constant Magic Formula Coefficients**

## Magic formula coefficients

Magic Formula B, C, D, and E coefficients. The defaults are:

В	С	D	E
10	1.9	1	0.97

 Load-dependent Magic Formula coefficients—Parametrize the Magic Formula directly with load-dependent coefficients. If you select this option, the panel changes from its default.

## **Load-Dependent Magic Formula Coefficients**

#### Tire nominal vertical load

Nominal normal force  $F_{z0}$  on tire. The default is 4e+3.

From the drop-down list, choose units. The default is newtons (N).

#### Magic formula coefficient parameters

Specify the parameters that define the load-dependent C, D, E, K, H, and V coefficients as vectors, one for each coefficient. The defaults are:

Coefficient	Parameters	Default Values
С	p_Cx1	1.685
D	[ p_Dx1 p_Dx2 ]	[ 1.21 -0.037 ]
E	[ p_Ex1 p_Ex2 p_Ex3 p_Ex4 ]	[ 0.344 0.095 -0.02 0 ]
K	[ p_Kx1 p_Kx2 p_Kx3 ]	[ 21.51 -0.163 0.245 ]
Н	[ p_Hx1 p_Hx2 ]	[ -0.002 0.002 ]
V	[ p_Vx1 p_Vx2 ]	[00]

### **Dimensions**

# **Rolling radius**

Unloaded tire-wheel radius  $r_{\rm w}$ . The default is 0.3.

From the drop-down list, choose units. The default is meters (m).

# **Dynamics**

## Compliance

Select how to model the dynamical compliance of the tire. The default is No compliance — Suitable for HIL simulation.

- No compliance Suitable for HIL simulation Tire is modeled with no dynamical compliance.
- Specify stiffness and damping—Tire is modeled as a stiff, dampened spring and deforms under load. If you select this option, the panel changes from its default.

## Tire Stiffness and Damping

#### Longitudinal stiffness

Tire longitudinal stiffness  $C_{Fx}$ . The default is 1e+6.

From the drop-down list, choose units. The default is N/m.

### Longitudinal damping

Tire longitudinal damping  $b_{Fx}$ . The default is **1000**.

From the drop-down list, choose units. The default is N/(m/s).

#### Inertia

Select how to model the rotational inertia of the tire. The default is No inertia.

- No inertia—Tire is modeled with no inertia.
- Specify inertia and initial velocity—Tire is modeled with rotational inertia. If you select this option, the panel changes from its default.

## **Tire Rotational Inertia and Initial Velocity**

#### Tire Inertia

Rotational inertia  $I_{\rm w}$  of the wheel-tire assembly. The default is 1.

From the drop-down list, choose units. The default is  $kg*m^2$ .

## **Initial velocity**

Initial angular velocity  $\Omega(0)$  of the tire. The default is 0.

From the drop-down list, choose units. The default is radians/second (rad/s).

# **Rolling Resistance**

## **Rolling resistance**

Method used to specify the rolling resistance acting on a rotating wheel hub. The default value is No rolling resistance. Options include:

No rolling resistance

Select this option to ignore the effect of rolling resistance on a model.

• Specify rolling resistance

Select between two rolling resistance models: Constant coefficient and Pressure and velocity dependent.

The default value is Constant coefficient.

#### Constant coefficient

#### Constant Coefficient

Coefficient that sets the proportionality between the normal force and the rolling resistance force. The parameter must be greater than zero. The default value is 0.015.

#### Velocity Threshold

Velocity at which the full rolling resistance force is transmitted to the rolling hub. The parameter ensures the force remains continuous during velocity direction changes, which increases the numerical stability of the simulation. The parameter must be greater than zero. The default value is  $0.001 \, \text{m/s}$ .

### Pressure and velocity dependent

#### Tire pressure

Inflation pressure of the tire. The parameter must be greater than zero. The default value is 250e+3 Pa.

## Alpha

Exponent of the tire pressure in the model equation. See "Pressure and Velocity Dependent Model" on page 1-310. The default value is -0.003.

#### Beta

Exponent of the normal force model equation. The default value is 0.97.

#### Coefficient A

Velocity independent force component in the model equation. The parameter must be greater than zero. The default value is 84e-4.

#### Coefficient B

Velocity dependent force component in the model equation. The parameter must be greater than zero. The default value is  $6.2e-4\,$  s/m.

#### Coefficient C

Force component that depends on the square of the velocity term in the model equation. The parameter must be greater than zero. The default value is 1.6e-4 s<sup>2</sup>/m<sup>2</sup>.

### **Velocity Threshold**

Velocity at which the full rolling resistance force is transmitted to the rolling hub. The parameter ensures the force remains continuous during velocity direction changes, which increases the numerical stability of the simulation. The parameter must be greater than zero. The default value is 1e-3 m/s.

# **Slip Calculation**

#### Velocity threshold

Wheel hub velocity  $V_{\rm th}$  below which the slip calculation is modified to avoid singular evolution at zero velocity. Must be positive. The default is 0.1.

From the drop-down list, choose units. The default is meters per second (m/s).

# **Extended Capabilities**

# Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, set the **Dynamics** > **Compliance** parameter to **No** compliance - Suitable for HIL simulation.

# References

[1] Pacejka, H. B. *Tire and Vehicle Dynamics*, Society of Automotive Engineers and Butterworth-Heinemann, Oxford, 2002, chapters 1,4,7, and 8

# See Also

## Simscape Blocks

Differential | Tire-Road Interaction (Magic Formula) | Translational Damper | Translational Spring | Vehicle Body

# **Topics**

"Complete Vehicle Model"

"Limited Slip Differential with Clutches"

"Torsen Differential"

"Vehicle with Dual Clutch Transmission"

Vehicle with Four-Speed Transmission

"Vehicle with Four-Wheel Drive"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Tire-Road Interaction (Magic Formula)**

Tire-road dynamics given by magic formula coefficients



# Library

Simscape / Driveline / Tires & Vehicles / Tire Subcomponents

# **Description**

This block models the interaction between the tire tread and road pavement. The longitudinal force arising from this interaction is given by the magic formula, an empirical equation based on four fitting coefficients. Tire properties such as compliance and inertia are ignored.

Port T represents the tire tread. Port H represents the wheel hub that transmits the thrust generated by the tire to the remainder of the vehicle. Port N accepts a physical signal input of the normal force acting on the tire. The normal force is positive if it acts downward on the tire, pressing it against the pavement. Port S outputs a physical signal with the tire slip measured during simulation.

The block provides two friction variants. The default variant, Fixed friction coefficients, accepts the magic formula coefficients as block parameters. This variant treats the coefficients as constants or load-dependent parameters. Use this variant to model tire dynamics under constant pavement conditions.

The alternative variant, Variable friction coefficients, accepts the magic formula coefficients as a physical signal input. Use this variant to model tire dynamics under variable pavement conditions. Selecting this variant exposes physical signal port M. Use this port to provide the magic formula coefficients as a four-element vector, specified in the order [b, c, d, e].

To change block variants:

- **1** Right-click the tire block.
- 2 In the context-sensitive menu, select **Simscape** > **Block choice**.
- **3** Select the desired block variant.

# **Tire-Road Interaction Model**

The Tire-Road Interaction (Magic Formula) block models the longitudinal forces at the tire-road contact patch using the Magic Formula of Pacejka [7].

The figure displays the forces on the tire. The table defines the tire model variables.



Tire-R	hea	Cont	act V	/aria	hlac
iire-r	vau	CONL	act v	aria	bies

Symbol	Description and Unit
Ω	Wheel angular velocity
$r_{ m w}$	Wheel radius
$V_{\mathrm{x}}$	Wheel hub longitudinal velocity
$r_{ m w}\Omega$	Tire tread longitudinal velocity
$V_{\rm sx} = r_{\rm w}\Omega - V_{\rm x}$	Wheel slip velocity = tread velocity T - hub velocity H
$\kappa = V_{\rm sx}/ V_{\rm x} $	Wheel slip
$F_z$ , $F_{z0}$	Vertical load and nominal vertical load on tire
$F_{\rm x} = f(\kappa, F_{\rm z})$	Longitudinal force exerted on the tire at the contact point.  Also a characteristic function $f$ of the tire.

# **Tire Response**

A tire model provides a steady-state tire characteristic function,  $F_x = f(\kappa, F_z)$ , the longitudinal force  $F_x$  on the tire, based on:

- Vertical load F<sub>z</sub>
- Wheel slip κ

The Magic Formula is a specific form for the tire characteristic function, characterized by four dimensionless coefficients (B, C, D, E), or stiffness, shape, peak, and curvature:

$$F_{\rm x} = f(\kappa,\,F_{\rm z}) = F_{\rm z} \cdot D \cdot \sin(~C \cdot \arctan[~\{~B\kappa - E \cdot [~B\kappa - \arctan(B\kappa)~]~\}~]~)~.$$

The slope of f at  $\kappa = 0$  is  $BCD \cdot F_z$ .

A more general Magic Formula uses dimensionless coefficients that are functions of the tire load. A more complex set of parameters  $p_i$ , entered in the dialog box, specifies these functions:

$$F_{\rm x0} = D_{\rm x} \cdot \sin(~C_{\rm x} \cdot \arctan[~\{~B_{\rm x} \kappa_{\rm x} - E_{\rm x} \cdot [~B_{\rm x} \kappa_{\rm x} - \arctan(B_{\rm x} \kappa_{\rm x})~]~\}~]~) ~+~ S_{\rm Vx}~,$$

where

$$\begin{split} df_{\rm z} &= (F_{\rm z} - F_{\rm z0})/F_{\rm z} \;, \\ \kappa_{\rm x} &= \kappa + {\rm S}_{\rm Hx} \;, \\ C_{\rm x} &= {\rm p\_Cx1} \;, \\ D_{\rm x} &= \mu_{\rm x} \cdot F_{\rm z} \;, \\ \mu_{\rm x} &= {\rm p\_Dx1} \;+ {\rm p\_Dx2} \cdot df_{\rm z} \;, \\ E_{\rm x} &= ({\rm p\_Ex1} \;+ {\rm p\_Ex2} \cdot df_{\rm z} \;+ {\rm p\_Ex3} \cdot df_{\rm z}^2)[1 \;- {\rm p\_Ex4} \cdot {\rm sgn}(\kappa_{\rm x})] \;, \\ K_{\rm xx} &= F_{\rm z} \cdot ({\rm p\_Kx1} \;+ {\rm p\_Kx2} \cdot df_{\rm z}) \cdot {\rm exp}({\rm p\_Kx3} \cdot df_{\rm z}) \;, \\ B_{\rm x} &= K_{\rm xx}/(C_{\rm x}D_{\rm x} \;+ \; \varepsilon_{\rm x}) \;, \\ S_{\rm Hx} &= {\rm p\_Hx1} \;+ \; {\rm p\_Hx2} \cdot df_{\rm z} \;, \\ S_{\rm Vx} &= F_{\rm z} \cdot ({\rm p\_Vx1} \;+ \; {\rm p\_Vx2} \cdot df_{\rm z}) \;. \end{split}$$

 $S_{\rm Hx}$  and  $S_{\rm Vx}$  represent offsets to the slip and longitudinal force in the force-slip function, or horizontal and vertical offsets if the function is plotted as a curve.  $\mu_{\rm x}$  is the longitudinal load-dependent friction coefficient.  $\varepsilon_{\rm x}$  is a small number inserted to prevent division by zero as  $F_{\rm z}$  approaches zero.

The block uses a representative set of Magic Formula coefficients. The block scales the coefficients to yield the peak longitudinal force  $F_{x0}$  at the corresponding slip  $\kappa_0$  that you specify, for rated vertical load  $F_{z0}$ .

Numerical values are based on empirical tire data. These values are typical sets of constant Magic Formula coefficients for common road conditions.

Surface	В	С	D	E
Dry tarmac	10	1.9	1	0.97
Wet tarmac	12	2.3	0.82	1
Snow	5	2	0.3	1
Ice	4	2	0.1	1

# Limitations

The Tire-Road Interaction (Magic Formula) block assumes longitudinal motion only and includes no camber, turning, or lateral motion.

# **Ports**

Port	Description
A	Conserving mechanical rotational port associated with the axle of the tire
Н	Conserving mechanical translational port associated with the hub of the tire
N	Physical signal input port associated with the normal force on the tire
M	Physical signal input associated with the static and kinetic friction coefficients of the tire
S	Physical signal output port associated with the relative slip between the tire and road

# **Parameters**

## Parameterize by

Select how to use the Magic Formula to model the tire-road interaction. The default setting is Peak longitudinal force and corresponding slip. This and all dependent parameters are visible only when the block variant is set to Fixed friction coefficients. For more information about the block variants, see the block description.

• Peak longitudinal force and corresponding slip — Parametrize the Magic Formula with physical characteristics of the tire.

# **Peak Force and Corresponding Slip**

#### Rated vertical load

Rated vertical load force  $F_{z0}$ . The default is 3000.

From the drop-down list, choose units. The default is newtons (N).

### Peak longitudinal force at rated load

Maximum longitudinal force  $F_{x0}$  that the tire exerts on the wheel when the vertical load equals its rated value  $F_{z0}$ . The default is 3500.

From the drop-down list, choose units. The default is newtons (N).

### Slip at peak force at rated load (percent)

The value of the contact slip  $\kappa_0$ , in percent (%), when the longitudinal force equals its maximum value  $F_{x0}$  and the vertical load equals its rated value  $F_{z0}$ . The default is 10.

 Constant Magic Formula coefficients — Parametrize the Magic Formula directly with constant coefficients. If you select this option, the panel changes from its default.

#### **Constant Magic Formula Coefficients**

#### Magic formula coefficients

Dimensionless Magic Formula B, C, D, and E coefficients. The defaults are:

В	С	D	E
10	1.9	1	0.97

 Load-dependent Magic Formula coefficients — Parametrize the Magic Formula directly with load-dependent coefficients. If you select this option, the panel changes from its default.

### **Load-Dependent Magic Formula Coefficients**

#### Tire nominal vertical load

Nominal normal force  $F_{z0}$  on tire. The default is 4e+3.

From the drop-down list, choose units. The default is newtons (N).

# Magic formula coefficient parameters

Specify the parameters that define the load-dependent C, D, E, K, H, and V coefficients as vectors, one for each coefficient. The defaults are:

Coefficient	Parameters	Default Values
K	[ p_Kx1 p_Kx2 p_Kx3 ]	[ 21.51 -0.163 0.245 ]

Coefficient	Parameters	Default Values
Н	[ p_Hx1 p_Hx2 ]	[ -0.002 0.002 ]
V	[ p_Vx1 p_Vx2 ]	[00]
С	p_Cx1	1.685
D	[ p_Dx1 p_Dx2 ]	[ 1.21 -0.037 ]
E	[ p_Ex1 p_Ex2 p_Ex3 p_Ex4 ]	[ 0.344 0.095 -0.02 0 ]

### **Velocity threshold**

The wheel hub velocity  $V_{\rm th}$  below which the slip calculation is modified to avoid singular evolution at zero velocity. Must be positive. The default is 0.1.

From the drop-down list, choose units. The default is meters per second (m/s).

## See Also

### **Simscape Blocks**

Tire (Friction Parameterized) | Tire (Magic Formula) | Tire (Simple)

## **Topics**

"Complete Vehicle Model"

## Tire (Simple)

No-slip tire model with minimal parameters



## Library

Simscape / Driveline / Tires & Vehicles

## **Description**

The block represents a simple, no-slip model of a tire parameterized by its radius. The model assumes an infinite torque transfer capability.

Connection A is a mechanical rotational conserving port associated with the axle of the tire. Connection H is a mechanical translational conserving port associated with the hub of the tire.

You can optionally add inertia, stiffness, or damping. These dynamics require additional computation and might make the model less suitable for real-time simulation.

## **Assumptions and Limitations**

- The tire does not slip.
- There is an infinite torque transfer capability.

### **Ports**

Port	Description
A	Conserving mechanical rotational port associated with the axle of the tire
Н	Conserving mechanical translational port associated with the hub of the tire

## **Parameters**

### **Rolling radius**

The rolling radius of the tire. The rolling radius must be greater than zero. Default is  $0.3\,$  m.

### **Compliance**

Specifies whether the model includes longitudinal stiffness and damping.

- No compliance suitable for HIL simulation (Default) Does not include longitudinal stiffness and damping.
- Specify stiffness and damping Includes longitudinal stiffness and damping. Exposes the Longitudinal stiffness and Longitudinal damping parameters.

## Longitudinal stiffness

The longitudinal stiffness of the tire. The parameter must be greater than zero. Default is  $1e6\,$  N/m.

The **Longitudinal stiffness** parameter appears if the **Compliance** parameter is Specify stiffness and damping.

## Longitudinal damping

The longitudinal damping of the tire. The parameter must be greater than zero. Default is 100 N/(m/s).

The **Longitudinal damping** parameter appears if the **Compliance** parameter is Specify stiffness and damping.

#### Inertia

Specifies whether the model includes tire inertia.

- No inertia (Default) Does not include tire inertia.
- Specify inertia and initial velocity Includes tire inertia and initial velocity. Exposes the **Tire inertia** and **Initial velocity** parameters.

#### Tire inertia

The rotational inertia of the tire. The parameter must be greater than zero. Default is  $1 \text{ kg*/m^2}$ .

The **Tire inertia** parameter appears if the **Inertia** parameter is **Specify inertia** and initial velocity.

### **Initial velocity**

The initial rotational velocity of the tire. Default is 0 rad/s.

The **Initial velocity** parameter appears if the **Inertia** parameter is **Specify** inertia and initial velocity.

## **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, set the **Parameters** > **Compliance** parameter to No compliance - Suitable for HIL simulation.

## See Also

### **Simscape Blocks**

Tire (Friction Parameterized) | Tire (Magic Formula) | Tire-Road Interaction (Magic Formula)

## **Topics**

- "Complete Vehicle Model"
- "Vehicle with Four-Wheel Drive"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

## **Torque Converter**

Viscous fluid coupling between rotating driveline shafts

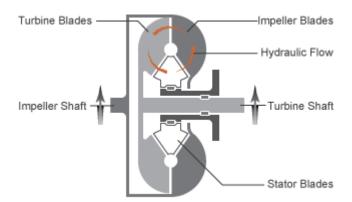


## Library

Simscape / Driveline / Couplings & Drives

## **Description**

A torque converter couples two driveline axes, transferring torque and angular motion by the hydrodynamic action of a viscous fluid. Unlike a friction clutch, a torque converter cannot lock the axes together. The Torque Converter block acts between the two ports I and T. The block acts as a lookup function of the relative angular velocity of the two connected driveline axes. This function is defined at discrete angular velocities. For model details, see "Torque Converter Model" on page 1-434.



### **Ports and Conventions**

The impeller or pump port I and turbine port T are rotational conserving ports.

The Torque Converter block follows these conventions:

- The impeller port I is the port that connects to the engine, and the turbine port T is the port that connects to the load. In normal operation, power thus flows from the impeller to the turbine.
- Forward power flow implies power flowing from I to T. Reverse power flow implies power flowing from T to I.
- The power input is through the shaft with the larger speed. The power output is through the shaft with the smaller speed.

## **Parameters**

## **Torque Characteristics**

### **Speed ratio vector**

Vector of values of the independent variable, the dimensionless speed ratio  $R_{\omega}$ . You must order these values in ascending order.

### Torque ratio vector

Vector of values of the block function's first dependent variable, the dimensionless torque ratio  $R_{\tau}$ . Each torque ratio value corresponds to a speed ratio value.

## Capacity factor parameterization

Definition of the capacity factor, either K (ratio of impeller speed  $\omega_I$  to square root of impeller torque  $\tau_I$ ) or  $K^*$  (ratio of  $\tau_I$  to  $\omega_I^2$ ). The default is K.

## Capacity factor reference speed

Choice of speed in the capacity factor definition, depending on speed ratio  $R_{\omega}$ . Select either:

- Impeller speed  $\omega_{\rm I}$  for all values of  $R_{\omega}$ .
- Impeller speed  $\omega_{\rm I}$  for  $R_{\omega} < 1$ , and turbine speed  $\omega_{\rm T}$  for  $R_{\omega} > 1$ .

### Capacity factor vector

Vector of values of the block function's second dependent variable, the torque conversion capacity factor K. Each capacity factor value corresponds to a speed ratio value.

From the drop-down list, choose units.

- If you choose the default capacity factor definition K, the default units are radians/ second/ $\sqrt{\text{(newton-meters)}(\text{rad/s/(N*m)}^0.5)}$ .
- If you choose the alternative capacity factor definition  $K^*$ , the default units are newton-meters/(radians/second)<sup>2</sup> (N\*m/(rad/s)^2).

### **Interpolation method**

Interpolates torque ratio and capacity factor functions between discrete relative velocity values within the range of definition. The default is Linear.

### **Extrapolation method**

Extrapolates torque ratio and capacity factor functions outside the range of definition. The default is Linear.

## **Dynamics**

### Model transmission lag

Select how to model transmission lag from input to output driveshaft. The default is Specify time constant and initial torque.

- No lag Suitable for HIL simulation Torque transfer is instantaneous.
- Specify time constant and initial torque ratio Torque is transferred with a time lag. If you select this option, the panel changes from its default.

### **Time Constant and Initial Torque Ratio**

## Torque transmission time constant

Dynamic torque transfer time constant  $t_c$ . The default is 0.02.

From the drop-down list, choose units. The default is seconds (s).

## Initial turbine-to-impeller torque ratio

Ratio of turbine torque  $\tau_T$  to impeller torque  $\tau_I$  at the start of the simulation.

## **Torque Converter Model**

The torque converter is a mechanism for transferring torque between impeller and turbine shafts. Because the coupling of I and T occurs by viscous action, the torque transfer depends on the difference  $\omega = \omega_{\rm T} - \omega_{\rm I} \neq 0$ , or the speed ratio  $R_\omega \neq 1$ . In normal operation, the two axes have different speeds, and the output axis speed never exactly reaches the input axis speed. The torque transfer is largest when  $R_\omega \to 0$  or  $\infty$ , and shrinks as  $R_\omega \to 1$ . Because  $R_\omega$  can never reach exactly one, a torque converter always transfers some torque.

## Speed Ratio, Torque Ratio, and Capacity Factor

You specify the torque ratio and the capacity factor of the torque converter as discrete functions of the speed ratio with tabular vector entries. The three vectors of the variable values must have the same length.

• The speed ratio  $R_{\omega}$  is the turbine angular speed divided by the impeller angular speed:

$$R_{\omega} = \omega_{\rm T}/\omega_{\rm I}$$
.

• The torque ratio  $R_{\tau}$  is the output (turbine) torque divided by the input (impeller) torque:

$$R_{\rm T} = \tau_{\rm T}/\tau_{\rm I}$$
.

- The capacity factor K or  $K^*$  is defined in two ways for  $R_{\omega} < 1$ , with either the default or the alternative definition:
  - Default, the input speed divided by the square root of the input torque:

$$K=\omega_{\rm I}\,/\,\sqrt{\tau_{\rm I}}\;.$$

• Alternative, the input torque divided by the square of the input speed:

$$K^* = \tau_{\rm I} / \omega^2_{\rm I}$$
.

• The capacity factor reference speed for  $R_{\omega} > 1$  is  $\omega_{\rm I}$  by default. That is, the input speed  $\omega_{\rm I}$  is used in the ratio that defines either K or  $K^*$ .

For  $R_{\omega} > 1$ , the alternative choice for reference speed is to replace  $\omega_{\rm I}$  by the output speed  $\omega_{\rm T}$  in this defining ratio.

The two dependent variables,  $R_{\tau}$  and K, are functions of the independent variable  $R_{\omega}$ . They specify the characteristics of the torque converter:

$$R_{\tau} = R_{\tau}(R_{\omega})$$
 ,  $K = K(R_{\omega})$  .

If you do not specify capacity factor data for a speed ratio of 1, the block uses a capacity factor value of  $10*K_{\rm Max}$ , where  $K_{\rm Max}$  is the maximum value in the specified capacity factor vector. The corresponding torque ratio is assumed to be 0. For all other speed ratio values not explicitly specified in the lookup table data, the block uses the interpolation or extrapolation method selected in the block dialog box.

## **Instantaneous Torque Transfer**

When there is no time lag, the input impeller (I) and output turbine (T) torques are:

$$au_{\rm I} = {\rm sgn}(1 - \omega_{\rm T}/\omega_{\rm I}) \cdot [\omega_{\rm I} \, / \, K]^2$$
 ,  $au_{\rm T} = au_{\rm I} \cdot R_{\tau}$  ,

in normal operation (forward power flow).

## **Lagged Torque Transfer**

You can optionally include the effect of torque transmission time lag, caused by internal fluid flow and compressibility. Instead of  $\tau_T$  and  $\tau_I$  being instantaneously constrained to one another, a first-order time lag introduces a delayed response in the impeller torque:

$$t_c \cdot (d\tau_I/dt) + \tau_I = \tau_I(\text{steady state})$$
.

The preceding instantaneous function of the capacity factor K determines the steady-state value of  $\tau_{\text{I}}$ .

## Limitations

The impeller shaft must always rotate in a positive direction. Simulation is not valid for  $\omega_{\rm I}$  < 0.

If you drive the Torque Converter from a torque source, such as the Generic Engine, you must include an inertia in the source, to represent the engine, shaft inertia, or other source components. To ensure that the impeller starts by rotating in a positive direction, set the initial speed for this inertia to a positive value.

## **Torque Transmission Time Lag**

Torque converters lag in their response to changing input torque. By default, Torque Converter includes no time lag in its response. You can include a response lag by specifying a time constant. Time lag simulation increases model fidelity but reduces simulation performance. See "Adjust Model Fidelity".

## **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, for the **Dynamics** > **Model transmission lag** parameter, select No lag - Suitable for HIL simulation.

## Reference

Society of Automotive Engineers, *Hydrodynamic Drive Test Code (Surface Vehicle Recommended Practice)*, SAE J643, May 2000.

## **See Also**

### Simscape Blocks

Disk Friction Clutch | Fundamental Friction Clutch | Generic Engine

## **Topics**

- "Complete Vehicle Model"
- "Vehicle with Four-Speed Transmission"
- "Vehicle with Four-Wheel Drive"
- "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

## **Torque Noise Source**

Model zero-mean normally (Gaussian) distributed torque **Library:** Sources



## **Description**

The Torque Noise Source block generates zero-mean normally (Gaussian) distributed torque using the Random Number source in the Simscape Foundation library. The torque produced by the block depends on two factors:

- The noise power spectral density input to the block
- A random number seed that you control using the Repeatability and, as applicable,
   Seed parameters

The defining equation for the torque that the block generates is

$$T = \sqrt{PSD/2} \, \frac{N(0,1)}{\sqrt{h}},$$

#### where:

- *T* is the output torque.
- *PSD* is the single-sided noise power spectral density.
- N is a Gaussian random number with zero mean and standard deviation of one.
- *h* is the sampling interval.

## **Ports**

## Input

### P - Single-sided noise power spectral density

physical signal

The power spectral density (PSD) of noise is the average noise power per unit of bandwidth, in  $(N*m)^2/Hz$ .

## Conserving

#### **B** — Base interface

mechanical rotational

Mechanical rotational conserving port associated with the base interface.

### F — Follower interface

mechanical rotational

Mechanical rotational conserving port associated with the follower interface.

## **Parameters**

### Sample time — Time step period and offset

1e-3 s (default) | [step, offset] s

The values of the time step period and the initial time offset. If you specify a scalar value for step, the block assumes an offset value of 0. To specify a nonzero value for the initial time offset, specify the parameter values using the vector [step, offset]. The offset value must be less than the step value and greater than or equal to zero.

### Repeatability — Random number seed control

Not repeatable (default) | Repeatable | Specify seed

The random number seed is the number that initializes the random number generator. The seed is  $\theta$  or a positive integer. To control the random number seed, set this parameter to:

• Not repeatable — The seed changes every time you simulate your model. The block resets the random seed using the MATLAB random number generator command:

```
seed = randi(2^32-1);
```

Repeatable — The seed is the same random number at the start of every simulation.
 The block sets the value using the same MATLAB random number generator command used by the Not repeatable parameter.

When you add a Torque Noise Source block to your model from the Sources library, the block generates and stores a random value for the repeated seed. When you make a copy of the Torque Noise Source block from an existing block in a model, the copy generates a new random value for the repeated seed.

Specify seed — The seed is a number that you specify using the Seed parameter.
 The Seed parameter is only available when you choose Specify seed for the Repeatability parameter.

## Seed — Random number generation seed value

0 (default)

The seed must be 0 or a positive integer. This parameter is only available when you select Specify seed for the **Repeatability** parameter.

## See Also

### **Simscape Blocks**

Force Noise Source | Random Number | Rotational Velocity Noise Source | Sinusoidal Torque Source | Translational Velocity Noise Source

#### **Functions**

randi

#### Introduced in R2016b

## **Torsional Spring-Damper**

Rotational spring and damper coupling, with Coulomb friction, locking, and hard stops



## Library

Simscape / Driveline / Couplings & Drives

## **Description**

The Torsional Spring-Damper block represents a dynamic element that imposes a combination of internally generated torques between the two connected driveshaft axes, the rod and the case. The complete torque includes these components:

- · Linear damped spring
- Coulomb friction (including locking static friction)
- Hard-stop compliance

The second and third components are optional.

The Torsional Spring-Damper block uses the models of these blocks:

Block	Contribution	Library
Loaded-Contact Rotational Friction	Coulomb friction	Simscape / Driveline / Brakes & Detents / Rotational
Rotational Damper, Rotational Spring	Damping	Simscape / Foundation Library / Mechanical /
Rotational Spring	Spring	Rotational Elements
Rotational Hard Stop	Hard stop	

## **Assumptions and Limitations**

• Including hard-stop and Coulomb friction enhances model fidelity, but reduces simulation speed. For more information, see "Driveline Simulation Performance".

## **Ports**

## Conserving

C

Mechanical rotational port associated with the slider that travels between stops installed on the case.

R

Mechanical rotational port associated with the rod.

## **Parameters**

## **Spring-Damper**

### **Restoring spring stiffness**

Torsional spring stiffness k acting between connected driveshafts. The default is 1000 N\*m/rad. The value must be greater than zero.

#### Viscous friction coefficient

Torsional damping  $\mu$  acting between the connected driveshafts. The default is 10 N\*m/(rad/s). The value must be greater than or equal to zero.

### **Coulomb friction torque**

Constant kinetic friction torque  $\tau_K$  acting between connected driveshafts. The default is  $\theta$  N\*m. The value must be greater than or equal to zero.

#### Ratio of static to kinetic friction

Constant ratio R of static Coulomb friction torque  $\tau_S$  to kinetic Coulomb friction torque  $\tau_K$  acting between connected driveshafts. The default is 1.1. The value must be greater than or equal to one.

### Velocity tolerance

Minimum relative angular speed  $\omega_{Tol}$  below which the two connected driveshafts can lock and rotate together. The default is 0.001 rad/s. The value must be greater than zero

## **Hard Stops**

### **Hard stop**

Include or exclude hard-stop torque by selecting one of these options:

- No hard stops Suitable for HIL simulation To enhance simulation speed by excluding the hard-stop torque contribution, select this default option.
- Compliant hard stops To enhance model fidelity by including the hard-stop torque contribution, select this option. Selecting this option enables other parameters.

### Upper bound

Upper hard-stop angular displacement  $\delta_+$  from the zero-torque reference angle  $\phi = 0$ . The default is 10 deg. The value must be greater than  $\delta_-$ .

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

#### Lower bound

Lower hard-stop angular displacement  $\delta_{-}$  from the zero spring force reference angle  $\phi$  = 0. The default is -10 deg. The value must be less than  $\delta_{+}$ .

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

#### **Contact stiffness**

Hard-stop stiffness  $k_{HS}$  applied if the relative angle  $\phi$  moves into the hard-stop region. The default is 1e6. N\*m/rad. The value must be greater than or equal to zero.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

### **Contact damping**

Hard-stop damping  $\mu_{HS}$  applied if the relative angle  $\phi$  moves into the hard-stop region. The default is 10 N\*m/(rad/s). The value must be greater than zero.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

### Hard stop model

Select the hard-stop model:

- Stiffness and damping applied smoothly through transition region, damped rebound Specify a transition region, in which the torque is scaled from zero. At the end of the transition region, the full stiffness and damping are applied. This model has damping applied on the rebound, but it is limited to the value of the stiffness torque. In this sense, damping can reduce or eliminate the torque provided by the stiffness, but never exceed it. All equations are smooth and produce no zero crossings.
- Full stiffness and damping applied at bounds, undamped rebound
   — This model has full stiffness and damping applied with impact at upper and lower bounds, with no damping on the rebound. Equations produce no zero crossings when velocity changes sign, but there is a position-based zero crossing at the bounds. Having no damping on rebound helps to push the slider past this position quickly. This model has nonlinear equations.
- Full stiffness and damping applied at bounds, damped rebound —
   This model has full stiffness and damping applied with impact at upper and lower
   bounds, with damping applied on the rebound as well. Equations are switched
   linear, but produce position-based zero crossings. Use this hard stop model if
   simscape.findNonlinearBlocks indicates that this is the block that prevents
   the whole network from being switched linear.

Selecting Compliant hard stops for the **Hard stop** parameter enables this parameter.

### **Transition region**

Region where the torque is ramped up from zero to the full value. At the end of the transition region, the full stiffness and damping are applied. The default value is 0.001 rad.

Selecting Stiffness and damping applied smoothly through transition region, damped rebound for the **Hard stop model** enables this parameter.

### **Initial Conditions**

#### **Initial deformation**

Initial deformation of the torsional spring relative to the zero-torque reference angle  $\phi=0.$  The default is 0 deg.

## **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Hard Stops** > **Hard stop** parameter default setting, No hard stops - Suitable for HIL simulation.

## See Also

### **Simscape Blocks**

Loaded-Contact Rotational Friction | Rotational Damper | Rotational Hard Stop | Rotational Spring

## **Topics**

"Gear Coupling Control Using Clutches"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

## **Translational Damper**

Faultable linear translational damper **Library:** Couplings & Drives / Springs & Dampers

RTC.

## **Description**

The Translational Damper block models a faultable linear translational viscous damper. From the start of the simulation, the block uses the nominal damping coefficient. If you enable faults for the block, the damping coefficient changes in response to one or both of these triggers:

- Simulation time A fault occurs at a specified time.
- Simulation behavior If the magnitude of the translational acceleration exceeds a specified maximum value, the block increments the number of shocks by one. A fault occurs if the number of shocks exceeds a specified maximum number of shocks.

If a fault trigger event occurs, the block uses the faulted damping coefficient for the remainder of the simulation. You can program the block to issue a fault report as a warning or error message.

The defining equations are

$$F = Dv$$

and

$$v = v_R - v_C$$
,

where

- F is the force transmitted through the damper.
- *D* is the damping (viscous friction) coefficient.
- *v* is the relative velocity.

•  $v_R$  and  $v_C$  are the absolute velocities of terminals R and C, respectively.

The positive block direction is from port R to port C. Therefore, the torque is positive if it acts in the direction from R to C.

## **Ports**

## Conserving

### R — Rod interface

mechanical translational

Mechanical translational conserving port associated with the rod interface.

#### C — Case interface

mechanical translational

Mechanical translational conserving port associated with the case interface.

## **Parameters**

#### Main

# Damping coefficient — Damping coefficient for the no-fault condition 100 N/(m/s) (default)

The oscillation-reducing force due to viscous friction that the block applies if no trigger events occur. Specify a value that is greater than or equal to zero.

#### **Faults**

## Enable faults — Fault mode capability

No (default) | Yes

To enable the block to use a different damping coefficient based on the simulation time or when the magnitude of the translational acceleration exceeds the specified number of shocks, select Yes.

### **Dependencies**

Selecting Yes makes these parameters visible:

- Faulted damping coefficient
- Enable temporal fault trigger
- Enable behavioral fault trigger
- Reporting when fault occurs

# Faulted damping coefficient — Damping coefficient for the fault condition 1e6 N/(m/s) (default)

The oscillation-reducing force due to viscous friction that the block applies if a trigger event occurs. Specify a value that is greater than or equal to zero.

### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

# **Enable temporal fault trigger — Fault trigger capability**Disabled (default) | Enabled

To use the faulted damping coefficient starting at a specified time in the simulation, select Enabled.

### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

Selecting Enabled makes the Simulation time for fault event parameter visible.

# **Simulation time for fault event — Temporal fault trigger** 5 s (default)

Specify the time during the simulation that you want the block to start using the faulted damping coefficient.

#### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter and **Enabled** for the **Enable temporal fault trigger** parameter.

# **Enable behavioral fault trigger — Fault trigger capability**Disabled (default) | Enabled

To use the faulted damping coefficient when the number of sustained shocks exceeds a specified maximum number of shocks, select Enabled.

### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

Selecting Enabled makes these parameters visible:

- Maximum permissible acceleration
- Maximum number of shocks

# Maximum permissible acceleration — Behavioral fault trigger 10 m/s^2 (default)

The maximum value that the magnitude of the translational acceleration can reach without causing the block to increment the number of sustained shocks.

### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter and **Enabled** for the **Enable behavioral fault trigger** parameter.

# Maximum number of shocks — Behavioral fault trigger 1 (default)

The maximum number of shocks that can be sustained without triggering the block to use the faulted damping coefficient.

### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter and **Enabled** for the **Enable behavioral fault trigger** parameter.

### Reporting when fault occurs — Fault reporting

None (default) | Warning | Error

Select your reporting preference for the fault condition.

### **Dependencies**

This parameter is only visible if you select Yes for the **Enable faults** parameter.

## **See Also**

Nonlinear Rotational Damper | Nonlinear Translational Damper | Rotational Damper | Variable Rotational Damper | Variable Translational Damper

Introduced in R2016b

## **Translational Detent**

Double-sided, spring-loaded translational detent



## Library

Brakes & Detents/Translational

## **Description**

The Translational Detent block represents a double-sided, spring-loaded translational detent with a ball and conical notch.

The detent slider slides horizontally over the detent case. These two parts develop a horizontal shear force between them. The inside of the slider is the conical notch. The detent case contains a vertical spring. The detent ball lies between the spring and the conical notch. With the block, you can model ball and angled notch detents with geometric and spring characteristics, peak force and notch width, or a lookup table. The model also includes viscous damping and kinetic friction between the slider and case. You can set the friction to zero.

### **Ports**

R and C are translational conserving ports associated with the slider and case, respectively.

### **Parameters**

### **Detent Characteristics**

#### **Parameterization**

Select how to specify the detent characteristics. The default is By peak force and notch width.

• By peak force and notch width — Specify detent characteristics by the peak shear force and the notch width.

#### **Peak Force and Notch Width**

#### Peak force

The peak shear force developed inside the detent. The default is 10.

From the drop-down list, choose units. The default is newtons (N).

#### Notch width

The width of the region where the shear force develops. The default is 30.

From the drop-down list, choose units. The default is millimeters (mm).

• By lookup table — Define the detent characteristics by one-dimensional table lookup based on the relative displacement between the slider and case. If you select this option, the panel changes from its default option.

### **Lookup Table**

### Relative displacement vector

Specify the vector of input relative displacements that correspond to the values in **Force vector**. These two vectors must be of the same size. The displacements must be specified in strictly increasing order. The default values are [-15 -12.3 -7.6 -1.1 1.1 7.6 12.3 15].

From the drop-down list, choose units. The default is millimeters (mm).

### **Force vector**

Specify the vector of input values for the shear force that correspond to the values in **Relative displacement vector**. The default values are [0 0 -8.365 -5.87 5.87 8.365 0 0].

From the drop-down list, choose units. The default is newtons (N).

### Interpolation method

Select one of these interpolation methods to approximate the output value when the input value is between two consecutive grid points:

- Linear Select this, default, option to get the best performance.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

• By geometry — Define the detent characteristics by ball-notch geometry and dynamics. If you select this option, the panel changes from its default option.

### **Geometric and Spring Parameters**

#### Ball diameter

Specify the diameter of the ball. The default is 12.

From the drop-down list, choose units. The default is millimeters (mm).

### Notch angle

Specify the full angle of the notch. Must be greater than 0 and less than or equal to 179 degrees. The default is 120.

From the drop-down list, choose units. The default is degrees (deg).

## Notch depth

Specify the depth of the notch in the slider. Must be greater than zero. The default is 4.5.

From the drop-down list, choose units. The default is millimeters (mm).

#### **Preload force**

Specify the force to which the detent spring is preloaded. Must greater than or equal to 0. The default is 15.

From the drop-down list, choose units. The default is newtons (N).

## Spring stiffness

Specify the stiffness of the detent spring. Must be greater than 0. The default is 3000.

From the drop-down list, choose units. The default is newtons/meter (N/m).

### Shear reversal region

Specify the width of the region where the ball moves from one notch face to the other. Must be greater than 0. The default is 0.1.

From the drop-down list, choose units. The default is millimeters (mm).

### **Initial relative position**

The relative displacement of the slider and case when simulation starts. The default is  $\theta$ .

From the drop-down list, choose units. The default is millimeters (mm).

### **Friction**

#### Viscous friction coefficient

Specify the viscous friction coefficient for the ball-notch contact. Must be greater than or equal to 0. The default is 0.1.

From the drop-down list, choose units. The default is newtons/(meters/second) (N/(m/s)).

### Friction to peak force ratio

Specify the kinetic friction coefficient for the ball-notch contact. Must be greater than or equal to 0. The default is 0.01.

The kinetic friction is this ratio multiplied by the peak shear force.

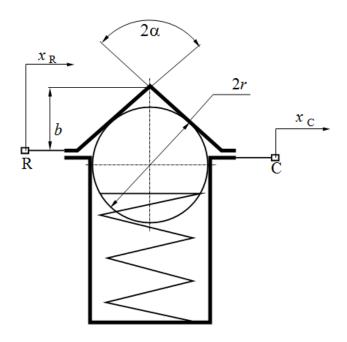
## Friction velocity threshold

Specify the relative velocity required for peak kinetic friction in the detent. Must be greater than 0. The default is 0.05.

From the drop-down list, choose units. The default is meters/second (m/s).

## **Translational Detent Model**

The geometry of the ball-notch detent is shown in the following figure. As the conical slider slides horizontally over the case, the relative displacement  $x = x_R - x_C$  causes a horizontal shear force F to develop.

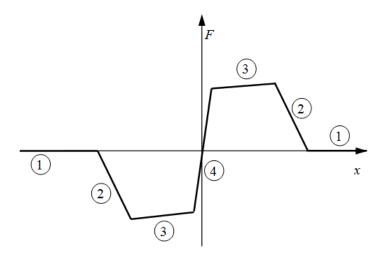


b	Notch depth
r	Ball radius
α	Notch half angle

Depending on your choice of parameterization, the shear force model is defined by geometric and spring parameters, by the peak force and notch width, or by a lookup table specifying relative displacement versus force.

## **Geometric and Spring Parameters**

The geometric and spring parameterization uses four regions to define the shear force. The following figure displays these regions.



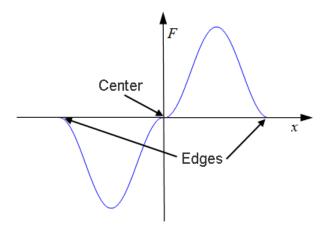
Because the ball is spherical and the notch is symmetric, the horizontal force versus displacement function is symmetric about the origin. (See "Peak Force and Notch Width" on page 1-455.)

Re gio n	Ball Position and Contact Angle	Shear Force
1	Ball is outside conical notch. Contact angle is vertical.	Viscous damping and kinetic friction only. No spring contribution.
2	Ball is entering notch, in contact with notch corner. Contact angle rotates from vertical.	Spring, viscous damping, and kinetic friction contributions. Peaks at transition from region 2 to region 3.
3	Ball slides along face of notch. Contact angle is constant.	Force decreases as spring extends, but does not go to zero (spring preload force).
4	Ball moves from one face to the other. Contact angle switches direction.	Force switches direction. Shear reversal region width controls how smooth this switch is.

## **Peak Force and Notch Width**

If you choose the peak force and notch width parameterization, the block ensures that the force-relative displacement curve provides a continuous force and force derivative over

the detent region. The peak forces are halfway between the detent center and detent edge, as shown in the following figure.



## **Lookup Table**

With the lookup table parameterization, you can create an arbitrary function relating shear force to relative displacement. If you create such a function, consider the following best practices.

If you want to ensure that the detent conserves energy, the total integral of the force-relative displacement curve (area under the curve) must be zero.

To stabilize simulation of the detent, avoid discontinuities in the force-relative displacement function. The most important requirement is to have a shear reversal region of nonzero width, analogous to region 4 in the geometric parameterization.

## Limitations

The model does not account for inertia. Add mass terms externally to the R and C ports as required.

If you use the peak force-notch width or the lookup table parameterization, the kinetic friction is independent of the detent normal force.

## **See Also**

Loaded-Contact Translational Friction | Rotational Detent

## **Topics**

"Clutches, Clutch-Like Elements, and Coulomb Friction"

<sup>&</sup>quot;Stepping Mechanism with Detents"

## **Translational Power Sensor**

Mechanical sensor used to measure average or instantaneous translational power



## Library

Sensors

## **Description**

The block represents a sensor that measures the translational power change due to one or more driveline components connected between ports R and C. The power output can be an instantaneous or average value. Two averaging options are available: period and vibration averaging.

The instantaneous power is the product of the current velocity and force. Use the instantaneous power to analyze peak power transmission and identify heavily loaded components.

The time-averaged power is the integral of the instantaneous power over one sample period, divided by that period. For simulation times smaller than the sample period, the average power is zero. The power is constant for each sample period.

The vibration-averaged power is the integral of the power over one vibration period, divided by that period. The vibration period is the time between two consecutive crossings from negative to positive velocity values. Use this averaging method only for oscillations with velocity passing through zero. If the vibration has a variable frequency, the averaging period can change. For simulation times smaller than the vibration period, the average power is zero. The power output is constant for each vibration period.

## **Parameters**

### **Measurement Type**

Select either instantaneous or average power measurement. The default type is Instantaneous Power.

- Instantaneous power Output the power measured for the current time step.
- Average power over a specified period— Output the power averaged over a fixed time period.

## **Averaging period**

Enter the time period used to compute the average power. Typical values include the cycle length of a reciprocating device or the actuation force.

The default value is 1. The default unit is s.

Average power over a vibration— Output the power averaged over one vibration period.

### Maximum vibration frequency

Enter the maximum vibration frequency over which to average the power. Very high values can reduce simulation speed. Very low values can result in lower power measurements.

The default value is 1000. The default unit is Hz.

## **Ports**

Port	Description
P	Physical signal output port for translational power
S	Mechanical translational conserving port associated with driving source
R	Mechanical translational conserving port associated with loaded driveline components
С	Mechanical translational conserving port associated with case holding loaded driveline components

# **See Also**

Rotational Power Sensor

Introduced in R2013a

## **Translational Velocity Noise Source**

Produce zero-mean normally (Gaussian) distributed translational velocity **Library:** Sources



## **Description**

The Translational Velocity Noise Source block generates zero-mean normally (Gaussian) distributed translational velocity using the Random Number source in the Simscape Foundation library. The translational velocity produced by the block depends on two factors:

- The noise power spectral density input to the block
- A random number seed that you control using the Repeatability and, as applicable,
   Seed parameters

The defining equation for the translational velocity that the block generates is

$$v = \sqrt{PSD/2} \frac{N(0,1)}{\sqrt{h}},$$

#### where:

- *v* is the output translational velocity.
- PSD is the single-sided noise power spectral density.
- ullet N is a Gaussian random number with zero mean and standard deviation of one.
- *h* is the sampling interval.

## **Ports**

## Input

### P - Single-sided noise power spectral density

physical signal

The power spectral density (PSD) of noise is the average noise power per unit of bandwidth, in  $(m/s)^2/Hz$ .

## Conserving

#### **B** — Base interface

mechanical translational

Mechanical translational conserving port associated with the base interface.

#### F — Follower interface

mechanical translational

Mechanical translational conserving port associated with the follower interface.

## **Parameters**

### Sample time — Time step period and offset

1e-3 s (default) | [step, offset] s

The values of the time step period and the initial time offset. If you specify a scalar value for step, the block assumes an offset value of 0. To specify a nonzero value for the initial time offset, specify the parameter values using the vector [step, offset]. The offset value must be less than the step value and greater than or equal to zero.

### Repeatability — Random number seed control

Not repeatable (default) | Repeatable | Specify seed

The random number seed is the number that initializes the random number generator. The seed is  $\theta$  or a positive integer. To control the random number seed, set this parameter to:

• Not repeatable — The seed changes every time you simulate your model. The block resets the random seed using the MATLAB random number generator command:

```
seed = randi(2^32-1);
```

• Repeatable — The seed is the same random number at the start of every simulation. The block sets the value using the same MATLAB random number generator command used by the Not repeatable parameter.

When you add a Translational Velocity Noise Source block to your model from the Sources library, the block generates and stores a random value for the repeated seed. When you make a copy of the Translational Velocity Noise Source block from an existing block in a model, the copy generates a new random value for the repeated seed.

Specify seed — The seed is a number that you specify using the Seed parameter.
 The Seed parameter is only available when you choose Specify seed for the Repeatability parameter.

## Seed — Random number generation seed value

0 (default)

The seed must be  $\theta$  or a positive integer. This parameter is only available when you select Specify seed for the **Repeatability** parameter.

## See Also

### **Simscape Blocks**

Force Noise Source | Random Number | Rotational Velocity Noise Source | Sinusoidal Translational Velocity Source | Torque Noise Source

#### **Functions**

randi

#### Introduced in R2016b

# **Unbalanced Load**

Load with angle-dependent rotational inertia



# Library

Inertias & Loads

# **Description**

This block models the effects of a load whose rotational inertia varies instantaneously with the rotation angle. Examples include the wobbling of a spinning axle and shaking of an off-center rotating machine. You can specify the load inertia in terms of its rotation path or as an angle-inertia lookup table.

The block provides two rotation path parameterizations. One assumes circular motion of the unbalanced load. The other assumes elliptical motion. In each case, the distance between the unbalanced load and the main rotation axis varies with the rotation angle. The varying distance causes the moment of inertia, given by the parallel-axis theorem, to vary during rotation:

$$I(\theta) = I_0 + Mr^2(\theta),$$

#### where:

- *I* is the moment of inertia about the main rotation axis.
- $I_0$  is the moment of inertia about the intrinsic rotation axis of the unbalanced load.
- *M* is the total mass of the unbalanced load.
- r is the distance between the unbalanced load and the main rotation axis.

The angle dependence of the moment of inertia leads to an angle dependence of the inertial torque acting on the unbalanced load:

$$T_I(\theta) = I(\theta)\dot{\omega},$$

where:

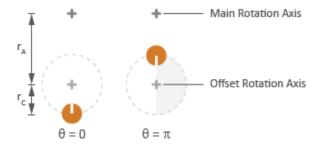
- $T_{\rm I}$  is the inertial torque.
- $\omega$  is the angular velocity of the load.

If the load moves in a circular path, its distance to the main rotation axis is given by

$$r(\theta) = \sqrt{\left(r_{C} cos(\theta) + r_{A}\right)^{2} + \left(r_{C} sin(\theta)\right)^{2}} \,, \label{eq:reduced}$$

where:

- $r_{\rm A}$  is the distance between the main rotation axis and the offset rotation axis.
- $r_{\rm C}$  is the radius of the circular path.



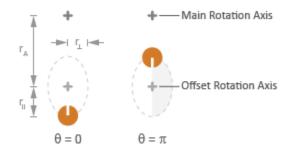
#### **Circular Rotation Path**

If the load moves in an elliptical path, its distance to the main rotation axis is given by

$$r(\theta) = \sqrt{\left(r_{||}cos(\theta) + r_{A}\right)^{2} + \left(r_{\perp}sin(\theta)\right)^{2}}\,,$$

where:

- $r_{\parallel}$  is the radius of the elliptical path in line with the distance from the main rotation axis.
- $r_{\perp}$  is radius of the elliptical path perpendicular to the distance from the main rotation axis.



**Elliptical Rotation Path** 

### **Parameters**

#### Inertia

#### **Parameterization**

Choice of parameterization for modeling the moment of inertia of the unbalanced load. Options include Circular rotation, Elliptical rotation, and Specify table lookup. The default setting is Circular rotation.

Select Circular rotation or Elliptical rotation to parameterize the load inertia in terms of the load's rotation path. Select Specify table lookup to provide the load inertia directly across its rotation path.

#### Moment of inertia about own axis

Moment of inertia about the intrinsic rotation axis of the unbalanced load. This moment of inertia is assumed constant throughout simulation. This parameter appears only when **Parameterization** is set to Circular rotation. The default value is 1 kg\*m2.

#### Mass

Mass of the unbalanced load. This parameter appears only when **Parameterization** is set to Circular rotation. The default value is 1 kg.

#### Distance from axis to center of rotation

Distance between the main rotation axis and the center of the rotation path. This parameter appears only when **Parameterization** is set to Circular rotation. The default value is 0.01 m.

#### Radius of rotation

Radius of the circular rotation path traversed by the unbalanced load. This parameter appears only when **Parameterization** is set to Circular rotation. The default value is 0.01 m.

#### Radius of rotation inline with distance from axis

Length of the semimajor axis of the elliptical rotation path traversed by the unbalanced load. The semimajor axis is in line with the line segment joining the main rotation axis and the elliptical rotation center. This parameter appears only when **Parameterization** is set to Elliptical rotation. The default value is 0.01 m.

#### Radius of rotation perpendicular to distance from axis

Length of the semiminor axis of the elliptical rotation path traversed by the unbalanced load. The semiminor axis is perpendicular to the line segment joining the main rotation axis and the elliptical rotation center. This parameter appears only when **Parameterization** is set to Elliptical rotation. The default value is  $0.005 \, \text{m}$ .

### **Angle vector**

Array of angular positions at which to specify the load inertia. The block calculates the load inertia between the angles specified using linear interpolation. This parameter appears only when **Parameterization** is set to Specify table lookup. The default vector is [0,pi,3\*pi/2] rad.

#### Inertia vector

Array of load inertias about the intrinsic rotation axis of the load. Each inertia corresponds to an angle specified in the **Angle vector** parameter. This parameter appears only when **Parameterization** is set to **Specify table lookup**. The default vector is [1,10,1] kg\*m^2.

#### **Initial Conditions**

#### Initialization

Choice of parameter through which to specify the initial state of the unbalanced load. Options include Specify angular momentum and Specify angular velocity.

#### Initial angular momentum

Angular momentum of the unbalanced load at the start of simulation. This parameter appears only when the **Initialization** parameter is set to Specify angular momentum. The default value is  $0 \text{ m}^2 \text{ kg/s}$ .

#### Initial angular velocity

Angular velocity of the unbalanced load at the start of simulation. This parameter appears only when the **Initialization** parameter is set to Specify angular velocity. The default value is 0 rad/s.

#### Initial angle

Angular position of the unbalanced load at the start of simulation. The initial angle determines the initial inertia of the unbalanced load. The default value is  $\theta$  rad.

## **Ports**

The block has one conserving rotational port. This port identifies the location of the unbalanced load in a driveline model.

## **See Also**

Variable Inertia | Variable Mass

# **Unidirectional Clutch**

Clutch that transmits power in a single direction



# Library

Clutches

# **Description**

The Unidirectional Clutch block models an ideal one-way clutch based on a coupled ringhub. It transmits torque when the relative velocity of hub and ring becomes positive or negative, depending on how you set the transmission direction. For model details, see "Unidirectional Clutch Model" on page 1-470.

### **Ports**

H and R are rotational conserving ports representing, respectively, the hub and ring driveshaft axes. The clutch motion is measured as the  $slip\ \omega = \omega_H - \omega_R$ , the angular velocity of hub relative to ring.

## **Parameters**

#### Transmission direction

From the drop-down list, select the relative rotation direction (sign of ) for which the clutch locks and transfers torque. The default is From hub to ring for positive rotation.

#### **Initial state**

Clutch state at the start of simulation. The clutch can be in one of two states, locked and unlocked. A locked clutch constrains the base and follower shafts to spin at the

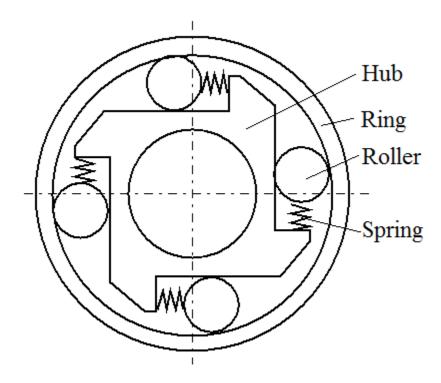
same velocity, that is, as a single unit. An unlocked clutch allows the two shafts to spin at different velocities, resulting in slip between the clutch plates. The default setting is Unlocked.

## **Unidirectional Clutch Model**

The Unidirectional Clutch, if locked, transmits torque from hub to ring. If it is unlocked, it transmits no torque. The clutch does not have a state of being unlocked but still engaged (transmitting torque).

## **Clutch Geometry, Variable, and State Summary**

The figure displays the geometry of the unidirectional clutch. The table summarizes the unidirectional clutch variables.



#### **Clutch Variable**

Symbol	Definition	Significance
ω	Relative angular velocity (slip)	$\omega_{\mathrm{H}}$ – $\omega_{\mathrm{R}}$

The Unidirectional Clutch block implements an ideal model of a one-way clutch and does not include any internal dynamics, such as the rollers and springs.

The transmission direction determines the condition for locking.

• If you choose transmission for the positive direction, the clutch locks if  $\omega = \omega_H - \omega_R \ge 0$  and becomes zero from positive values. The slip  $\omega$  then remains zero, and the clutch transfers torque.

If the driveline dynamics then causes  $\omega < 0$  at a later time, the clutch abruptly unlocks and stops transferring torque.

• If you choose transmission for the negative direction, the clutch locks if  $\omega = \omega_H - \omega_R \le 0$  and becomes zero from negative values. The slip  $\omega$  then remains zero, and the clutch transfers torque.

If the driveline dynamics then causes  $\omega > 0$  at a later time, the clutch abruptly unlocks and stops transferring torque.

For example, locking and torque transfer in the positive direction as follows.

- When the hub rotates faster than the ring ( $\omega > 0$ ), the small gap prearranged between the hub and the ring is cleared. The spring-loaded rollers wedge between the hub and the ring, causing the two to contact, lock, and rotate together;  $\omega$  resets to zero. (The rotation convention in the figure is clockwise.)
- If the ring rotates faster than the hub ( $\omega$  < 0), the rollers are pushed out of contact and the clutch unlocks.

For a clutch schematic, see "Clutch Geometry, Variable, and State Summary" on page 1-470.

The unidirectional clutch is ideal and does not dissipate power. Either the clutch is unlocked and applies no kinetic friction, or it is locked (no slip) and applies only static friction.

# **Example**

The sdl\_stepping\_mechanism example model uses the Unidirectional Clutch to translate a mass in one direction only (ratcheting).

# See Also

Dog Clutch | Fundamental Friction Clutch

# **Topics**

"Gear Coupling Control Using Clutches"

"Ratchet Leadscrew Mechanism"

# **Universal Joint**

Rotational coupling between two driveline shafts



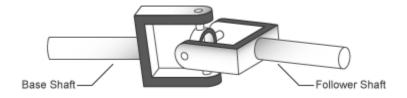
# Library

Couplings & Drives

# **Description**

This block represents a rotational coupling between two driveline shafts. The coupling transfers torque between the shafts so they spin as a unit under an applied load. Two rotational degrees of freedom, internal to the coupling, allow the shafts to connect at an angle. This intersection angle varies according to the physical signal input from port A. Compliance, modeled as a parallel spring-damper set, allows the coupling to deform under load.

You can use the Universal Joint block as a connection between two rotational driveline components—for example, between the driving and driven shafts in an automobile drive train.



The ratio of the shaft angular velocities depends on two parameters: the intersection angle between the two shafts and the rotation angle of the base shaft. A physical signal

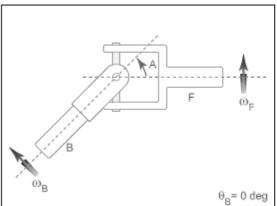
input provides the intersection angle while a dialog box parameter provides the initial base shaft angle. These two angles fix the ratio of the two shaft angular velocities according to the nonlinear equation:

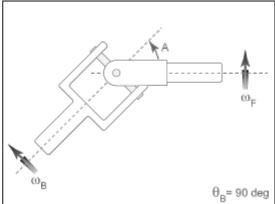
$$\omega_F = \frac{\cos(A)}{1 - \sin^2(A) \cdot \cos^2(\theta_B)} \, \omega_B,$$

#### where:

- $\omega_F$  is the angular velocity of the follower shaft about its length axis.
- $\omega_B$  is the angular velocity of the base shaft about its length axis.
- $\theta_B$  is the rotation angle of the base shaft about its length axis.
- A is the intersection angle between base and follower shafts about the base shaft pin.

The two schematics in the figure illustrate the equation parameters. In each schematic, the left shaft represents the base shaft, while the right shaft represents the follower shaft. The right schematic shows the coupling seen in the left schematic after the shafts spin 90° about their length axes (dashed line segments).





In the figure, the intersection angle is the angle between the two shafts about the pin of the base shaft. The absolute value of this angle must fall in the range  $0 \le A < Ma \times imum$  intersection angle. The base shaft angle is the angle of the base shaft about its length axis. The base shaft angle is also the time-integral of the base shaft angular velocity,  $\omega_B$ .

### **Parameters**

#### Maximum joint angle

Maximum intersection angle the joint allows. This angle measures the rotation between base and follower shafts about the base shaft pin. The value of this angle must fall in the range $0 \le A < pi/2$ . From the drop-down list, select a physical unit. The default value is pi/4 rad.

#### Joint stiffness

Linear spring stiffness of the joint. The spring stiffness accounts for elastic energy storage in the joint due to material compliance. In the drop-down list, select a physical unit. The default value is 1e6 N\*m/rad.

#### Joint damping

Linear damping coefficient of the joint. The damping coefficient accounts for energy dissipation in the joint due to material compliance. In the drop-down list, select a physical unit. The default value is 1e3 N\*m/(rad/s).

### Initial base shaft angle

Rotation angle of the base shaft about its length axis at time zero. From the drop-down list, select a physical unit. The default value is  $\theta$  rad.

### Initial torque from base to follower shaft

Torque that the base shaft transfers to the follower shaft at time zero. This torque determines the initial state of material compliance at the joint. Set this value to greater than zero to preload the shafts with torque. Changing this value alters the initial transient response due to material compliance. Select a physical unit. The default value is 0 N\*m.

### **Ports**

Port	Description	
В	Conserving rotational port associated with the base shaft	
F	Conserving rotational port associated with the follower shaft	
A	Physical signal input port for the intersection angle	

# **See Also**

Belt Drive | Belt Pulley | Chain Drive | Flexible Shaft | Rope Drum

# **Variable Inertia**

Time-varying inertia specified as physical signal input



# Library

Inertias & Loads

# **Description**

This block models the effects of a time-varying inertia. Components with variable inertia include satellites unfolding arrays of solar panels. A physical signal input port provides the instantaneous inertia at each time step throughout simulation. To minimize solver errors, avoid discontinuities and abrupt changes in the input signal.

As the component inertia changes, so does the inertial torque acting on that component:

$$T_I = I\dot{\omega},$$

where:

- $T_{\rm I}$  is the inertial torque.
- *I* is the variable inertia.
- $\omega$  is the angular velocity of the inertia.

The physical signal input saturates at the minimum inertia specified in the block dialog box. Whenever the input falls below the minimum inertia, the block performs its calculations on the minimum inertia instead. The inertial torque becomes:

$$T_I = I_{Min}\dot{\omega},$$

#### where:

•  $I_{Min}$  is the minimum inertia allowed.

The angular momentum of the variable inertia is conserved. In the absence of external torques, a decrease in the moment of inertia leads to a proportional increase in angular velocity. The angular momentum remains constant until a net external torque causes it to change.

#### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

# **Ports**

The block has one conserving rotational port and one physical signal input port. The conserving rotational port identifies the driveline component whose inertia varies with time. The physical signal input port provides the means to specify the inertia as a function of time.

## **Parameters**

#### Minimum inertia

Lowest value that the variable inertia can take on during simulation. The physical signal input saturates at this value. If the input falls below the minimum inertia, it is set equal to the minimum inertia value. The default value is  $0.1 \text{ kg*m}^2$ .

## See Also

Unbalanced Load | Variable Mass

# **Variable Mass**

Time-varying mass specified as physical signal input



# Library

Inertias & Loads

# **Description**

This block models the effects of a time-varying mass. Components with variable mass include fuel tanks with progressively lower fuel contents. A physical signal input port provides the instantaneous mass at each time step throughout simulation. To minimize solver errors, avoid discontinuities and abrupt changes in the input signal.

As the component mass changes, so does the inertial force acting on that component:

$$F_I = m\dot{v},$$

where:

- $F_{I}$  is the inertial force.
- *m* is the variable mass.
- *v* is the velocity of the mass.

The physical signal input saturates at the minimum mass specified in the block dialog box. Whenever the input falls below the minimum mass, the block performs its calculations on the minimum mass instead. The inertial force becomes:

$$F_I=m_{Min}\dot{v},$$

#### where:

•  $m_{\rm Min}$  is the minimum mass allowed.

The linear momentum of the variable mass is conserved. In the absence of external forces, a decrease in mass leads to a proportional increase in linear velocity. The linear momentum remains constant until a net external force causes it to change.

#### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

### **Ports**

The block has one conserving translational port and one physical signal input port. The conserving translational port identifies the driveline component whose mass varies with time. The physical signal input port provides the means to specify the mass as a function of time.

## **Parameters**

#### Minimum mass

Lowest value that the variable mass can take on during simulation. The physical signal input saturates at this value. If the input falls below the minimum mass, it is set equal to the minimum mass value. The default value is  $0.1 \, \text{kg}$ .

### See Also

Unbalanced Load | Variable Inertia

# **Variable Ratio Transmission**

Dynamic gearbox with variable and controllable gear ratio, transmission compliance, and friction losses



# Library

Simscape / Driveline / Couplings & Drives

# **Description**

The Variable Ratio Transmission block represents a gearbox that dynamically transfers motion and torque between the two connected driveshaft axes, base and follower.

Ignoring the dynamics of transmission compliance, the driveshafts are constrained to corotate with a variable gear ratio that you control. You can choose whether the follower axis rotates in the same or opposite direction as the base axis. If they rotate in the same direction,  $\omega_F$  and  $\omega_B$  have the same sign. If they rotate in opposite directions,  $\omega_F$  and  $\omega_B$  have opposite signs.

Transmission compliance introduces internal time delay between the axis motions. Therefore, unlike a gear, a variable ratio transmission does not act as a kinematic constraint. You can also control torque loss caused by transmission and viscous bearing losses. For model details, see "Variable Ratio Transmission Model" on page 1-482.

### **Ports**

B and F are rotational conserving ports representing, respectively, the base and follower driveshafts.

You specify the unitless variable gear ratio  $g_{FB}(t)$  as a function of time at the physical signal input at port r. If the signal value becomes zero or negative, the simulation stops with an error.

## Variable Ratio Transmission Model

## **Ideal Motion and Torque Transfer**

Variable Ratio Transmission is a dynamical mechanism for transferring motion and torque between base and follower.

If the relative compliance  $\phi$  between the axes is absent, the block is equivalent to a gear with a variable ratio  $g_{\rm FB}(t)$ . Such a gear imposes a time-dependent kinematic constraint on the motions of the two driveshafts:

$$\omega_{\rm B} = \pm g_{\rm FB}(t) \cdot \omega_{\rm F}$$
 ,  $\tau_{\rm F} = \pm g_{\rm FB}(t) \cdot \tau_{\rm B}$  .

However, Variable Ratio Transmission does include compliance between the axes. Dynamical motion and torque transfer replace the kinematic constraint, with a nonzero  $\phi$  that dynamically responds through base compliance parameters  $k_{\rm p}$  and  $k_{\rm v}$ :

$$\begin{split} d\phi/dt &= \pm g_{\rm FB}(t) \cdot \omega_{\rm F} - \omega_{\rm B} \;, \\ \tau_{\rm B} &= -k_{\rm p}\phi - k_{\rm v}d\phi/dt \;, \\ \pm g_{\rm FB}(t) \cdot \tau_{\rm B} + \tau_{\rm F} - \tau_{\rm loss} = 0 \;. \end{split}$$

 $\tau_{\rm loss} = 0$  in the ideal case.

- You can estimate the base angular compliance  $k_{\rm p}$  from the transmission time constant  $t_{\rm c}$  and inertia J:  $k_{\rm p} = J(2\pi/t_{\rm c})^2$ .
- You can estimate the base angular velocity compliance  $k_v$  from the transmission time constant  $t_c$ , inertia J, and damping coefficient C:  $k_v = (2Ct_c)/2\pi = 2C\sqrt{(J/k_p)}$ .

### **Nonideal Torque Transfer and Losses**

With nonideal torque transfer,  $\tau_{loss} \neq 0$ . Losses in the Variable Ratio Transmission are modeled similarly to how losses are modeled in nonideal gears. For general information on nonideal gear modeling, see "Model Gears with Losses".

In a nonideal gearbox, the angular velocity and compliance dynamics are unchanged. The transferred torque and power are reduced by:

- Coulomb friction (for example, between belt and wheel, or internal belt losses due to stretching) characterized by an efficiency  $\eta$ .
- Viscous coupling of driveshafts with bearings, parametrized by viscous friction coefficients  $\mu$ .

$$\tau_{\rm loss} = \tau_{\rm Coul} \cdot \tanh(4\omega_{\rm out}/\omega_{\rm th}) + \mu_{\rm B}\omega_{\rm B} + \mu_{\rm F}\omega_{\rm F}$$
,  $\tau_{\rm Coul} = |\tau_{\rm F}| \cdot (1 - \eta)$ .

When the angular velocity changes sign, the hyperbolic tangent regularizes the sign change in the Coulomb friction torque.

Power Flow	Power Loss Condition	Output Driveshaft $\omega_{ ext{out}}$
Forward	$\omega_{\rm B} \tau_{\rm B} > \omega_{\rm F} \tau_{\rm F}$	Follower, $\omega_{ ext{F}}$
Reverse	$\omega_{\rm B} \tau_{\rm B} < \omega_{\rm F} \tau_{\rm F}$	Base, $\omega_{\mathrm{B}}$

## **Meshing Efficiency**

The friction loss represented by efficiency  $\eta$  is fully applied only if the absolute value of the follower angular velocity  $\omega_F$  is greater than a velocity threshold  $\omega_{th}$ .

If this absolute velocity is less than  $\omega_{\rm th}$ , the actual efficiency is automatically regularized to one at zero velocity.

## **Parameters**

### Main

### **Output shaft rotates**

From the drop-down list, choose how the output driveshaft rotates relative to the input driveshaft. The default is In same direction as input shaft.

## **Compliance**

#### Transmission stiffness at base (B)

Reciprocal of transmission angular compliance  $k_{\rm p}$ , angular displacement per unit torque, measured at the base. The default is 30000.

From the drop-down list, choose units. The default is newton-meters/radian (N\*m/rad).

#### Transmission damping at base (B)

Reciprocal of transmission angular compliance damping  $k_v$ , angular speed per unit torque, measured at the base. The default is 0.05.

From the drop-down list, choose units. The default is newton-meters/(radian/second) (N\*m/(rad/s)).

#### Initial input torque at base (B)

Torque applied at the base driveshaft at the start of simulation (t = 0). The default is  $\theta$ .

From the drop-down list, choose units. The default is newton-meters (N\*m).

### **Transmission Losses**

#### Losses model

Select how to implement friction losses from nonideal torque transfer. The default is No losses.

- No losses Suitable for HIL simulation Torque transfer is ideal.
- Constant efficiency Transfer of torque across gearbox is reduced by a constant efficiency  $\eta$  satisfying  $0 < \eta \le 1$ . If you select this option, the panel changes from its default.

### **Constant Efficiency**

### **Efficiency**

Effective torque transfer efficiency  $\eta$  between the base and follower driveshafts.

### Follower angular velocity threshold

Absolute angular velocity threshold  $\omega_{th}$  above which full efficiency loss is applied, for follower velocity  $\omega_F$ .

From the drop-down list, choose units. The default is radians/second (rad/s).

## **Viscous Bearing Losses**

#### Viscous friction coefficients at base (B) and follower (F)

Vector of viscous damping coefficients  $[\mu_B \mu_F]$  applied at the base and follower driveshafts, respectively. The default is  $[0\ 0\ ]$ .

From the drop-down list, choose units. The default is newton-meters/(radian/second) (N\*m/(rad/s)).

# **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Transmission Losses > Losses model** parameter default setting, No losses - Suitable for HIL simulation.

## See Also

### **Simscape Blocks**

Simple Gear | Torque Converter

## **Topics**

"Gear Coupling Control Using Clutches"

"Variable Ratio Gear"

"Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Variable Rotational Damper**

Rotational damper with variable damping coefficient



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a rotational viscous damper with a variable damping coefficient. A physical signal input port provides the magnitude of the damping coefficient. The magnitude of the damping torque is equal to the product of the physical signal input and the relative angular velocity between the two rotational conserving ports, R and C. A minimum damping coefficient prevents non-physical negative damping values.

The damping torque satisfies the following expression:

$$T = \begin{cases} B \cdot \omega & B \ge B_{\min} \\ B_{\min} \cdot \omega & B < B_{\min} \end{cases},$$

The parameters are:

- ullet T- Torque transmitted through damper
- $\bullet \quad B- \hbox{Viscous damping coefficient}$
- $\omega$  Relative angular velocity measured between the two rotational conserving ports according to  $\omega=\omega_R-\omega_C$
- $\omega_{\text{R}}$  Angular velocity of rotational conserving port R
- $\omega_{\it C}$  Angular velocity of rotational conserving port C

The block applies equal and opposite damping torques on the rotational conserving ports. The sign of the damping torque acting on port R is equal to the sign of the relative angular velocity. A positive relative angular velocity corresponds to a positive damping torque acting on port R, and a negative damping torque of equal magnitude acting on port C.

## **Assumptions and Limitations**

- The block represents only viscous damping
- The value of the damping coefficient must be equal to or greater than zero.

## **Ports**

В

Physical signal input port representing the variable damping coefficient.

C

Rotational conserving port.

R

Rotational conserving port.

## **Parameters**

### Minimum damping coefficient

Minimum value allowed for the damping coefficient. The physical signal input saturates below this level. The parameter must be greater than or equal to zero. The default value is  $0 \, N*m/(rad/s)$ .

## See Also

Nonlinear Rotational Damper | Nonlinear Translational Damper | Rotational Damper | Translational Damper | Variable Translational Damper

# **Variable Rotational Spring**

Rotational spring with variable spring stiffness



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a torsional spring with variable spring stiffness. A physical signal input port provides the value of the variable spring stiffness. The magnitude of the spring torque is equal to the product of the physical signal input and the relative angular displacement between the two rotational conserving ports. A minimum spring rate value prevents non-physical values.

The rotational spring torque satisfies the following expression:

$$T = \begin{cases} K \cdot \theta & K \geq K_{\min} \\ K_{\min} \cdot \theta & K < K_{\min} \end{cases},$$

The parameters are:

- *T* Torque transmitted through the spring
- K Spring rate (stiffness)
- $K_{min}$  Minimum allowable spring rate (stiffness)
- $\theta$  Relative angular displacement measured between the two rotational conserving ports according to  $\theta=\theta_{init}+\theta_R-\theta_C$
- $oldsymbol{ heta}_{ ext{init}}$  Initial angular deformation between the two rotational conserving ports

- $\theta_R$  Absolute angular displacement of rotational conserving port R
- $\theta_{\rm C}$  Absolute angular displacement of rotational conserving port C

The block applies equal and opposite spring torques on the two rotational conserving ports. The sign of the spring torque acting on port R is equal to the sign of the relative angular velocity. A positive relative angular velocity corresponds to a positive damping torque acting on port R, and a negative damping torque of equal magnitude acting on port C.

#### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

## **Assumptions and Limitations**

The value of the spring rate must be greater than zero.

## **Ports**

K

Physical signal input port representing the variable spring stiffness.

C

Rotational conserving port.

R

Rotational conserving port.

## **Parameters**

### Minimum spring rate

Minimum value allowed for the spring rate (stiffness). The physical signal input saturates below the specified value. The parameter must be greater than zero. The default value is 0.01. The default unit is (N\*m/rad).

# See Also

Nonlinear Rotational Spring | Nonlinear Translational Spring | Variable Translational Spring

# Variable Translational Damper

Translational viscous damper with variable damping coefficient



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a translational viscous damper with variable damping coefficient. A physical signal input port provides the magnitude of the translational damping coefficient. The magnitude of the damping force is equal to the product of the physical signal input and the relative linear velocity between the two translational conserving ports. A minimum damping coefficient prevents non-physical negative damping values.

The translational damping force satisfies the following expression:

$$F = \begin{cases} B.v, & B \ge B_{\min} \\ B_{\min} \cdot v, & B < B_{\min} \end{cases},$$

The parameters are:

- ${\it F}$  Force transmitted through the translational damper between the two translational conserving ports
- B Viscous damping coefficient
- $B_{min}$  Minimum allowed damping coefficient
- $\nu$  Relative linear velocity measured between the two translational conserving ports
- $v_R$  Linear velocity of port R

v<sub>C</sub> — Linear velocity of port C

The block applies equal and opposite damping forces on the two translational conserving ports. The sign of the damping force acting on port R is equal to the sign of the relative linear velocity. A positive linear velocity corresponds to a positive damping force acting on port R, and a negative damping force of equal magnitude acting on port C.

## **Assumptions and Limitations**

- The block represents strictly viscous damping.
- The value of the damping coefficient must be greater than or equal to zero.

## **Ports**

В

Physical signal input port representing the variable translational damping coefficient.

C

Translational conserving port.

R

Translational conserving port.

### **Parameters**

### Minimum damping coefficient

Minimum value allowed for the variable damping coefficient. The physical signal input saturates below the specified value. The parameter must be greater than or equal to zero. The default value is  $0 \, N/(m/s)$ .

## See Also

Nonlinear Rotational Damper | Nonlinear Translational Damper | Rotational Damper | Translational Damper | Variable Rotational Damper

# **Variable Translational Spring**

Translational spring with variable spring stiffness



# Library

Couplings & Drives/Springs & Dampers

# **Description**

The block represents a translational spring with variable spring stiffness. A physical signal input port provides the variable spring stiffness. The magnitude of the spring force is equal to the product of the physical signal input and the relative linear displacement between the two translational conserving ports. A minimum spring rate prevents non-physical values.

The translational spring force satisfies the following expression:

$$F = \begin{cases} K \cdot x, & K \ge K_{\min} \\ K_{\min} \cdot x & K < K_{\min} \end{cases},$$

The parameters are:

- F Force transmitted through the spring between the two translational conserving ports
- K Spring rate (stiffness)
- $K_{min}$  Minimum allowed spring rate (stiffness)
- $\bullet$  x Relative displacement between the two translational conserving ports according

to 
$$x = x_{init} + x_R - x_C$$

- $x_{init}$  initial spring deformation
- x<sub>R</sub> Absolute displacement of translational conserving port R
- x<sub>C</sub> Absolute displacement of translational conserving port C

The block applies equal and opposite spring forces on the two translational conserving ports. The sign of the spring force acting on port R is equal to the sign of the relative linear displacement between the two ports. A positive linear velocity corresponds to a positive spring force acting on port R, and a negative spring force of equal magnitude acting on port C.

#### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

# **Assumptions and Limitations**

The value of the variable spring stiffness must be greater than zero.

## **Ports**

K

Physical signal input port representing the variable spring stiffness.

C

Translational conserving port.

R

Translational conserving port.

# **Parameters**

### Minimum spring rate

Minimum value allowed for the spring rate. The physical signal input saturates below the specified value. The parameter must be greater than zero. The default value is  $1\,$  N/m.

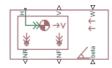
# See Also

Nonlinear Rotational Spring | Nonlinear Translational Spring | Variable Rotational Spring

# **Vehicle Body**

Two-axle vehicle with longitudinal dynamics and motion and adjustable mass, geometry, and drag properties

**Library:** Simscape / Driveline / Tires & Vehicles



# **Description**

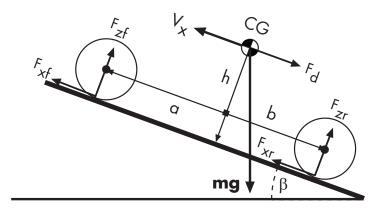
The Vehicle Body block represents a two-axle vehicle body in longitudinal motion. The vehicle can have the same or a different number of wheels on each axle. For example, two wheels on the front axle and one wheel on the rear axle. The vehicle wheels are assumed identical in size. The vehicle can also have a center of gravity (CG) that is at or below the plane of travel.

The block accounts for body mass, aerodynamic drag, road incline, and weight distribution between axles due to acceleration and road profile. Optionally include pitch and suspension dynamics. The vehicle does not move vertically relative to the ground.

### Model

The vehicle axles are parallel and form a plane. The longitudinal, x, direction lies in this plane and perpendicular to the axles. If the vehicle is traveling on an incline slope,  $\beta$ , the normal, z, direction is not parallel to gravity but is always perpendicular to the axlelongitudinal plane.

This figure and table define the vehicle motion model variables.



**Vehicle Dynamics and Motion** 

### **Vehicle Model Variables**

Symbol	Description
g	Gravitational acceleration
β	Incline angle
m	Mass of the vehicle
h	Height of vehicle center of gravity (CG) above the ground
a, b	Distance of front and rear axles, respectively, from the normal projection point of vehicle CG onto the common axle plane
$V_{x}$	Velocity of the vehicle. When $V_x > 0$ , the vehicle moves forward. When $V_x < 0$ , the vehicle moves backward.
$V_w$	Wind speed. When $V_w > 0$ , the wind is headwind. When $V_w < 0$ , the wind is tailwind.
n	Number of wheels on each axle
$F_{xf}$ , $F_{xr}$	Longitudinal forces on each wheel at the front and rear ground contact points, respectively
$F_{zf}$ , $F_{zr}$	Normal load forces on each wheel at the front and rear ground contact points, respectively
A	Effective frontal vehicle cross-sectional area
$C_d$	Aerodynamic drag coefficient
ρ	Mass density of air
$F_d$	Aerodynamic drag force

## **Equations**

The vehicle motion is a result of the net effect of all the forces and torques acting on it. The longitudinal tire forces push the vehicle forward or backward. The weight mg of the vehicle acts through its center of gravity (CG). Depending on the incline angle, the weight pulls the vehicle to the ground and pulls it either backward or forward. Whether the vehicle travels forward or backward, aerodynamic drag slows it down. For simplicity, the drag is assumed to act through the CG.

$$m\dot{V}_x = F_x - F_d - mg \cdot \sin\beta$$

$$F_x = n(F_{xf} + F_{xr})$$

$$F_d = \frac{1}{2}C_d\rho A(V_x + V_w)^2 \cdot \operatorname{sgn}(V_x + V_w)$$

Zero normal acceleration and zero pitch torque determine the normal force on each front and rear wheel.

$$F_{zf} = \frac{-h(F_d + mg\sin\beta + m\dot{V}_x) + b \cdot mg\cos\beta}{n(a+b)}$$

$$F_{zr} = \frac{+h(F_d + mg\sin\beta + m\dot{V}_x) + a \cdot mg\cos\beta}{n(a+b)}$$

The wheel normal forces satisfy  $F_{zf} + F_{zr} = mg \frac{\cos\beta}{n} \, . \label{eq:fitting}$ 

The rate of the pitch that occurs during vehicle acceleration depends on three torque components and the inertia of the vehicle:

$$\alpha = \frac{(f \cdot h) + (F_{zf}a) - (F_{zr}b)}{I}$$

Where:

- $\alpha$  is the pitch rate.
- *f* is the longitudinal force.
- *J* is the inertia.

If you choose a linear model for suspension stiffness and damping, the block uses small angle approximation for pitch calculations. If you choose a table lookup model, the block uses the vectors that you specify calculate pitch dynamics. For hard stop equations, see Translational Hard Stop.

#### **Variables**

Use the **Variables** tab to set the priority and initial target values for the block variables before simulating. For more information, see "Set Priority and Initial Target for Block Variables" (Simscape).

Unlike block parameters, variables do not have conditional visibility. The **Variables** tab lists all the existing block variables. If a variable is not used in the set of equations corresponding to the selected block configuration, the values specified for this variable are ignored.

## **Limitations and Assumptions**

The Vehicle Body block lets you model only longitudinal dynamics, parallel to the ground and oriented along the direction of motion. The vehicle is assumed to be in pitch and normal equilibrium. The block does not model pitch or vertical movement. As such, the equations assume that the wheels never lose contact. This constraint can result in negative normal forces.

## **Ports**

### Input

#### W — Headwind speed

scalar

Physical signal input port for headwind speed.

#### beta — Road incline angle

scalar

Physical signal input port for road incline angle.

### **Output**

#### V — Longitudinal velocity

scalar

Physical signal output port for vehicle longitudinal velocity.

#### NF — Front axle normal force

scalar

Physical signal output port for normal force on the front axle. Wheel forces are considered positive if acting downwards.

#### NR — Rear axle normal force

scalar

Physical signal output port for normal force on the rear axle. Wheel forces are considered positive if acting downwards.

## Conserving

#### **H** — Horizontal motion

mechanical translational

Conserving port associated with the horizontal motion of the vehicle body. Connect tire traction motion to this port.

## **Parameters**

#### Main

Mass — Vehicle mass

1200 kg (default)

Mass of the vehicle.

#### Number of wheels per axle — Wheel count

2 (default) | scalar number or a two-element array

Wheel counts on the front and rear axles. If the input is a scalar number, the wheel counts of the front and rear axles are assumed the same. For example, if the input is 2, then the front and rear axles are each assumed to have two wheels.

If the input is a two-element array, the first number is the front-axle wheel count and the second number the rear-axle wheel count. For example, if the input is the array [2,1], then the front axle is assumed to have two wheels and the rear axle one wheel.

# Horizontal distance from CG to front axle — CG-to-front axle distance 1.4 m (default)

Horizontal distance, a, from the center of gravity to the front wheel axle of the vehicle.

# Horizontal distance from CG to rear axle — CG-to-rear axle distance 1.6 m (default)

Horizontal distance, b, from the center of gravity to the rear wheel axle of the vehicle.

## CG height above ground — CG-to-ground distance 0.5 m (default)

Distance, h, between the center of gravity of the vehicle and the ground.

# **Gravitational acceleration — Gravitational acceleration** 9.81 m/s^2 (default)

Acceleration due to gravitational force acting at the center of gravity of the vehicle.

## Warn on negative normal force — Warning No (default) | Yes

To see a warning when the block calculates negative values for normal force during simulation, select Yes. The block can generate negative forces because the equations assume that the wheels never lose contact.

## Drag

#### Frontal area — Effective cross-sectional area

3 m<sup>2</sup> (default)

Effective cross-sectional area, *A*, presented by the vehicle in longitudinal motion. The block uses this value to calculate the aerodynamic drag force on the vehicle.

### Drag coefficient — Aerodynamic drag coefficient

0.4 (default)

Aerodynamic drag coefficient,  $C_{\rm d}$ . The block uses this value to calculate the aerodynamic drag force on the vehicle.

#### Air density — Ambient air density

1.18 kg/m<sup>3</sup> (default)

Density of the air that surrounds the vehicle.

#### Pitch

The table shows how the visibility of some parameters depends on the option that you choose for other parameters. To learn how to read the table, see "Parameter Dependencies" on page B-2.

## **Pitch Parameter Dependencies**

Pitch	1					
Model Pitch Dynamics — Choose No or Yes						
No	Yes					
	Pitch moment of inertia					
	Suspension model — Choose Lir	near or Table Lookup				
	Linear Table Lookup					
	Front suspension stiffness Front suspension stiffness force v					
	Front suspension damping Front suspension deformation v					
	Rear suspension stiffness Front suspension damping force v					
	Rear suspension damping	Front suspension velocity vector				
		Rear suspension stiffness force vector				
		Rear suspension deformation vector				
		Rear suspension damping force vector				
		Rear suspension velocity vector				
		Interpolation method				
		Extrapolation method				
	Model hard stop — Choose No or	Yes				
	No	Yes				
		Front upper bound				
		Front lower bound				
		Front contact stiffness				
		Front contact damping				
		Rear upper bound				
	Rear lower bound Rear contact stiffness					
	Rear contact damping					
	Initial pitch					
	Initial pitch rate					

#### Model pitch dynamics — Pitch dynamics modelling

No (default) | Yes

Option to model pitch dynamics.

#### **Dependencies**

Selecting Yes for this parameter enables parameters for:

- Suspension model
- Hardstop model
- Initial pitch conditions

For more information, see the Pitch Parameter Dependencies table.

#### Pitch moment of inertia — Pitch moment of inertia

4000 kg/m<sup>2</sup> (default) | positive scalar

Moment of inertia for pitch calculations.

### **Dependencies**

This parameter is enabled when you set **Model pitch dynamics** to Yes.

For more information, see the Pitch Parameter Dependencies table.

### Suspension model — Suspension parameterization method

Linear (default) | Table lookup

Parameterization method for suspension modeling.

You parameterize the suspension using stiffness and damping data. To specify the data using scalar values, select Linear. To specify the data using vector values, select Table Lookup.

#### **Dependencies**

This parameter is enabled when you set **Model pitch dynamics** to Yes.

For more information, see the Pitch Parameter Dependencies table.

### Front suspension stiffness — Front suspension stiffness

1e4 N/m (default) | positive scalar

Front suspension stiffness per axle.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- · Model pitch dynamics to Yes
- Suspension model to Linear

For more information, see the Pitch Parameter Dependencies table.

## Front suspension damping — Front suspension damping 1e4N/(m/s) (default) | positive scalar

Front suspension damping per axle.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Linear

For more information, see the Pitch Parameter Dependencies table.

# Rear suspension stiffness — Rear suspension stiffness 1e4 N/m (default) | positive scalar

Rear suspension stiffness per axle.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Linear

For more information, see the Pitch Parameter Dependencies table.

# Rear suspension damping — Rear suspension damping 1e4N/(m/s) (default) | positive scalar

Rear suspension damping per axle.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Linear

For more information, see the Pitch Parameter Dependencies table.

# Front suspension stiffness force vector — Front suspension stiffness force [-2000, -1000, 0, 1000, 2000] N (default) | increasing vector

Stiffness force of the front suspension. Specify the output values for the lookup table as a vector. The number of elements in the output vector must be the same as the number of elements in the input vector. The input vector parameter is the **Front suspension deformation vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

# Front suspension deformation vector — Front suspension deformation [-.4, -.2, 0, .2, .4] m (default) | increasing vector

Deformation of the front suspension specified in terms of displacement. Specify the input values for the lookup table as a vector. The values of the elements in the vector must increase from left to right. The minimum number of elements in the vector depends on the interpolation method that you select. For linear interpolation, provide at least two elements. For smooth interpolation, provide at least three elements. The output vector parameter is the **Front suspension stiffness force vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

# Front suspension damping force vector — Front suspension damping force [-200, -100, 0, 100, 200] N (default) | increasing vector

Damping force of the front suspension. Specify the output values for the lookup table as a vector. The number of elements in the output vector must be the same as the number of elements in the input vector. The input vector parameter is the **Front suspension velocity vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

# Front suspension velocity vector — Front suspension velocity [-4, -2, 0, 2, 4] m/s (default) | increasing vector

Velocity of the front suspension. Specify the input values for the lookup table as a vector. The values of the elements in the vector must increase from left to right. The minimum number of elements in the vector depends on the interpolation method that you select. For linear interpolation, provide at least two elements. For smooth interpolation, provide at least three elements. The output vector parameter is the **Front suspension damping force vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- · Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

# Rear suspension stiffness force vector — Rear suspension stiffness force [-2000, -1000, 0, 1000, 2000] N (default) | increasing vector

Stiffness force of the rear suspension. Specify the output values for the lookup table as a vector. The number of elements in the output vector must be the same as the number of

elements in the input vector. The input vector parameter is the **Rear suspension deformation vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

# Rear suspension deformation vector — Rear suspension deformation [-.4, -.2, 0, .2, .4] m (default) | increasing vector

Deformation of the rear suspension specified in terms of displacement. Specify the input values for the lookup table as a vector. The values of the elements in the vector must increase from left to right. The minimum number of elements in the vector depends on the interpolation method that you select. For linear interpolation, provide at least two elements. For smooth interpolation, provide at least three elements. The output vector parameter is the **Rear suspension stiffness force vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

# Rear suspension damping force vector — Rear suspension damping force [-200, -100, 0, 100, 200] N (default) | increasing vector

Damping force of the rear suspension. Specify the output values for the lookup table as a vector. The number of elements in the output vector must be the same as the number of elements in the input vector. The input vector parameter is the **Rear suspension velocity vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

## Rear suspension velocity vector — Rear suspension velocity

[-4, -2, 0, 2, 4] m/s (default) | increasing vector

Velocity of the rear suspension. Specify the input values for the lookup table as a vector. The values of the elements in the vector must increase from left to right. The minimum number of elements in the vector depends on the interpolation method that you select. For linear interpolation, provide at least two elements. For smooth interpolation, provide at least three elements. The output vector parameter is the **Rear suspension damping force vector** parameter.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

### Interpolation method — Interpolation method

linear (default) | smooth

Interpolation methods for approximating the output value when the input value is between two consecutive grid points are:

- Linear Select this default option to get the best performance. Provide at least two values per dimension.
- Smooth Select this option to produce a continuous curve with continuous first-order derivatives. Provide at least three values per dimension.

For more information on interpolation algorithms, see the PS Lookup Table (1D) block reference page.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

#### Extrapolation method — Extrapolation method

linear (default) | smooth

Extrapolation method for determining the output value when the input value is outside the range specified in the argument list are:

- Linear Produces a curve with continuous first-order derivatives in the extrapolation region and at the boundary with the interpolation region.
- Nearest Produces an extrapolation that does not go above the highest point in the data or below the lowest point in the data.

For more information on extrapolation algorithms, see the PS Lookup Table (1D) block reference page.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Suspension model to Table lookup

For more information, see the Pitch Parameter Dependencies table.

### Model hard stop — Hard-stop modeling option

No (default) | Yes

Option to model hardstops for the front and rear suspension.

#### **Dependencies**

This parameter is enabled when you set the **Model pitch dynamics** to Yes:

Selecting Yes for this parameter enables parameters for the front and rear hardstop:

- Upper bound
- Lower bound

- Contact stiffness
- Contact damping

# Front upper bound — Hardstop front suspension upper bound . 25 (default)

Upper bound of the hardstop for the front suspension.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Front lower bound — Vehicle front lower bound - .25 (default)

Lower bound of the hardstop for the front suspension.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Front contact stiffness — Vehicle front contact stiffness 1e6 (default)

Contact stiffness of the hardstop for the front suspension.

#### **Dependencies**

This parameter is enabled when you set both of these options:

• Model pitch dynamics to Yes

#### Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Front contact damping — Vehicle front contact damping 150 (default)

Contact damping of the hardstop for the front suspension.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Rear upper bound — Vehicle rear upper bound . 25 (default)

Upper bound of the hardstop for the rear suspension.

### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Rear lower bound — Vehicle rear lower bound - .25 (default)

Lower bound of the hardstop for the rear suspension.

### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

# Rear contact stiffness — Vehicle rear contact stiffness 1e6 (default)

Contact stiffness of the hardstop for the rear suspension.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Rear contact damping — Vehicle rear contact damping 150 (default)

Contact damping of the hardstop for the rear suspension.

#### **Dependencies**

This parameter is enabled when you set both of these options:

- Model pitch dynamics to Yes
- Hardstop to Yes

For more information, see the Pitch Parameter Dependencies table.

# Initial pitch — Pitch at the beginning of the simulation 0 rad (default)

Pitch at the beginning of the simulation.

### **Dependencies**

This parameter is enabled when you set **Model pitch dynamics** to Yes.

For more information, see the Pitch Parameter Dependencies table.

# Initial pitch rate — Pitch rate at the beginning of the simulation 0 rad/s (default)

Pitch rate at the beginning of the simulation.

### **Dependencies**

This parameter is enabled when you set **Model pitch dynamics** to Yes.

For more information, see the Pitch Parameter Dependencies table.

## See Also

Tire (Friction Parameterized) | Tire (Magic Formula) | Tire (Simple) | Tire-Road Interaction (Magic Formula) | Translational Hard Stop

## **Topics**

"Complete Vehicle Model"

### Introduced in R2011b

## **Worm Gear**

Worm gear with adjustable gear ratio and friction losses



## Library

Simscape / Driveline / Gears

## **Description**

The block represents a rotational gear that constrains the two connected driveline axes, worm (W) and gear (G), to rotate together in a fixed ratio that you specify. You can choose whether the gear rotates in a positive or negative direction. Right-handed rotation is the positive direction. If the worm thread is right-handed,  $\omega_W$  and  $\omega_G$  have the same sign. If the worm thread is left-handed,  $\omega_W$  and  $\omega_G$  have opposite signs.

### **Thermal Modeling**

You can model the effects of heat flow and temperature change through an optional thermal conserving port. By default, the thermal port is hidden. To expose the thermal port, right-click the block in your model and, from the context menu, select **Simscape** > **Block choices**. Select a variant that includes a thermal port. Specify the associated thermal parameters for the component.

## **Worm Gear Model**

### **Model Variables**

$R_{ m WG}$	Gear ratio
$\omega_{ m W}$	Worm angular velocity
$\omega_{ m G}$	Gear angular velocity
α	Normal pressure angle
λ	Worm lead angle
L	Worm lead
d	Worm pitch diameter
$ au_{ m G}$	Gear torque
$ au_{ m W}$	Torque on the worm
$ au_{ m loss}$	Torque loss due to meshing friction. The loss depends on the device efficiency and the power flow direction. To avoid abrupt change of the friction torque at $\omega_G = 0$ , the friction torque is introduced via the hyperbolic function.
$ au_{ m fr}$	Steady-state value of the friction torque at $\omega_G \rightarrow \infty$ .
k	Friction coefficient
$\eta_{WG}$	Torque transfer efficiency from worm to gear
$\eta_{GW}$	Torque transfer efficiency from gear to worm
$p_{ m th}$	Power threshold
$[\mu_{\mathrm{W}} \; \mu_{\mathrm{G}}]$	Vector of viscous friction coefficients for the worm and gear

## **Ideal Gear Constraint and Gear Ratio**

Worm gear imposes one kinematic constraint on the two connected axes:

$$\omega_{\rm W}=R_{\rm WG}\omega_{\rm G}\;.$$

The two degrees of freedom are reduced to one independent degree of freedom. The forward-transfer gear pair convention is (1,2) = (W,G).

The torque transfer is:

```
R_{WG}\tau_W - \tau_G - \tau_{loss} = 0 \ , with \tau_{loss} = 0 in the ideal case.
```

#### **Nonideal Gear Constraint**

In the nonideal case,  $\tau_{loss} \neq 0$ . For general considerations on nonideal gear modeling, see "Model Gears with Losses".

In the contact friction case,  $\eta_{WG}$  and  $\eta_{GW}$  are determined by:

- The worm-gear threading geometry, specified by lead angle  $\lambda$  and normal pressure angle  $\alpha$ .
- The surface contact friction coefficient k.

```
\begin{split} &\eta_{\rm WG} = (\cos\alpha - k \cdot \tan\lambda)/(\cos\alpha + k/\tan\lambda) \;, \\ &\eta_{\rm GW} = (\cos\alpha - k/\tan\lambda)/(\cos\alpha + k \cdot \tan\lambda) \;. \end{split}
```

In the constant friction case, you specify  $\eta_{WG}$  and  $\eta_{GW}$ , independently of geometric details.

 $\eta_{\rm GW}$  has two distinct regimes, depending on lead angle  $\lambda$ , separated by the *self-locking point* at which  $\eta_{\rm GW}=0$  and  $\cos\alpha=k/\tan\lambda$ .

- In the *overhauling regime*,  $\eta_{\rm GW} > 0$ , and the force acting on the nut can rotate the screw.
- In the *self-locking regime*,  $\eta_{\rm GW} < 0$ , and an external torque must be applied to the screw to release an otherwise locked mechanism. The more negative is  $\eta_{\rm GW}$ , the larger the torque must be to release the mechanism.

 $\eta_{\rm WG}$  is conventionally positive.

## Meshing Efficiency

The efficiencies  $\eta$  of meshing between worm and gear are fully active only if the transmitted power is greater than the power threshold.

If the power is less than the threshold, the actual efficiency is automatically regularized to unity at zero velocity.

### **Viscous Friction Force**

The viscous friction coefficient  $\mu_W$  controls the viscous friction torque experienced by the worm from lubricated, nonideal gear threads and viscous bearing losses. The viscous friction torque on a worm driveline axis is  $-\mu_W \omega_W$ .  $\omega_W$  is the angular velocity of the worm with respect to its mounting.

The viscous friction coefficient  $\mu_G$  controls the viscous friction torque experienced by the gear, mainly from viscous bearing losses. The viscous friction torque on a gear driveline axis is  $-\mu_G\omega_G$ .  $\omega_G$  is the angular velocity of the gear with respect to its mounting.

### Limitations

- · Gear inertia is assumed negligible.
- Gears are treated as rigid components.
- Coulomb friction slows down simulation. See "Adjust Model Fidelity".

## **Ports**

Port	Description
W	Rotational conserving port representing the worm component
G	Rotational conserving port representing the gear component
Н	Thermal conserving port for thermal modeling

## **Parameters**

## Main

#### Gear ratio

Gear or transmission ratio  $R_{WG}$  determined as the ratio of the worm angular velocity to the gear angular velocity. The default is 25.

#### Worm thread type

Choose the directional sense of gear rotation corresponding to positive worm rotation. The default is Right-handed. If you select Left-handed, rotation of the worm in the generally-assigned positive direction results in the gear rotation in negative direction.

#### **Friction Losses**

Parameters for friction losses vary with the block variant chosen—that with a thermal port for thermal modeling or that without a thermal port.

#### Without Thermal Port

#### **Friction model**

Select how to implement friction losses from nonideal meshing of gear threads. The default is No friction losses.

- No friction losses Suitable for HIL simulation Gear meshing is ideal.
- Constant efficiency Transfer of torque between worm and gear is reduced by friction. If you select this option, the panel expands.

### **Constant Efficiency**

### Friction parametrization

Select how to characterize the friction between gear threads. The default is Friction coefficient and geometrical parameters.

• Friction coefficient and geometrical parameters — Friction is determined by contact friction between surfaces.

### Normal pressure angle

The thread pressure angle  $\alpha$  in the normal plane. Must be greater than zero and less than 90 degrees. The default is 17.5.

From the drop-down list, choose units. The default is degrees (deg).

### Lead angle

Thread helix angle  $\lambda = \arctan[L/(\pi d)]$ . L is the worm lead, d is the worm pitch diameter. Must be greater than zero. The default is 20.

From the drop-down list, choose units. The default is degrees (deg).

#### Friction coefficient

Dimensionless coefficient of normal friction in the thread. Must be greater than zero. The default is 0.08.

Efficiencies — Friction is determined by constant efficiencies 0 < η <</li>
 If you select this option, the panel changes from its default.

#### **Efficiencies**

#### Worm-gear efficiency

Efficiency  $\eta_{WG}$  of the power transfer from worm to gear.

### Gear-worm efficiency

Efficiency  $\eta_{GW}$  of the power transfer from gear to worm.

#### Power threshold

Power threshold above which full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value provided by the temperature-efficiency lookup table at the power threshold. The default value is 0.001 W.

#### With Thermal Port

### **Temperature**

Array of temperatures used to construct a 1-D temperature-efficiency lookup table. The array values must increase left to right. The temperature array must be the same size as the **Efficiency** array. The default array is [280 300 320] K.

### Worm-gear efficiency

Array of component efficiencies with the worm as the driver—that is, with power flowing from the worm to the gear. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.75 0.7 0.65].

### Gear-worm efficiency

Array of component efficiencies with the gear as the driver—that is, with power flowing from the gear to the worm. The array values are the efficiencies at the temperatures in the **Temperature** array. The two arrays must be the same size. The default array is [0.5 0.45 0.4].

#### Power threshold

Power threshold above which the full efficiency factor is in effect. A hyperbolic tangent function smooths the efficiency factor between zero at rest and the value

provided by the temperature-efficiency lookup table at the power threshold. The default value is  $0.001\,\mathrm{W}$ .

#### **Viscous Losses**

#### Viscous friction coefficients at worm (W) and gear (G)

Vector of viscous friction coefficients  $[\mu_W \mu_G]$ , for the worm and gear, respectively. The default is  $[0 \ 0]$ .

From the drop-down list, choose units. The default is newton-meters/(radians/second) (N\*m/(rad/s)).

#### **Thermal Port**

#### Thermal mass

Thermal energy required to change the component temperature by a single degree. The greater the thermal mass, the more resistant the component is to temperature change. The default value is 50 J/K.

### **Initial temperature**

Component temperature at the start of simulation. The initial temperature alters the component efficiency according to an efficiency vector that you specify, affecting the starting meshing or friction losses. The default value is 300 K.

## **Extended Capabilities**

## Real-Time and Hardware-in-the-Loop Simulation

For optimal simulation performance, use the **Friction Losses** > **Friction model** parameter default setting, No friction losses - Suitable for HIL simulation.

## See Also

### **Simscape Blocks**

Leadscrew | Sun-Planet | Sun-Planet Worm Gear

## **Topics**

- "Basic Motion, Torque, and Force Modeling"
- "Model Thermal Losses in Driveline Components"

  "Prepare Simscape Driveline Models for Real-Time Simulation Using Simscape Checks"

# **Technical Conventions**

## **Driveline Abbreviations and Conventions**

#### In this section...

"Abbreviations" on page A-2

"Angular Motion" on page A-2

"Gear Ratios" on page A-2

#### **Abbreviations**

An important abbreviation is DoF, which means *degree of freedom* and refers to one coordinate of angular motion. All driveline rotational DoFs are measured with respect to a single absolute coordinate system at rest.

## **Angular Motion**

Standard symbols for angular motion analysis include the following:

Symbol	Meaning (Units)
r	Gear radius
N	Number of gear teeth
g	Gear ratio
$\theta$	Angle
ω	Angular velocity
τ	Torque

## **Gear Ratios**

For a pair of coupled, coplanar gear wheels, the gear ratio  $g_{21}$  of gear 2 to gear 1 is defined as the ratio of the second gear wheel radius to the first. This definition is equivalent to the ratio of the number of teeth on the second gear wheel to the number of teeth on the first.

$$g_{21} \equiv r_2/r_1 = N_2/N_1$$

The gear ratio is the ratio of torques and the reciprocal of the angular velocity ratio.

$$g_{21}=\tau_2/\tau_1=\omega_1/\omega_2$$

For gear boxes made of more than two gear wheels, the gear ratio is defined to be the ratio of torques or the reciprocal of the ratio of angular velocities, between the output and input shafts.

If the gear is reversing, the output  $\omega$  and  $\tau$  have opposite signs from the input  $\omega$  and  $\tau$ .

# **Parameter Dependencies**

## **Parameter Dependencies**

A Simscape block parameter is considered *visible* when it appears in the Simulink Property Inspector, in a block dialog box, or as a block choice on the Simscape context menu. A block parameter is considered *configurable* or *enabled* when you can configure it by selecting an option, entering a value, or selecting or clearing a check box. Parameters that are visible but are not enabled are typically dimmed.

The visibility and configurability of some parameters depend on the options that you select for other parameters. Parameter dependencies are typically listed in the parameter description in the documentation for the block. For some blocks, the documentation also includes a parameter dependency table.

## **Parameter Dependency Tables**

Parameter dependency tables show how the visibility and configurability of some parameters depend on the options that you select for other parameters.

Parameter dependency tables indicate which parameter options affect the *visibility* of other parameters. For example, the next table shows the dependencies for the **Effects** and Initial Conditions parameters for the Pipe (2P) block from the **Simscape** > Foundation Library > Two-Phase Fluid > Elements library.

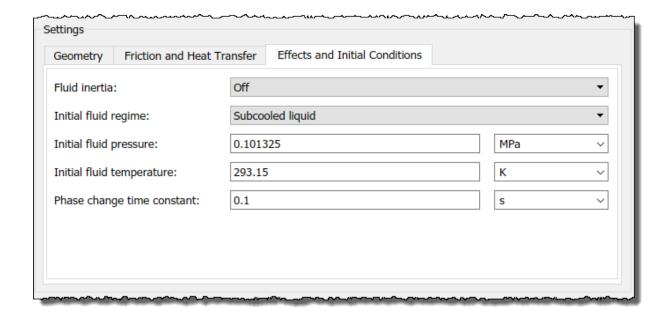
The row numbers in this table are for reference only. The first column of a parameter dependency table typically includes all parameters that are visible by default.

Parameters that affect the visibility or configurability of other parameters are shown in bold text. The options for the parameters that affect other parameters are shown in italic text in the following row of the table. Parameters that do not affect other parameters are shown in plain text.

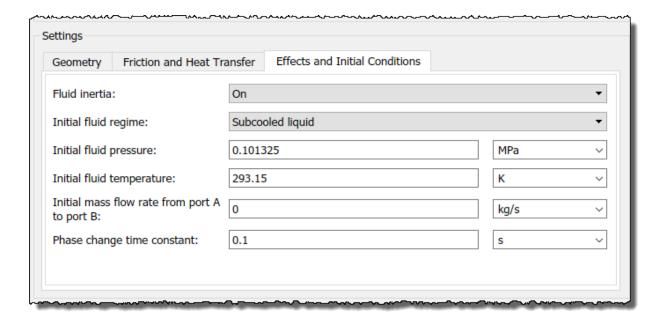
### **Effects and Initial Conditions Parameter Dependencies**

Row	Parameters and Options					
1	Fluid Inertia					
2	Off			On		
3	Initial fluid r	regime		Initial fluid regime		
4	Subcooled liquid	Two-phase mixture	Superheate d vapor	Subcooled liquid	Two-phase mixture	Superheate d vapor
5	Initial fluid pressure	Initial fluid pressure	Initial fluid pressure	Initial fluid pressure	Initial fluid pressure	Initial fluid pressure
6	Initial fluid temperature	Initial fluid vapor quality	Initial fluid temperature	Initial fluid temperature	Initial fluid vapor quality	Initial fluid temperature
7				Initial mass flow rate from port A to port B	Initial mass flow rate from port A to port B	flow rate
8	Phase change time constant	Phase change time constant	Phase change time constant	Phase change time constant	Phase change time constant	Phase change time constant

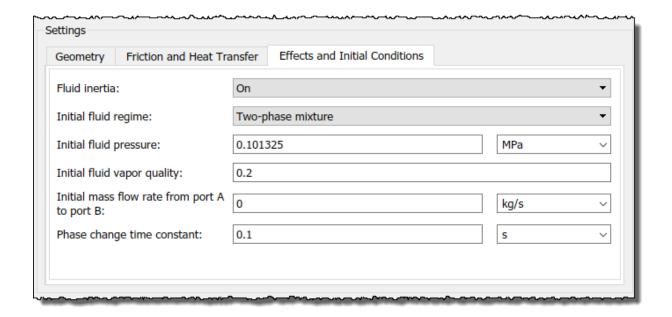
The figure shows the **Effects and Initial Conditions** parameters that are visible by default on the block dialog box for the Pipe (2P) block.



If you change the **Fluid Inertia** parameter from **Off** to **On**, the **Initial mass flow rate from port A to port B** parameter becomes visible. The table shows this dependency in rows 1, 2, and 7.



If you then change the **Initial fluid regime** parameter from **Subcooled liquid** to Two-phase mixture, the **Initial fluid temperature** parameter is hidden and **Initial fluid vapor quality** becomes visible. The table shows these dependencies in rows 3, 4, and 6.



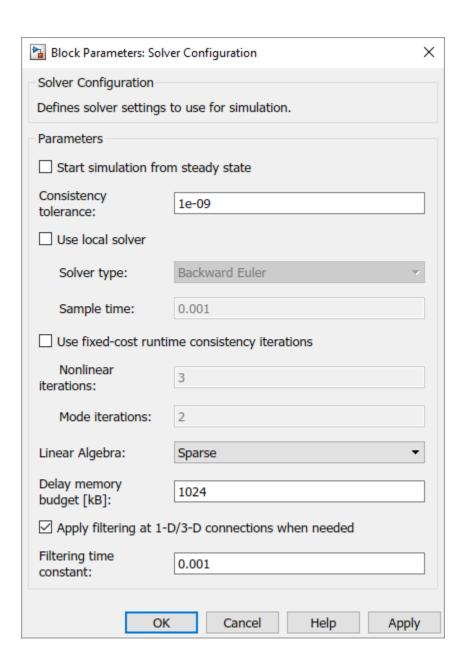
Parameter dependency tables also indicate which parameter options *enable* other parameters. For example, the next table shows the dependencies for the parameters for the Solver Configuration block from the **Simscape > Foundation Library > Utilities** library. The first column in the table contains row numbers, which are for reference only. The second column includes all parameters that are visible by default.

Parameters that affect the visibility and configurability of other parameters are shown in bold text. The options for the parameters that affect other parameters are shown as selected and cleared check boxes in the following row of the table. Parameters that are shown in plain text are enabled but do not affect other parameters. Parameters that are not enabled are not shown.

## **Solver Configuration Block Parameter Dependencies**

Row	Parameters and Options				
1	Start simulation from steady state				
2	Consistency toler	ance			
3	Use local Solver	,			
4					
5			Solver type	Solver type	
6			Sample time	Sample time	
7	Use fixed-cost runtime consistency iterations		Use fixed-cost runtime consistency iterations		
8					
9		Nonlinear iterations	Nonlinear iterations		
10		Mode iterations			
11	Linear Algebra				
12	Equation formulation				
13	Delay memory budget [kB]				
14	Apply filtering at 1-D/3-D connections when needed				
15					
16	Filtering time cor	nstant			

The figure shows the parameters that are visible by default on the block dialog box for the Solver Configuration block. The dimmed parameters, for example, **Solver type**, are not enabled.

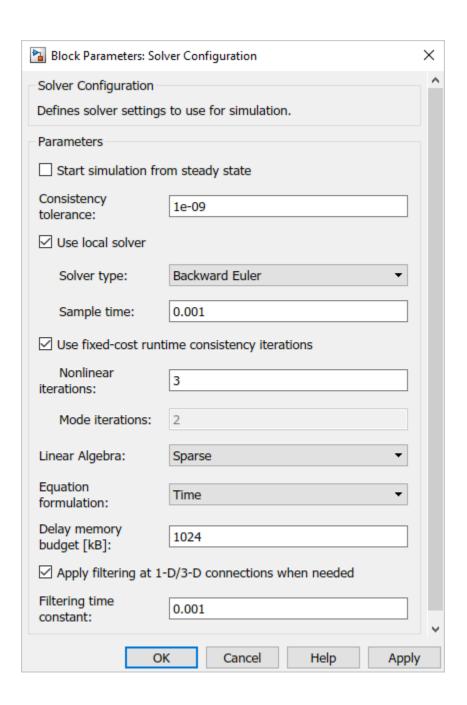


If you select the **Use local solver** check box, the **Use fixed-cost runtime consistency** check box becomes selected and these parameters become enabled.

- Solver type
- Nonlinear iterations
- Sample time

Selecting **Use local solver** does not enable the **Mode iterations** parameter. The **Mode iterations** parameter is only enabled when the **Use local solver** check box is cleared while **Use fixed-cost runtime consistency** check box is selected.

The table shows these dependencies in rows 3-10.



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